Abstract—In this paper we assess the transmission of a standard definition (SD) video over a 1000 m vertical time-varying underwater acoustic channel (UAC) using multiple-input multiple-output (MIMO) systems with spatial multiplexing gain. The MIMO systems are integrated with filter bank multi-carrier (FBMC) modulation and Orthogonal Frequency Division Multiplexing (OFDM) and their bit error rate (BER) performances are evaluated over the channel using preamble-based channel estimation. In this work we chose to use the FBMC system based on the Offset Quadrature Amplitude Modulation (OQAM) as it achieves maximum spectral efficiency. Simulation results show that MIMO-FBMC/OQAM provides a better error performance than MIMO-OFDM in the UAC, outlining its robustness against both time and frequency dispersions. Furthermore, the absence of a cyclic prefix (CP) in FBMC/OQAM implies that more useful bits can be transmitted per second, making it a better candidate than OFDM for transmitting real-time video with acceptable quality over a long acoustic link.

I. INTRODUCTION

Over the past few years, a number of applications such as marine-life exploration and oil spillage monitoring have made underwater acoustic (UWA) communication an active area of research. Some applications require high quality real-time underwater wireless video transmission but this is very challenging due to the limited bandwidth in an underwater acoustic channel (UAC). In order to cope with the physical limitations of the UAC and simultaneously achieve a high data rate, technologies such as multiple-input multiple-output (MIMO) and orthogonal frequency division multiplexing (OFDM) have been investigated for UWA communication (e.g., [1]).

The channel impulse response (CIR) in a UAC is often very long, especially in shallow water where the direction of transmission is horizontal with respect to the sea floor. For an OFDM-based system, the cyclic prefix (CP) duration should be at least equal to the length of the CIR to avoid intersymbol interference (ISI). Consequently, in order to maintain a high bandwidth efficiency, the OFDM symbol duration should be made very long [2]. However, the variations across each OFDM symbol in a fast time-varying channel will result in performance degradation due to intercarrier interference (ICI) caused by Doppler effect [2]. This drawback of OFDM has triggered research on another multi-carrier technique for UWA communication, namely filter bank multi-carrier (FBMC) modulation. The absence of a CP in FBMC implies that it offers a higher bandwidth efficiency than OFDM. Furthermore, in FBMC we can use filters which are well localized both in time and frequency to provide robust performance in doubly-dispersive UACs (e.g., [3]–[5]).
II. UAC CHARACTERISTICS

The UAC is often described in literature as the worst channel in use today since it is severely affected by factors such as high transmission loss, ambient noise, multipath distortion, high propagation delays and Doppler spreading. The combined effect of these factors significantly limits the available bandwidth and also makes it dependent on both distance and frequency [7]. Hence the bandwidth for long range acoustic links (> 1 km) is usually in the order of a few kHz.

The transmission loss for a distance $x$ and frequency $f$ is computed as follows [8]

$$A(x, f) = x^h \cdot \alpha(f)^r,$$  \hspace{1cm} (1)

where $\alpha(f)$ is the absorption coefficient which can be computed in dB/km for $f$ in kHz using the Thorp [9] or Fisher and Simmons [10] models and $k$ denotes the geometrical spreading factor with values of 1 and 2 for shallow and deep water respectively.

Ambient noise, which is often referred to as colored noise, is mainly caused by turbulence ($N_{tb}$), breaking waves ($N_w$), shipping ($N_s$) and thermal ($N_{th}$) noise sources. These are defined by the following equations ($f$ is in kHz) [8]

$$10\log N_{tb}(f) = 17 - 30\log(f),$$

$$10\log N_s(f) = 40 + 20(s - 0.5) + 26\log(f) - 60\log(f + 0.03),$$

$$10\log N_w(f) = 50 + 7.5w^{0.5} + 20\log(f) - 40\log(f + 0.4),$$

$$10\log N_{th}(f) = -15 + 20\log(f),$$  \hspace{1cm} (2)

where $s$ is the shipping factor with values between 0 and 1 for low and high activity respectively and $w$ is the speed of wind in m/s. The overall power spectral density (PSD) of the ambient noise is expressed as follows [8]

$$N_{psd}(f) = N_{tb}(f) + N_s(f) + N_w(f) + N_{th}(f).$$  \hspace{1cm} (3)

