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Reconstructing Paleosalinity from $\delta^{18}$O: Coupled model simulations of the Last Glacial Maximum, Last Interglacial and Late Holocene

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Abstract

Reconstructions of salinity are used to diagnose changes in the hydrological cycle and ocean circulation. A widely used method of determining past salinity uses oxygen isotope ($\delta_{Ow}$) residuals after the extraction of the global ice volume and temperature components. This method relies on a constant relationship between $\delta_{Ow}$ and salinity throughout time. Here we use an isotope-enabled fully coupled General Circulation Model (GCM) to test the application of spatially and time-independent relationships in the reconstruction of past ocean salinity. Simulations of the Late Holocene (LH), Last Glacial Maximum (LGM), and Last Interglacial (LIG) climates are performed and benchmarked against existing compilations of stable oxygen isotopes in carbonates ($\delta_{Oc}$), which primarily reflect $\delta_{Ow}$ and temperature. We summarise that HadCM3 produces an accurate representation of the surface ocean $\delta_{Oc}$ distribution for the LH and LGM. Our simulations show considerable variability in spatial and temporal $\delta_{Ow}$-salinity relationships. We show that spatial gradients are generally shallower but within $\sim 50\%$ of the actual simulated LH to LGM and LH to LIG temporal gradients and temporal gradients calculated from multi-decadal variability are generally shallower than both spatial and actual simulated gradients. The largest sources of uncertainty in salinity reconstructions are found to be caused by changes in regional freshwater budgets, ocean circulation, and sea ice regimes. These can cause errors in salinity estimates exceeding 4 psu. Our results suggest that paleosalinity reconstructions in the South Atlantic, Indian and Tropical Pacific Oceans should be most robust, since these regions exhibit relatively constant $\delta_{Ow}$-salinity relationships across spatial and temporal scales. Largest uncertainties will affect North Atlantic and high latitude paleosalinity reconstructions. Finally, the results show that it is difficult to generate reliable salinity estimates for regions of dynamic oceanography, such as the North Atlantic, without additional constraints.

Keywords: Paleosalinity, isotopes, oxygen-18, Last Glacial Maximum, Last Interglacial,
1. Introduction

Discussion of past and future climate change is often difficult without reference to the oceanic global thermohaline circulation, a wind and density driven circulation of mass, heat and salt (Wunsch, 2002; Munk and Wunsch, 1998; Ferrari and Ferreira, 2011). The transition between cold glacial and warm interglacial periods has been linked to large changes in global ocean density structure (Adkins, 2013). At a given pressure, density is determined by seawater temperature and salinity via the equation of state. Patterns of ocean surface salinity also reflect patterns of surface water fluxes (evaporation and precipitation [E-P]) and have therefore been used to fingerprint changes in the global water cycle (e.g. Durack et al., 2012). Knowledge of past salinity is therefore important to characterise ocean circulation (Boyle, 2002; Adkins et al., 2002) as well as provide information on regional changes in hydrology (Stott et al., 2004; Durack et al., 2012). Although salinity can be measured in the modern ocean with very high accuracy, there are no direct measurements of past salinity before the historical era (Bingham, 2002). Thus, reconstructing past salinity changes in the ocean usually relies on proxies developed in marine sediment cores combined with a modern empirical calibration (Rohling and Bigg, 1998).

Oxygen stable isotopes ($\delta^{18}O$ reported in units of $\%_{oo}$ with respect to Vienna standard mean ocean water [VSMOW]) are a common tool in paleoceanography (e.g. Shackleton, 1974; Fairbanks, 1989; Broecker, 1989; Duplessy et al., 1993). Local changes in the $\delta^{18}O$ composition of seawater ($\delta_{Ow}$) tend to be dependent on changes in freshwater and ocean circulation (Waelbroeck et al., 2014; Duplessy et al., 1991; Delaygue et al., 2001; Benway and Mix, 2004; LeGrande and Schmidt, 2006; Abe et al., 2009; Munksgaard et al., 2012). Hence, $\delta_{Ow}$ provides information about salinity changes and is indeed sometimes incorrectly called the ‘salinity effect’, given the tight coupling between salinity and $\delta_{Ow}$ (Delaygue et al., 2000, 2001; Rohling and Bigg, 1998; Rohling, 2000). On timescales relevant for ice sheet processes, a global ice volume effect (known as the glacial effect) also influences $\delta_{Ow}$ due to storage of the lighter isotope ($^{16}O$) in ice sheets. Global $\delta_{Ow}$ can therefore be used to reconstruct past global ice volume (Shackleton, 1967; Labeyrie et al., 1987; Fairbanks, 1989).

The $\delta_{Ow}$ of past seawater is not directly measurable. However, the $\delta^{18}O$ of CaCO$_3$ in shells ($\delta_{OC}$) can be measured from current and old foraminifera recovered from marine sediment cores (e.g. Shackleton, 1974; Fairbanks, 1989; Broecker, 1989). Values of $\delta_{OC}$ are dependent on $\delta_{Ow}$, seawater temperature, and
species-specific offsets. Therefore, after species-specific corrections, measurements of $\delta_{Oc}$ can be used to reconstruct past seawater temperature if $\delta_{Ow}$ is known, or alternatively past $\delta_{Ow}$ can be reconstructed if temperature can be independently constrained (Waelbroeck et al., 2014). An ongoing challenge in paleoceanography has therefore been to separate $\delta_{Oc}$ into its individual temperature and $\delta_{Ow}$ components (Shackleton, 1967; Labeyrie et al., 1987; Chappell and Shackleton, 1986; Broecker, 1989; Cutler et al., 2003).

The $\delta_{Ow}$ residual method is the most commonly used approach for paleosalinity reconstruction (Rohling and Bigg, 1998; Rohling, 2000). This method assumes that, once a $\delta_{Ow}$ signal has been corrected for changes in global ice volume and the temperature signal has been independently constrained, the remaining $\delta_{Ow}$ anomaly relates linearly to changes in ocean salinity via a calibration between modern $\delta_{Ow}$ and salinity (e.g. Rostek et al., 1993; Weldeab, 2012; Hennissen et al., 2014; Broecker, 1989; Duplessy et al., 1991, 1993; Schmidt, 1999b; Duplessy et al., 1991). Early attempts to reconstruct paleosalinity assumed a globally uniform linear salinity versus $\delta_{Ow}$ gradient. A linear regression between modern salinity and $\delta_{Ow}$ measurements suggested a 0.5‰ increase in $\delta_{Ow}$ for a 1 psu increase in salinity (Craig and Gordon, 1965; Broecker, 1989; Duplessy et al., 1993). Although this gradient may be representative of a global average (Schmidt, 1999b), additional measurements of surface ocean properties have demonstrated that considerable geographical variability exists in this relationship (e.g. LeGrande and Schmidt, 2006; Conroy et al., 2014; Delaygue et al., 2001; McConnell et al., 2009; Bigg and Rohling, 2000; Schmidt, 1999a).