The speed of sound in water is about 200,000 times less than the speed of electromagnetic waves in air. Therefore the UAC experiences longer propagation delays than terrestrial radio links. A reasonable approximation of the speed of sound ($v$) in seawater as a function of the depth ($z$) in meters, temperature ($\theta$) in degrees Celsius, and salinity ($S$) in parts per thousand is as follows [11]

$$v = 1448.96 + 4.591\theta - 0.05304\theta^2 + 0.0002374\theta^3$$

$$+ 1.34(S - 35) + 0.0163z + 1.675 \times 10^{-7}z^2$$

$$- 0.001025\theta(S - 35) - 7.139 \times 10^{-13}\theta z^3.$$  \hspace{1cm} (4)

This equation is valid for $0 \leq \theta \leq 30^\circ$C, $30 \leq S \leq 40$ parts per thousand and $0 \leq z \leq 8000$ m.

The available bandwidth and transmission range for UWA communication depend on the signal-to-noise ratio (SNR) which is determined by the attenuation and noise level. The fact that the attenuation increases with frequency while the ambient noise decays with frequency makes the SNR vary over the signal bandwidth [7]. The SNR of an underwater acoustic signal can be expressed as follows [7]

$$SNR(x, f) = \frac{S_{tx}(f)}{N_{psd}(f).A(x, f)},$$  \hspace{1cm} (5)

where $S_{tx}(f)$ is the PSD of the transmitted signal.

The acoustic link can be classified as vertical or horizontal depending on the direction of the acoustic wave with respect to the sea floor. While carefully positioned vertical channels may exhibit long multipath delay spreads which can span over tens or even hundreds of milliseconds depending on the depth and distance between the transmitter and receiver [12]. The frequency response of the $r$th path in a multipath channel is expressed as [13]

$$H_r(f) = \frac{\Gamma_r}{\sqrt{A(x, f)}},$$  \hspace{1cm} (6)

where $x_r$ is the length of the $r$th path which can be calculated using plane geometry and $\Gamma_r$ is the cumulative reflection coefficient along the $r$th propagation path [7]. Given that each path has a delay $\tau_r$, the overall frequency response is expressed as [7]

$$H(f) = \sum_r H_r(f) e^{-j2\pi f\tau_r},$$  \hspace{1cm} (7)

and the impulse response is given by

$$h(t) = \sum_r h_r(t - \tau_r),$$  \hspace{1cm} (8)

where $h_r(t)$ is the inverse Fourier transform of $H_r(f)$.

A baseband model of the time-varying UAC with $N_{path}$ discrete multipath components can be represented as follows [8]

$$h(\tau, f) = \sum_{r=1}^{N_{path}} \Psi_r(\tau)\delta(\tau - |\tau_r - \xi_r|).$$  \hspace{1cm} (9)

where $\Psi_r(t)$ represents the time-varying amplitude of the $r$th path and $\xi = v_{rel}/v$ is a Doppler scale factor that can be applied to each path. $v_{rel}$ is the relative speed between the transmitter and receiver. If the underwater vehicle is moving a few m/s, this factor can be as high as $10^{-3}$ and hence the Doppler effect is regarded as non-negligible [7].