As these calibrations are generally derived under present day conditions (Schmidt, 1999a), they thus rely on the assumption that the controls on the proxy relationship have not changed through the past. This is known as the stationary assumption and is arguably the largest uncertainty in the use of modern proxy relationships (Stott et al., 2004; Rohling, 2000; LeGrande and Schmidt, 2011; Furtado et al., 2009). For example, measurements and model output suggest that the $\delta_{Ow}$-salinity gradient can vary significantly over time due to local changes in sea ice cover, ocean circulation, and individual terms in the freshwater budget, such as local changes in the $\delta^{18}O$ of precipitation (e.g. Frew et al., 2000, 1995; Schmidt et al., 2007; LeGrande and Schmidt, 2011; Schmidt, 1999a; Leduc et al., 2013; Conroy et al., 2014; Rohling and Bigg, 1998; Benway and Mix, 2004). Further investigations are thus needed to test the validity of the stationary assumption.

Isotope enabled general circulation models (GCMs) allow isotopic variations to be interpreted beyond traditional single parameter reconstructions. The array of timescales accessible to models enables the sta-
tionary assumption to be rigorously tested. Isotope-enabled simulations have been used to reproduce the present-day climate (Tindall et al., 2009; Noone and Simmonds, 2002; Lee et al., 2007; Werner et al., 2011) as well as past climates, including warm interglacials (Schmidt et al., 2007; LeGrande and Schmidt, 2011; Masson-Delmotte et al., 2011; Sime et al., 2009, 2013; Tindall et al., 2010), and cold glacial climates, such as the Last Glacial Maximum (Lee et al., 2008; Roche et al., 2004; Caley et al., 2014). Indeed, the interpretation of surface temperature from ice core isotopic records has benefitted from isotope-enabled atmospheric GCMs (e.g. Noone and Simmonds, 2002; Jouzel et al., 2003; Sime et al., 2008, 2009, 2013; Masson-Delmotte et al., 2011). The inclusion of isotope tracers into oceanic GCMs has led to similar investigation of the relationship between seawater isotopes and salinity (e.g. Schmidt, 1999b; Delaygue et al., 2000). The δOw-salinity relationship is a key test for fully coupled isotope modelling and has been used to explore the validity of the stationary assumption in response to changes in orbital forcing (Schmidt et al., 2007; LeGrande and Schmidt, 2011). However, holes still exist in the scope of timescales invested; paleosalinity modelling investigations have primarily focussed on warm interglacial periods (e.g. Schmidt et al., 2007; LeGrande and Schmidt, 2006, 2011; Tindall and Haywood, submitted; Russon et al., 2013). Therefore, the question of whether uncertainties are similar during periods of drastically different boundary conditions, such as glacial periods, is still very much open.

Here we explore the δOc, δOw, and salinity relationships using a set of water isotope (δOw) enabled paleoclimate simulations. The simulations cover the key Last Glacial Maximum period, when major changes in the thermohaline circulation affected climate (Adkins, 2013; Adkins et al., 2002; Annan and Hargreaves, 2013; Ruddiman et al., 1984; Clark et al., 2009; MARGO Project Members, 2009), and the Last Interglacial period, the last climatic period with higher than present sea level (Kopp et al., 2009, 2013) and warmer than present temperatures (IPCC, 2013; Turney and Jones, 2010; Capron et al., 2014). The simulations enable us to characterise the magnitude of uncertainty induced by assumptions of geographical uniformity and stationarity. We outline the design of the model experiments and compare simulated ocean isotopes against observed δOc records. We then examine the relationships between δOw and salinity and test the application of spatially and time-independent relationships in the reconstruction of past ocean salinity; i.e. how large could errors in reconstructions of salinity over time be, if a gradient determined from the modern spatial δOw-salinity distribution were to be used? The implications of our results, in terms of possible changes in the δOw-salinity relationship through time, are then discussed.
2. Materials and Methods

2.1. Model Description

Experiments are set up using an isotope-enabled version of the Hadley Centre Coupled Model, version 3 (HadCM3) GCM. HadCM3 consists of a linked atmosphere, ocean and sea ice model and has been widely used to study past, present and future climates (e.g. Solomon et al., 2007; IPCC, 2013). The ocean component of HadCM3 is a rigid lid model based on Cox (1984). The ocean has a fixed volume and the model conserves water through salinity conservation. This study uses the isotope-enabled version of HadCM3 to investigate links between $\delta^{18}O$ and salinity. For a detailed description of the implementation of isotopes into HadCM3, the reader is referred to Tindall et al. (2009). Ice sheets and sea ice in the model are initialised with a $\delta^{18}O$ value of -40 and -2 $^\circ/o$, respectively. The isotope component of HadCM3 ignores the small fractionation associated with sea ice processes and thus makes the approximation that sea ice melting/formation is non-fractionating (Tindall et al., 2009; Pfirman et al., 2004).

Model temperature and salinity have been evaluated in previous work for the modern climate (Gordon et al., 2000; Pardaens et al., 2003). Pardaens et al. (2003) concluded that the global hydrological cycle is well represented by the model, although its strength is overestimated compared to observations. Pardaens et al. (2003) observe a drift towards a more saline Atlantic Ocean throughout the simulation due to an overestimate of local evaporation. Gordon et al. (2000) evaluated the coupled model simulation of sea surface temperature (SST), sea ice and ocean heat transport, concluding a good representation, in broad agreement with observed estimates. A good balance between the ocean and atmosphere heat budgets results in no large SST drift and, consequently, no heat flux adjustments are required in HadCM3 (Gordon et al., 2000). Although there are drifts in salinity (<0.1 psu/100 years), the magnitude does not significantly effect the ocean circulation and thus do not impact on the coupled ocean-atmosphere simulation of climate (Gordon et al., 2000).