III. SYSTEM MODEL

A. Single-Input Single-Output (SISO)-FBMC/OQAM

In FBMC/OQAM, real PAM symbols are transmitted on each subcarrier and since the duration of the real symbols is half that of OFDM/QAM, we obtain the same spectral efficiency as with OFDM (without the CP). The orthogonality condition in FBMC/OQAM is relaxed to the real field and this allows pulse shaping filters which have good time and...
frequency localization to be used. The discrete-time transmitted FBCM/OQAM signal at the synthesis filter bank (SFB) output is given by [14]

\[
s(l) = \sum_{m=0}^{M-1} \sum_{n} d_{m,n} g(l-n) M \frac{2}{\pi} (\sinh \frac{t}{2}) e^{j\phi_{m,n}},
\]

where \( M \) is the number of subcarriers, \( d_{m,n} \) represent the OQAM symbols for the \( m \)th subcarrier and \( n \)th symbol time, \( \phi_{m,n} = \phi_0 + \frac{n}{2}(m+n) \mod \pi \) (\( \phi_0 \) can have an arbitrary value) and \( g \) is the impulse response of the prototype filter which has a length of \( L_g = KM \) for an overlapping factor of \( K \). It is to be noted that \( g_{m,n} \) is orthogonal only in the real field. Thus, imaginary interference is inherent in an FBMC/OQAM system and is expressed as [14]

\[
\sum_l g_{m,n}(l)g_{\ast p,q}(l) = j(g_{m,n})^{\ast p,q},
\]

where \((g_{m,n})^{\ast p,q} = -j(g_{m,n})_{p,q}\) and \((g_{m,n})_{p,q}\) is purely imaginary for \((m,n) \neq (p,q)\) [15]. If the number of subcarriers is large enough such that each subcarrier experiences flat fading and assuming that the channel is constant over the duration of the prototype filter, then the output of the analysis filter bank (AFB) at the \( p \)th subcarrier and \( q \)th FBMC/OQAM symbol can be represented as [14]

\[
y_{p,q} = H_{p,q} d_{p,q} + j \sum_{(m,n) \neq (p,q)} H_{m,n} d_{m,n} (g)_{m,n}^{p,q} + \eta_{p,q},
\]

where \( H_{p,q} \) is the channel frequency response (CFR), \( I_{p,q} \) and \( \eta_{p,q} \) are the interference and noise terms respectively. If a prototype filter which is well localized in time and frequency is used, it can be assumed that the interference is due to only the first-order neighbors of the frequency-time points (FT) \((p,q)\), i.e., \( \Omega_{p,q} = \{(p \pm 1, q \pm 1), (p, q \pm 1), (p \pm 1, q)\} \) [14]. Moreover, if the CFR is also constant over the first-order neighbors, the expression in (12) is approximated as follows [14]

\[
y_{p,q} \approx H_{p,q} c_{p,q} + \eta_{p,q},
\]

where

\[
c_{p,q} = d_{p,q} + j \sum_{(m,n) \in \Omega_{p,q}} d_{m,n} (g)_{m,n}^{p,q} = d_{p,q} + j u_{p,q},
\]

and

\[
u_{p,q} = \sum_{(m,n) \in \Omega_{p,q}} d_{m,n} (g)_{m,n}^{p,q}.
\]  

Fig. 1. 2 x \( N_r \) IAM-C preamble \((M=8)\) (a) Transmit Hydrophone 1 (b) Transmit Hydrophone 2

B. MIMO-FBCM/OQAM

The above concept can be easily applied to a MIMO system with \( N_t \) transmit and \( N_r \) receive hydrophones. Thus the signal at each receive hydrophone can be written as [14]

\[
y_{p,q} = H_{p,q} c_{p,q} + \eta_{p,q},
\]

where \( H_{p,q} \) is the \( M \)-point CFR from the \( i \)th transmit hydrophone to the \( j \)th receive hydrophone, \( c_{p,q} \) and \( \eta_{p,q} \) are the transmitted virtual symbol and noise respectively. The overall expression for a MIMO-FBMC/OQAM system is given by [14]

\[
y_{p,q} = \frac{1}{2} y_{p,q}[\eta_{p,q}]^{T},
\]

where

\[
y_{p,q} = \left[ y_{p,q} \ y_{p,q} \ ... \ y_{p,q} \right],
\]

\[
\eta_{p,q} = \left[ \eta_{p,q} \ \eta_{p,q} \ ... \ \eta_{p,q} \right]^{T},
\]

\[
H_{p,q} = \left[ H_{p,q}^{1,1} \ H_{p,q}^{1,2} \ ... \ H_{p,q}^{1,N_t} \right] \left[ H_{p,q}^{2,1} \ H_{p,q}^{2,2} \ ... \ H_{p,q}^{2,N_t} \right] ...
\]