Isotopic output has been validated for both the atmosphere only (Sime et al., 2008) and the coupled ocean-atmosphere model (Tindall et al., 2009, 2010; Xinping et al., 2012). Isotopic output has been compared against the Global Network of Isotopes in Precipitation (GNIP) observational database (Tindall et al., 2009; Xinping et al., 2012), the Masson-Delmotte et al. (2008) 20th century Antarctic surface snow $\delta^{18}O$ dataset (Sime et al., 2008), and the Waelbroeck et al. (2005) dataset of Late Holocene planktic foraminifera $\delta_{Oc}$ (Tindall et al., 2010). Modelled isotope output captures the general spatial distribution of isotopes, including the latitude effect, amount effect, continental effect, and altitude effect, and is in good agreement
with present-day observations (Tindall et al., 2009; Sime et al., 2008). Modelled ocean isotopes have been combined with model temperature output to compute $\delta_{oc}$ and used to interpret pre-industrial coral (Russon et al., 2013) and ocean core records (Tindall et al., 2010). $\delta_{ow}$ has been converted to $\delta_{oc}$ using a variety of calibration equations and compared to ocean core top values, reproducing a zonal pattern that is in good agreement with data regardless of the chosen calibration equation (Tindall et al., 2010). The isotope component of HadCM3 has previously been used to investigate paleoclimates including the last interglacial (Sime et al., 2009, 2013), the Eocene (Tindall et al., 2010), the Pliocene (Tindall and Haywood, submitted), as well as periods of abrupt climate change (Tindall and Valdes, 2011).

### 2.2. Model Simulations

A Late-Holocene control simulation (hereafter LH) was run along with two sensitivity experiments; representing the period 21 thousand years BP (ka) and 125 ka. The period 21 ka represents the peak of the last glacial period, or the Last Glacial Maximum (hereafter LGM), a period of global cold and maximum ice sheet extent relative to the last glacial cycle (Adkins, 2013; Adkins et al., 2002; Annan and Hargreaves, 2013; Ruddiman et al., 1984; Clark et al., 2009; MARGO Project Members, 2009). In contrast, the period 125 ka corresponds to a minimum in global ice volume and characterises a period of global warmth during the last interglacial (hereafter LIG) (Dutton and Lambeck, 2012; Kukla et al., 2002; Shackleton et al., 2002; IPCC, 2013; Turney and Jones, 2010; Capron et al., 2014).

HadCM3 does not include interactive ice sheets, carbon cycle, or methane. Any changes in orbit, GHG, dust, ozone and ice sheet evolution must be prescribed. The prescribed boundary conditions for each model integration are outlined in Table 1. Our LH simulation was set up following pre-industrial control guidelines from the Paleoclimate Model Intercomparison Project (PMIP), with atmospheric gas composition set to values for 1850 years BP (CO$_2$ is 280 ppmv; CH$_4$ is 760 ppbv; and N$_2$O is 270 ppbv). Paleo changes in orbit and GHG concentrations are relatively well constrained. We adopt the same boundary forcing as applied by Singarayer and Valdes (2010) (see Table 1 for details). Sea level reconstructions suggest that sea levels were $\sim$6 m higher than present during the last interglacial (Kopp et al., 2009, 2013). There is still large uncertainty as to the source and timing of this additional sea level contribution, with contributions likely from both Greenland and Antarctica (IPCC, 2013). Considering the magnitude of the sea level anomaly relative to the resolution of HadCM3, we follow the approach of Singarayer and Valdes (2010) and apply no ice sheet anomaly to our LIG simulation. For the LGM simulation, data suggest a roughly 120 m drop in sea level (Fairbanks, 1989). Again following Singarayer and Valdes (2010), we apply an LGM
ice sheet configuration based on the ICE-5G model (Peltier, 2004) used in the PMIP Phase 2 (PMIP2; https://pmip2.lsce.ipsl.fr/pmip2/, Braconnot et al., 2007) and a number of simulations included in PMIP3 (http://pmip3.lsce.ipsl.fr/).

Isotopes are added to simulations with climates that have already been spun up with the respective boundary conditions. All of our simulations are initialised with an isotopic value of 0 $\%_{oo}$ for $\delta^{18}$O in the atmosphere and ocean. Once isotopes had been initialised, the LH and LIG simulations were integrated for a total of 600 years and the LGM for 800 years. By the end of all three simulations, surface and deep ocean $\delta_{ow}$ changes by $<0.01 \%_{oo}$/100 years.

Table 2.3. Reconstructing salinity from $\delta_{ow}$ residuals

To use $\delta^{18}$O as a proxy for spatial or temporal paleo-climate reconstruction, the relationship between the proxy and the desired, but unobservable, variable is often defined by the gradient of a linear relationship (e.g. Sime et al., 2008). For example, in the case of salinity, where $\delta_{ow}$ is the proxy and salinity ($S$) is the target variable, this would take the form $\delta_{ow} = \alpha S + b$, where the gradient $\alpha = \Delta \delta_{ow}/\Delta S$. By definition of the linear relationship, the intercept value, $b$, is an indicator of the freshwater end-member ($\delta_F$), defined as the value of $\delta_{ow}$ when $S=0$ (Delaygue et al., 2001; LeGrande and Schmidt, 2006; Munksgaard et al., 2012).

The slope of the relationship, $\alpha$, can be applied to spatial or temporal $\delta_{ow}$ and $S$ observations to obtain either a spatial or temporal gradient; i.e. by selecting either a stationary point in time and observing the co-variability of $\delta_{ow}$ and salinity across a defined spatial domain (the spatial gradient) or selecting a stationary point in space and observing the co-variability of $\delta_{ow}$ and salinity at that location with time (the temporal gradient). The gradient of the linear regression between spatial or temporal $\delta_{ow}$ and $S$ is defined as $\alpha_{SPACE}$ and $\alpha_{TIME}$ respectively. Changes to the temporal gradient are therefore; $\Delta \alpha_{TIME} = \partial \alpha / \partial t$ at a single point, where $t$ is time, and changes in the spatial gradient are; $\Delta \alpha_{SPACE} = \partial \alpha / \partial x$ at a single time, where $x$ is a geographic location. The value of $\alpha_{SPACE}$ can be measured in modern ocean water and is the value that is traditionally applied when reconstructing past oceanographic changes, assuming that the spatial and temporal relationships are the same, i.e. $\alpha_{SPACE} = \alpha_{TIME}$.