The IAM-C (complex pilots) preamble proposed in [16] is used in this work. In order to estimate the CFR, we require at least \( 2N_t + 1 \) FBMC/OQAM symbol durations, while for MIMO-OFDM we would require \( N_t + \frac{1}{2} \) complex symbol durations [14]. An example of the IAM-C preamble structure for a \( 2 \times N_r \) MIMO system is shown in Fig. 1. The alternate zero vectors prevent the pilot vectors from being affected by interference from the data parts. By taking into account only the pilot vectors at timing instants \( q = 1,3 \), the expression in (18) can be re-written as follows [14]

\[
[y_{p,1} \ y_{p,3}] = H_{p,1} \left[ \eta_{p,1} \ \eta_{p,3} \right] + \left[ c_{p,1} \ c_{p,3} \right].
\]  

From the preamble structure in Fig. 1, one can notice that \( c_{p,1} = c_{p,3} = c_{p,2} = c_{p,3} = c_{p} \) and hence

\[
[y_{p,1} \ y_{p,3}] = H_{p,1} c_{p} Q_2 + \left[ \eta_{p,1} \ \eta_{p,3} \right],
\]

where \( Q_2 \) is a Hadamard matrix of order \( N_t \) (two in this case). An estimate of the CFR matrix at the \( p \)th subcarrier is thus given by [14]

\[
\hat{H}_{p,1} = \left[ y_{p,1} \ y_{p,3} \right] \frac{1}{c_{p}} Q_2^{-1}.
\]
TABLE I
CHANNEL PARAMETERS

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water depth</td>
<td>1000 m</td>
</tr>
<tr>
<td>Transmitter (TX) depth</td>
<td>999 m</td>
</tr>
<tr>
<td>Receiver (RX) depth</td>
<td>1 m</td>
</tr>
<tr>
<td>TX-RX Horizontal separation</td>
<td>5 m</td>
</tr>
<tr>
<td>Bandwidth</td>
<td>25 kHz</td>
</tr>
<tr>
<td>Carrier frequency</td>
<td>32.5 kHz</td>
</tr>
</tbody>
</table>

IV. PERFORMANCE EVALUATION

A. BER performance and bit rate

The vertical channel configuration parameters are given in Table I. It is assumed that the relative speed between the transmitter and receiver is 0.5 m/s. This may be caused by unintentional movement due to tides or sea currents. The maximum Doppler frequency in the UAC is approximately 11 Hz. The time-varying channel coefficients are obtained using a statistical model based on the maximum entropy principle [17] which only relies on a few parameters such as channel average power and Doppler spread to model. The channel impulse response (CIR) with a maximum delay spread of 2.6 ms and channel scattering function (CSF) as a function of delay ($\tau$) and Doppler ($\nu$) are shown in Fig. 2. The Doppler spread for the channel tap delays in Fig. 2 increases linearly from 0.5 Hz to 2 Hz. For the purpose of simulation, we used colored noise instead of additive white Gaussian noise (AWGN) since it better represents noise in an UAC. The simulation parameters for the MIMO-OFDM and FBMC/OQAM systems are summarized in Table II. Considering the same transmission time, the BER performances for the MIMO-OFDM and MIMO-FBMC/OQAM systems in the vertical UAC are shown in Fig. 3. Each frame of a $2 \times N_r$ FBMC/OQAM system consists of 5 real preamble symbols. As for the $4 \times N_r$ FBMC/OQAM system, each frame consists of 9 real preamble symbols. For the $2 \times N_r$ and $4 \times N_r$ OFDM systems, the preamble lengths are 2 and 4 complex symbol durations, respectively. A simple one-tap equalizer is used for the MIMO-OFDM system while the MIMO-FBMC/OQAM receiver processing consists of a 3-tap equalizer [18]. A Hermite prototype filter with an overlapping factor of 4 is used for the FBMC systems.

It is observed that both the coded and uncoded MIMO-FBMC/OQAM systems outperform the MIMO-OFDM systems. This shows the robustness of FBMC against both time and frequency dispersions. With 1/2 rate Turbo code, the BER performances of both systems are greatly improved. For instance, at a BER of $10^{-4}$, the Turbo-coded $2 \times 12$ and $4 \times 12$ FBMC/OQAM systems outperform the Turbo-coded OFDM systems by 4 dB in both cases.

For the bit rate computation, the parameters as given in Table II are assumed. The theoretical bit rates that can be achieved with the different systems in the 1000 m vertically configured UAC are given in Table III. For similar parameters, the $2 \times N_r$ and $4 \times N_r$ FBMC/OQAM systems achieve about 17% and 25% higher bit rate than the $2 \times N_r$ and $4 \times N_r$ OFDM systems respectively.

B. Video Transmission in an UAC

While MPEG-4 has been used for underwater wireless video transmission in UACs (e.g [19]–[21]) and has achieved real-time low resolution video transmission with satisfactory quality, more efficient video compression standards are available now. These include H.264 (MPEG-4 Part 10 AVC) and High Efficiency Video Coding (HEVC). In this work we consider the H.264/AVC standard for video compression ahead of High Efficiency Video Coding (HEVC). For the same bit rate, HEVC is known to achieve a better video quality than H.264/AVC. However, for a target bit rate HEVC uses a complex prediction process to remove the redundant information in the video and minimize the coding distortion [22]. Hence, it has a higher computational complexity than H.264/AVC and is more efficient when the video is encoded in non-real-time.
For the video transmission part we consider the Turbo-coded MIMO-FBMC/OQAM systems in Table III since they not only achieve higher bit rates than the MIMO-OFDM systems but also a better error performance. We consider an uncompressed standard definition (SD) video with a resolution of 640×480, frame rate of 30 fps and duration 12 s. The video stream (365 frames) is compressed to target bit rates of 70 kbps and 100 kbps for the $2 \times N_r$ and $4 \times N_r$ FBMC/OQAM systems respectively.

Frequent coding of the I-frames avoids propagation of errors between frames, thereby improving the error resilience of the video streams. Hence, a short intraperiod of 8 is used. The maximum packet size is set at 800 bytes and the number of reference frames for video coding is set at 5, which is adequate for practical implementations [23].

1) Frame Rate Computation: The average number of bits per frame for the video streams compressed at 70 kbps and 100 kbps are 2,355 and 3,364 respectively. It is to be noted that the I-frames consist of more bits than the P and/or B video frames. Assuming the maximum supported capacity of the systems, the calculated frame rate for the $2 \times N_r$ and $4 \times N_r$ FBMC/OQAM systems is 31.3 fps in both cases. This value is greater than the original frame rate of 30 fps, implying real-time transmission is theoretically feasible.

2) Packet Loss: The H.264/AVC bitstreams are encoded in 502 and 543 video packets for the $2 \times N_r$ and $4 \times N_r$ FBMC/OQAM systems respectively.

V. CONCLUSION

In this work we have seen that FBMC/OQAM provides a better error performance than OFDM in a time-varying UAC since it is based on a pulse-shaping filter with good time and frequency localization features. Furthermore, FBMC/OQAM achieves a higher bit rate than OFDM for the same bandwidth since it does not include a CP. High data rates are desirable
for modern underwater applications involving wireless video transmission. The bit rates obtained with the FBMC/OQAM systems over the 1000 m vertical acoustic link are sufficiently high to transmit a video with acceptable quality in real-time.

REFERENCES