In order to define a measure of $\alpha_{TIME}$ for each simulation, the methodology is applied to decadally averaged $\delta_{ow}$ and salinity output and defined as $\alpha_{DECADAL}$. To assess the temporal variability of the $\delta_{ow}$-salinity relationship on long timescales, i.e. between simulations, $\alpha_{SLICE}$ is defined as; $\alpha_{SLICE}^{LGM-LH} = (\delta_{ow}^{LGM} - \delta_{ow}^{LH}) / (S_{LGM} - S_{LH})$ and similarly for $\alpha_{SLICE}^{LIG-LH}$. Values of $\alpha_{SLICE}$ are calculated by averaging $S$ and $\delta_{ow}$ over the final 100 years of each simulation. $\alpha_{SLICE}$ represents the ‘real’ value for $\alpha$ (in model world) between the two climates and
using this gradient will produce accurate estimates of past salinity. Therefore, because we only observe 
\( \alpha^{SPACE} \) (and to a lesser extent \( \alpha^{DECADAL} \)) in the modern ocean, a perfect estimate of past salinity could be provided by the \( \delta_{Ow} \) residual method if \( \alpha^{SPACE} = \alpha^{DECADAL} = \alpha^{SLICE} \). Here, we test the extent to which this is true in model world. In the following sections we quantify the spatial and temporal bias in inferred salinity by evaluating the \( \delta_{Ow}-\text{salinity gradient during the LH, LGM and LIG, using the notation; } \alpha^{SPACE}_{LH}, \alpha^{SPACE}_{LGM} \) and \( \alpha^{SPACE}_{LIG} \) for spatial trends; \( \alpha^{DECADAL}_{LH}, \alpha^{DECADAL}_{LGM} \) and \( \alpha^{DECADAL}_{LIG} \) for intrinsic multi-decadal variability; and \( \alpha^{SLICE}_{LGM-LH} \) and \( \alpha^{SLICE}_{LIG-LH} \) to represent the simulated \( \delta_{Ow}-\text{salinity relationship on long glacial-interglacial timescales.} \\

3. Results

3.1. Benchmarking modelled \( \delta_{Ow} \)

The performance of the isotope-enabled HadCM3 is first evaluated against the patterns observed in marine sediment core \( \delta_{Oc} \) records. We focus our benchmarking on the LH and LGM simulations as these time periods have most data coverage, can be accurately dated using \( ^{14}C \), and have sufficient confidence levels on the data (Waelbroeck et al., 2005; MARGO Project Members, 2009; Waelbroeck et al., 2014; Caley et al., 2014).

To compare with marine sediment core foraminiferal calcite, modelled \( \delta_{Ow} \) is converted to \( \delta_{Oc} \) using the quadratic approximation of O’Neil et al. (1969), given in Shackleton (1974). Assuming that calcification temperature can be approximated by sea water temperature, modelled \( \delta_{Ow} \) and ocean temperature (\( T \)) fields are used from the top model layer (0-5 m) to invert for \( \delta_{Oc} \):

\[
\delta_{Oc} = \delta_{Ow} - 0.27 + 21.9 - \sqrt{310.6 + 10T}
\]

The factor -0.27 is the conversion between scales, from SMOW to PDB, according to Hut (1987) \( (\delta_{Ow} [VPDB] = \delta_{Ow} [VSMOW] - 0.27) \). We recognise that the use of surface ocean properties will introduce bias when comparing to observed \( \delta_{Oc} \) due to the variable depth habitat of different species of planktonic foraminifera. However, we find the choice of surface ocean depth has only minor affect on the following comparison. For comparative statistics, modelled \( \delta_{Oc} \) is taken from the nearest model grid point to the equivalent ocean core location. This means that our comparison is weighted to the non-uniform geographic distribution of available measurements.

We compare modelled surface ocean \( \delta_{Oc} \) against planktonic foraminifer calcite \( \delta_{Oc} \) (Figure 1). The LH simulation is compared against the Late Holocene data synthesis of Waelbroeck et al. (2005). This synthesis
forms a Late Holocene time slice as part of the Multiproxy Approach for the Reconstruction of the Glacial Ocean surface (MARGO) project (MARGO Project Members, 2009) and is chronologically defined as the last 4 ka. For the LGM, modelled $\delta_{Oc}$ anomalies are compared against the compilation of Caley et al. (2014). Caley et al. (2014) report anomalies as the difference between mean $\delta_{Oc}$ between 19-23 ka for the LGM and the last 3 ka for the LH.

Figure 1 shows a strong latitudinal trend in both modelled and observed $\delta_{Oc}$. Values are enriched in high latitude oceans and become progressively depleted towards the equator. This trend reflects the temperature dependent fractionation of calcification, approximately equalling a 0.2 $^\circ$/oo depletion per °C increase in temperature (O’Neil et al., 1969). Consequently, the inverse of $\delta_{Oc}$ closely approximates the meridional temperature gradient of surface waters. A strong temperature dependence is also evident in LGM $\delta_{Oc}$ anomalies, which, after subtracting the glacial effect of 1 $^\circ$/oo (see section 3.1.3.; Schrag et al., 1996; Adkins et al., 2002; Duplessy et al., 2002; Schrag et al., 2002), are positive over much of the global surface ocean, reflecting cooler glacial sea surface temperatures. In contrast, LGM $\delta_{Oc}$ anomalies are negative in the high latitude Arctic. Meteoric waters, which feed surface and subsurface runoff, are more depleted than surface ocean $\delta_{Ow}$. During the LGM, high-latitude meteoric waters are significantly more depleted than during the LH and, consequently, act to deplete $\delta_{Ow}$ in the surface ocean. This effect is amplified close to Arctic coastlines due the direct influence of glacial runoff. Therefore, strong negative $\delta_{Oc}$ anomalies around the peripheries of the Eurasian ice sheet reflect highly depleted surface water $\delta_{Ow}$.

Overall for the Late Holocene, planktonic foraminifera data compare well with modelled surface $\delta_{Oc}$, producing a Root Mean Squared Error (RMSE) of 0.82 $^\circ$/oo. A small negative bias is evident from modelled $\delta_{Oc}$, with a Mean Bias Error (MBE) of -0.27 $^\circ$/oo. This bias is significant in the mid-latitudes of the North Atlantic, where the model is more depleted than observations (Figure 1). However, modelled $\delta_{Oc}$ shows a small positive bias in the Greenland, Iceland, Norwegian (GIN) seas and the Arctic Ocean, where modelled $\delta_{Oc}$ values are more enriched than planktonic foraminifera $\delta_{Oc}$. The Waelbroeck et al. (2005) dataset was chosen as it provides the largest spatial coverage. More recent Late Holocene syntheses have been modified to increase the data confidence but this also reduces the quantity of data points (e.g. Waelbroeck et al., 2014; Caley et al., 2014). Comparing the model to more recent compilations improves the RMSE to 0.66 and 0.77 $^\circ$/oo for the Waelbroeck et al. (2014) and Caley et al. (2014) Late Holocene datasets respectively, but provides less information about spatial patterns. Waelbroeck et al. (2005) state the $\delta_{Oc}$ composition of fossil foraminifera in the MARGO dataset to be 0.2-0.8 $^\circ$/oo more enriched than that of living foraminifera.
This bias is related to the stratification of upper ocean waters and decreases with latitude (Waelbroeck et al., 2005). This offset could in part explain the small negative bias observed in modelled LH $\delta _{Oc}$ ($-0.24 \%_o$).

For the LGM, the model again compares well with observed $\delta _{Oc}$ anomalies and produces a smaller RMSE of 0.61 %o. Subtraction of the glacial effect removes most of the model bias for the glacial climate (MBE = -0.07 %o). An ongoing paleoclimate debate surrounds the disagreement between models and data regarding the glacial North Atlantic zonal $\delta _{Oc}$ gradient (Braconnot et al., 2007; MARGO Project Members, 2009). The model simulates strongly enriched LGM $\delta _{Oc}$ in the western Atlantic, decreasing towards the east. Once the data has been corrected for the global ice volume effect, observed anomalies are closer to zero in the west and increase towards the east. Similarly large positive model anomalies are observed in the North Pacific, associated with changes in the Kuroshio Current. However, a lack of data coverage in the central North Pacific precludes any assessment of this feature's accuracy. In the North Atlantic, the large positive anomalies during the LGM are associated with a southward shift of the Gulf Stream and intensification of the Subpolar Gyre. This region is no longer characterised by warm waters advected from the Florida Coast and is instead replaced by a strong Labrador Current advecting cold waters from the north. The positive $\delta _{Oc}$ anomalies therefore reflect surface ocean cooling. The model disagreement with marine core $\delta _{Oc}$ may thus be due to a poor simulation of the glacial Gulf Stream. Previous work has noted the stronger and more zonal Gulf Stream simulated by HadCM3 during the LGM (Hewitt et al., 2003), which is in disagreement with some reconstructions (e.g. Lynch-Stieglitz et al., 1999).

For the LH, a significant model-data disagreement exists in the GIN seas and the high latitude Arctic. Foraminiferal blooms in these regions will be strongly seasonal due to light limitation. Schmidt and Mulitza (2002) found the standard error of modelled coretop $\delta _{Oc}$ decreased from 1.2 %o, when assuming annual average mixed layer equilibrium calcite, to 0.53 %o, when combined with their ecological model, including parameters for species temperature ranges, optimum temperatures, depth habitat, and amount of secondary calcification. Our model calculated $\delta _{Oc}$ does not account for these factors. However, observed $\delta _{Oc}$ values can be compared against simulated summer $\delta _{Oc}$ (JJA for the northern hemisphere and DJF for the southern hemisphere) to test the effect of seasonality, assuming that $\delta _{Oc}$ is primarily a summer signal. Using simulated summer $\delta _{Oc}$ has negligible effect on the LGM comparison (RMSE and MBE of 0.58 and -0.09 %o respectively) and slightly worsens the LH comparison (RMSE and MBE of 0.96 and -0.54 %o respectively). Other areas of model-data disagreement are concentrated in regions of dynamic oceanography and sharp oceanographic fronts. Model resolution limits the accurate simulation of $\delta _{Oc}$ in regions such as the North
Atlantic and regions characterising water mass boundaries due to the presence of sharp property gradients. This considered, the model appears to simulate a polar front extent that largely agrees with the data in the North Atlantic and the Atlantic sector of the Southern Ocean, indicated by sharp horizontal gradients in δ\text{Oc}. Despite local discrepancies, the model-data comparison suggests a good overall representation of Late-Holocene and LGM δ\text{Oc} simulated by the isotope-enabled HadCM3 model.

Although a compilation of δ\text{Oc} is not available for the LIG, the model suggests a similar surface ocean δ\text{Oc} distribution between the LIG and LH (Figure 1 bottom panels). LIG δ\text{Oc} is slightly more enriched in the tropics in response to the higher obliquity component during the LIG, and slightly more depleted around the coast of Greenland, reflecting changes in sea ice regime in response to the higher summer insolation.

3.1.1. The glacial effect

The bias between the LGM modelled and observed δ\text{Oc} for the surface ocean can in part be explained by the uncertainty in quantifying the glacial effect (Δδ\text{g}). The precise value of the glacial effect is not well constrained. Early work suggested an enrichment of Δδ\text{g} = 0.012z_{sl} ± 0.001‰/oo, where z_{sl} is the sea level drop in meters (Labeyrie et al., 1987; Shackleton, 1987; Fairbanks, 1989; Rohling, 2000). The uncertainty suggests a range for Δδ\text{g} of 1.32 to 1.56 ‰/oo for a 120 m drop in sea level. However, Schrag et al. (1996) argued that Δδ\text{g} = 0.008z_{sl} is more appropriate. More recently, a number of approaches have converged towards the latter estimate, establishing a mean ocean δ\text{Ow} enrichment for the LGM of 1.0 ± 0.1 ‰/oo (Schrag et al., 1996; Adkins et al., 2002; Duplessy et al., 2002; Schrag et al., 2002). The full uncertainty in Δδ\text{g} is difficult to constrain, particularly because it is influenced by the size and isotopic composition of glacial reservoirs (Sima et al., 2006).

Because the model simulations were initialised with a δ\text{Ow} value of 0 ‰/oo, the discrepancy between modelled and observed δ\text{Oc} can be used to suggest a model ‘best fit’ value for the glacial effect (e.g. Thresher, 2004), if we assume an otherwise perfect simulation of LGM δ\text{Oc} and that the uncertainty in Δδ\text{g} is the only cause of model-data disagreement. The mean data-model error for the LGM provides a value for the glacial effect; Δδ\text{g} = (∑_\text{d} − ∑_\text{m}) where ∑_\text{d} and ∑_\text{m} are the mean LGM data and model isotopic composition at the core site locations respectively. Dividing Δδ\text{g} by the inferred sea level fall in meters then gives a value for the glacial enrichment per meter of sea level change; i.e. η = Δδ\text{g}/z_{sl}, where η is the value for the isotopic enrichment per meter of sea level lowering. Solving this relation for the planktonic LGM data produces a value for Δδ\text{g} of 1.08 ‰/oo, and a value of η of 0.009 ‰/oo/m for both annual average and summer-only modelled δ\text{Oc}. This value of Δδ\text{g} sits between the range of previously suggested LGM glacial enrichments,
of 0.9 to 1.56 %/oo.

3.2. Paleosalinity - δOw residual method

In this section, the methodology set out in section 2.3. is applied to model salinity and δOw output to evaluate both spatial (αSPACE) and temporal (αDECADAL and αSLICE) relationships. We first assess the regional patterns of αSPACE for the LH followed by the variability in the δOw-salinity relationship during the LGM and LIG.

3.2.1. Spatial variability in the δOw-salinity relationship

Modelled LH αSPACE is compared to present-day observations from the Global Seawater Oxygen-18 Database (Schmidt, 1999b; Bigg and Rohling, 2000, http://data.giss.nasa.gov/o18data/) (Figure 2). Enclosed seas are masked for the comparison. Modelled regional δOw-salinity relationships for each simulation are presented in Table 2, including the gradient (αSPACE), the intercept (δF) and associated r² values from the spatial least squares linear regression.

Variability in salinity and δOw is larger in the observations than the model (Figure 2). This will in part be due to model resolution smoothing out variability and, even though enclosed seas have been masked, most of the observations lie in coastal regions affected by fresh and depleted continental and river runoff. Observed gradients decrease in most regions when data within one grid cell of the coastlines are masked (not shown). Including all model grid points within each region, and not only where observations are available, HadCM3 simulates an open ocean (excluding marginal seas, the Arctic Ocean poleward of 60°N and the Southern Ocean poleward of 60°S) αSPACE of 0.18 %/oo/psu for the LH (data 0.23 %/oo/psu). If all observed and modelled ocean data are included in the analysis, δF becomes more depleted (from -8 to -13 and -6 to -7 %/oo for the observations and model respectively) and the gradients steepen (from 0.23 to 0.38 and 0.18 to 0.21 %/oo/psu respectively). The simulated values lie within previous estimates of the δOw-salinity gradient and intercept for the major ocean basins (LeGrande and Schmidt, 2006). In the Southern Ocean, the freshwater endmember is less depleted than other regions as it trends towards the value of sea ice melt water, prescribed in the model as -2 %/oo (Table 2; Southern Ocean LH δF = -2.45 %/oo). This effect, plus the over-active hydrological cycle in HadCM3 (Pardaens et al., 2003), helps explain the shallow gradients simulated in mid and high-latitudes.

Spatial patterns in the δOw-salinity relationship remain similar between the LH and LIG simulations, but change significantly for the LGM. αSPACE remains similar in the glacial tropics but shows large and
<table>
<thead>
<tr>
<th>Region</th>
<th>OBS</th>
<th>LH</th>
<th>LGM</th>
<th>LIG</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\alpha_{\text{SPACE}}$</td>
<td>$\delta_F$</td>
<td>$r^2$</td>
<td>$\alpha_{\text{SPACE}}$</td>
</tr>
<tr>
<td>All Ocean</td>
<td>0.39</td>
<td>-13.40</td>
<td>0.80</td>
<td>0.21</td>
</tr>
<tr>
<td>Open Ocean</td>
<td>0.23</td>
<td>-8.04</td>
<td>0.60</td>
<td>0.18</td>
</tr>
<tr>
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<td>-5.11</td>
<td>0.72</td>
<td>0.16</td>
</tr>
<tr>
<td>Mid-lat (30-60N/S)</td>
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<td>-12.34</td>
<td>0.79</td>
<td>0.16</td>
</tr>
<tr>
<td>High-lat (60-90N/S)</td>
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<td>-18.15</td>
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</tr>
<tr>
<td>Pacific</td>
<td>0.41</td>
<td>-14.31</td>
<td>0.92</td>
<td>0.17</td>
</tr>
<tr>
<td>Trop Pacific</td>
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<td>-9.71</td>
<td>0.58</td>
<td>0.18</td>
</tr>
<tr>
<td>S. Atlantic</td>
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<td>-13.04</td>
<td>0.52</td>
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<tr>
<td>N. Atlantic</td>
<td>0.21</td>
<td>-7.41</td>
<td>0.53</td>
<td>0.16</td>
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<tr>
<td>Tropical Atlantic</td>
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<td>-5.11</td>
<td>0.80</td>
<td>0.16</td>
</tr>
<tr>
<td>Indian</td>
<td>0.16</td>
<td>-5.41</td>
<td>0.31</td>
<td>0.18</td>
</tr>
<tr>
<td>Arctic</td>
<td>0.53</td>
<td>-18.21</td>
<td>0.92</td>
<td>0.15</td>
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<td>Southern Ocean</td>
<td>0.40</td>
<td>-13.94</td>
<td>0.70</td>
<td>0.07</td>
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</table>

Table 2: Gradient ($\alpha_{\text{SPACE}}$), intercept ($\delta_F$) and $r^2$ values from least squares linear regressions on spatial sea surface salinity and $\delta_{OW}$ data. Values are presented for observations (OBS) from the Global Seawater Oxygen-18 Database (Schmidt, 1999b; Bigg and Rohling, 2000, http://data.giss.nasa.gov/o18data/) and for the LH, LGM and LIG simulations. Observed values are biased to the spatial sampling coverage. Model values are calculated using all ocean grid points within each region and have been re-gridded to an equal area 100km grid.
opposing changes in mid and high-latitudes. During the LGM, $\alpha_{SPACE}$ decreases by $>60\%$ in the mid-latitudes and more than triples at high latitudes. The high latitude steepening of $\alpha_{SPACE}$ is concentrated in the Arctic in response to strongly depleted glacial precipitation and runoff, resulting in a reduced $\delta_{O_{w}}$ by $\sim 10 \%/oo$. For many regions, the LGM yields the lowest $r^2$ values, suggesting that $\delta_{O_{w}}$ and salinity are most decoupled during glacial climate. There is almost no correlation between $\delta_{O_{w}}$ and salinity for the LGM Southern Ocean, when sea ice extent is largest and the signal-to-noise ratio becomes too low. Changes in $\alpha_{SPACE}$ between the LH and LIG are within $\pm 0.01 \%/oo/psu$ for all regions.

3.2.2. Temporal variability in paleosalinity reconstructions

The following section evaluates the temporal relationship between $\delta_{O_{w}}$ and salinity. Regional values of $\alpha_{DECADAL}$ and $\alpha_{SLICE}$ are presented in Table 3. Similar to Table 2, the gradient, intercept and $r^2$ values are presented from the least squares linear regression between decadal $\delta_{O_{w}}$ and salinity for each simulation and region. Correlations between decadal $\delta_{O_{w}}$ and salinity are much weaker than the spatial relationships. Regional values of $\alpha_{SPACE}$, $\alpha_{DECADAL}$, and $\alpha_{SLICE}$ are compared for each simulation in Figure 3. For most regions, values of $\alpha_{SPACE}$ are steeper than $\alpha_{DECADAL}$, and $\alpha_{SLICE}$ values are steeper than $\alpha_{SPACE}$ and $\alpha_{DECADAL}$. Over large regions (eg. mid latitudes) the gradient between climates ($\alpha_{SLICE}$) is relatively consistent with the LH spatial gradient ($\alpha_{SPACE}^{LH}$), in agreement with results for the Pliocene presented by Tindall and Haywood (submitted).

The spatial patterns of $\alpha_{DECADAL}$ and $\alpha_{SLICE}$, calculated at each model grid point, are shown in Figures 4 and 5 respectively. $\alpha_{DECADAL}$ varies significantly across small spatial scales. The LGM $\alpha_{DECADAL}$ anomalies ($\alpha_{DECADAL}^{LGM-LH}$) are generally negative in the North Atlantic and positive in the Arctic. The North Atlantic anomalies coincide with changes in the location of the Gulf Stream in the west, and changes in the location of the polar front in the north-east. The LIG shows generally negative $\alpha_{DECADAL}$ anomalies ($\alpha_{DECADAL}^{LIG-LH}$) along the equator and positive anomalies in the latitude band of the Antarctic Circumpolar Current (ACC). The spatial pattern of $\alpha_{SLICE}$ differs from $\alpha_{DECADAL}$ for both the LGM and LIG (Figure 5). For most of the ocean, values of $\alpha_{SLICE}$ are steeper than $\alpha_{DECADAL}$. Exceptions to this are in the LIG equatorial Atlantic, where $\alpha_{SLICE}^{LIG-LH}$ is negative close to regions of small/negligible salinity change (masked areas in Figure 5), and in the glacial western Arctic, where $\alpha_{SLICE}^{LGM-LH}$ is also negative, suggesting that the $\delta_{O_{w}}$-salinity signal is too small compared to the noise component in the system.

Figure 6 presents the spatial and temporal $\delta_{O_{w}}$-salinity relationships for a selection of ocean regions. The gradients differ significantly in a number of regions, such as the North Atlantic. During the LH, there
<table>
<thead>
<tr>
<th>Region</th>
<th>LH $\alpha^{\text{DECADAL}}$</th>
<th>LH $\delta_F$</th>
<th>LH $r^2$</th>
<th>LGM $\alpha^{\text{DECADAL}}$</th>
<th>LGM $\delta_F$</th>
<th>LGM $r^2$</th>
<th>LIG $\alpha^{\text{DECADAL}}$</th>
<th>LIG $\delta_F$</th>
<th>LIG $r^2$</th>
<th>$\alpha^{\text{SLICE}}_{\text{LGM-LH}}$</th>
<th>$\alpha^{\text{SLICE}}_{\text{LIG-LH}}$</th>
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</thead>
<tbody>
<tr>
<td>All Ocean</td>
<td>0.10</td>
<td>-3.45</td>
<td>0.54</td>
<td>0.18</td>
<td>-6.24</td>
<td>0.50</td>
<td>0.07</td>
<td>-2.31</td>
<td>0.83</td>
<td>0.41</td>
<td>0.42</td>
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<td>Open Ocean</td>
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<td>-1.28</td>
<td>0.03</td>
<td>0.13</td>
<td>-4.26</td>
<td>0.51</td>
<td>0.08</td>
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<td>0.52</td>
<td>0.20</td>
<td>-0.39</td>
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<tr>
<td>Mid-lat (30-60N/S)</td>
<td>0.04</td>
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<td>0.11</td>
<td>0.10</td>
<td>-3.52</td>
<td>0.33</td>
<td>0.08</td>
<td>-2.62</td>
<td>0.74</td>
<td>0.18</td>
<td>0.14</td>
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<td>-4.42</td>
<td>0.82</td>
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<td>0.83</td>
<td>0.12</td>
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<tr>
<td>N. Atlantic</td>
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<td>0.08</td>
<td>0.08</td>
<td>-2.56</td>
<td>0.56</td>
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<td>-2.03</td>
<td>0.70</td>
<td>0.34</td>
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</tr>
<tr>
<td>Tropical Atlantic</td>
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<td>0.07</td>
<td>-2.16</td>
<td>0.62</td>
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<td>-0.25</td>
</tr>
<tr>
<td>Indian</td>
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<td>-3.68</td>
<td>0.71</td>
<td>0.14</td>
<td>-4.83</td>
<td>0.69</td>
<td>0.10</td>
<td>-3.44</td>
<td>0.92</td>
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<td>0.13</td>
</tr>
<tr>
<td>Arctic</td>
<td>0.04</td>
<td>-2.03</td>
<td>0.11</td>
<td>0.39</td>
<td>-13.96</td>
<td>0.70</td>
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<td>-1.63</td>
<td>0.31</td>
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<tr>
<td>Southern Ocean</td>
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<td>-1.55</td>
<td>0.45</td>
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<td>0.06</td>
<td>-2.15</td>
<td>0.73</td>
<td>0.04</td>
<td>0.16</td>
</tr>
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</table>

Table 3: As Table 2 but for temporal relationships. Gradient ($\alpha^{\text{DECADAL}}$), intercept ($\delta_F$) and $r^2$ values from least squares linear regressions on decadally averaged surface salinity and $\delta_{O_2}$ data from the last 100 years of each simulation. Regional $\alpha^{\text{SLICE}}$ values are also presented in the last two columns. Model values are calculated using all ocean grid points within each region.
is no significant relationship between decadal $\delta_{Ow}$ and salinity in the North Atlantic ($r^2 < 0.1$). Temporal gradients in the Southern Ocean remain $<0.1$ $^\circ$C/psu for all but the LIG-LH gradient. For most regions, the spatial gradient ($\alpha^{SPACE}$) and the gradient between climates ($\alpha^{SLICE}$) are steeper than each climate’s intrinsic gradient ($\alpha^{DECADAL}$). Similar differences between the intrinsic and intra-simulation temporal gradients have been found for simulations covering the mid-Holocene and pre-industrial periods (Schmidt et al., 2007).

The simulated salinity anomalies for the LGM and LIG and the magnitude of error in the estimated salinity using the $\delta_{Ow}$ residual method (applying the LH spatial $\delta_{Ow}$-salinity gradients to simulated $\delta_{Ow}$ anomalies) are shown in Figure 7. The $\delta_{Ow}$ residual method captures the correct large-scale pattern in salinity anomalies in the mid and low-latitudes for both climates (Figure 7a-d). However, regional biases in the estimated salinity can exceed $\pm 4$ psu for both the LGM and LIG (Figure 7e,f). The observed bias in the Mediterranean Sea will in part stem from the use of the open ocean $\delta_{Ow}$-salinity gradient in this region, chosen due to the coarse resolution of the enclosed sea on the GCM grid. The agreement between spatial and temporal gradients may thus be improved if a Mediterranean specific gradient were applied. In the glacial Arctic, the estimated salinity change is of opposing sign to the actual simulated salinity anomaly. The difference between the estimated and actual salinity anomalies in the glacial northeast Atlantic and south of Greenland suggests that the actual salinity change may be larger than that inferred using the LH spatial gradients. Further south the estimated salinity anomalies overestimate the actual changes. For the LIG, estimated salinity anomalies are larger than the actual changes around the coast of Greenland, in the GIN seas, and in the Tropical Atlantic. Estimated salinity anomalies are slightly weaker than the actual change in the northern Indian Ocean. Across both climates, the error in the estimated salinity is generally smallest in the South Atlantic, Indian and Tropical Pacific Oceans.

4. Discussion

4.1. Modelling insights for paleosalinity reconstruction

Our model simulations do not help characterise paleosalinity reconstruction uncertainties due to dia-
genetic errors, age uncertainties, species offsets or errors in the isolation of $\delta_{Ow}$ from $\delta_{Oc}$. However, the large-scale model realisation of the $\delta_{Ow}$-salinity relationship in HadCM3 can provide insight into the con-
siderations necessary to interpret unevenly distributed isotope data for paleosalinity reconstruction.

By comparing spatial and temporal relationships across regions it is possible to identify locations where paleosalinity reconstructions have low uncertainties and those with large uncertainties. Problem regions are
the North Atlantic, Tropical Atlantic and high latitude regions, where a small signal-to-noise ratio produces low $r^2$ values between $\delta_{Ow}$ and salinity for one or more of the simulations. High latitude regions are clearly problematic for glacial-interglacial paleosalinity reconstructions, where $\alpha^{SLICE}$ is negative and the largest differences between gradients are observed (Table 2 and Figure 3). During the LIG, the smallest differences between $\alpha^{SLICE}$ and $\alpha^{DECADAL}$ are found in the Indian Ocean and the Tropical Pacific, where $\alpha^{DECADAL}$ is within 30% of $\alpha^{SLICE}$, suggesting good agreement in the $\delta_{Ow}$-salinity relationship across temporal scales. For the LGM, the smallest differences are observed in the Tropical Pacific and South Atlantic, where $\alpha^{DECADAL}$ is within 10% of $\alpha^{SLICE}$. For both the LGM and LIG, $\alpha^{DECADAL}$ is only within 50% of $\alpha^{SLICE}$ in the Tropical Pacific and within 55% in the South Atlantic, Indian and Pacific Oceans.

4.2. Physical controls on the $\delta_{Ow}$-salinity relationship

These simulations can provide insight of the fundamental controls on $\delta_{Ow}$ and salinity. Below we address why spatial and temporal $\delta_{Ow}$-salinity gradients might not agree and discuss the sources of uncertainty in paleosalinity reconstruction, including how these may vary between glacial and interglacial climates.

4.2.1. Hydrological cycle

The coupling between $\delta_{Ow}$ and salinity generally observed in the global ocean suggests that the processes affecting both $\delta_{Ow}$ and salinity, such as regional E-P balance, dominate over processes which preferentially influence one variable over the other, such as a change in precipitation moisture source (Russon et al., 2013). However, these simulations show that changes in the distribution of insolation can produce feedbacks in the climate system that affect $\delta_{Ow}$ independently of salinity and thus complicate the interpretation of $\delta_{Ow}$.

During the LIG, when no ice sheet changes have been applied, changes in the $\delta_{Ow}$-salinity relationship are primarily driven by changes in the distribution of insolation. In this case, atmospheric water vapour pathways and conditions along an airmass trajectory are the fundamental cause of variability in $\delta_{Ow}$-salinity relationships in the main ocean basins (LeGrande and Schmidt, 2011). Pathways of water exchange determine a region’s freshwater end-member and any process that alters $\delta_F$ will lead to a changes in the $\delta_{Ow}$-salinity relationship. Studies in the mid-latitudes and tropics have interpreted values of $\delta_F$ in terms of river discharge (Munksgaard et al., 2012), the isotopic composition of regional precipitation ($\delta_{Op}$) (Benway and Mix, 2004; LeGrande and Schmidt, 2006; Abe et al., 2009), local evaporation regime (Conroy et al., 2014), and a mixture of evaporation, precipitation and runoff (Delaygue et al., 2001). Benway and Mix
(2004) conclude that possible changes in the isotopic composition of freshwater budget terms is the largest source of error in paleosalinity reconstructions in the Panama Bight, estimating that a change in $\delta_{Op}$ of 3.5 $^\circ/o_0$ would cause a 2 psu error in inferred salinity. This magnitude of change in $\delta_{Op}$ is well within the regional anomalies between our simulations.

The higher obliquity during the LIG and associated warmer northern hemisphere summer temperatures produces a reorganisation of the Intertropical Convergence Zone (ITCZ) and enriches $\delta_{Op}$ at high latitudes (thus enriching $\delta_F$). These changes cause significant uncertainties in salinity reconstruction in the tropics and in the Arctic. Past salinity values determined from $\delta_{Ow}$ residuals alone may therefore require correcting for orbitally driven changes in atmospheric circulation in order to accurately isolate changes in E-P and thus the salinity signal, even during periods characterised by similar boundary conditions to today (LeGrande and Schmidt, 2009).

4.2.2. Ice-sheets and freezing processes

During glacial periods, changes in boundary conditions are larger and include the growth of ice sheets. Differences in $\delta_{Ow}$-salinity relationships are thus larger as additional feedbacks, such as meltwater processes, add to the orbitally driven biases. This is the case for our LGM simulation, when the large northern hemisphere ice sheets cause large changes in the temporal $\delta_{Ow}$-salinity gradient around its peripheries. The water stored in these ice sheets is highly depleted in $\delta_{Ow}$. When this water reaches the surface ocean it depletes $\delta_F$ and significantly steepens the $\delta_{Ow}$-salinity gradient (LeGrande and Schmidt, 2006; Schmidt et al., 2007).

The highly depleted freshwater from high-latitude ice sheets has been linked to instability in the oceanic thermohaline circulation and large changes in climate (Tindall and Valdes, 2011; LeGrande and Schmidt, 2008; Stouffer et al., 2007; Weaver et al., 2003). Miller et al. (2012) suggest that reduced basal melting around the fringes of the Antarctic ice sheet during the LGM may have played an important role in increasing the salinity of southern sourced waters. Changes in the freezing/melting regime around high latitude ice sheets can therefore significantly modify the $\delta_{Ow}$-salinity relationship in the surrounding surface ocean and have globally reaching effects on deep ocean properties, through variable inputs of depleted freshwater and variable subsurface salt fluxes.

Decoupling of the $\delta_{Ow}$-salinity relationship can also occur in the high latitude oceans due to changes in sea ice regime. Freezing processes result in salinity increases that are accompanied by essentially no observable change in seawater isotopic composition (Craig and Gordon, 1965; Lehmann and Siegenthaler,
and therefore HadCM3 treats sea ice formation as non-fractionating. Consequently, melting and freezing have opposed (shallowing and steepening) effects on the $\delta_{O_{18}}$-salinity gradient (Strain and Tan, 1993). These largely seasonal changes are not necessary reversible (Rohling and Bigg, 1998). Higher surface salinities from sea ice formation can initiate convection and mix surface waters with the ocean interior (e.g. Frew et al., 1995, 2000) or sea ice can be exported and subsequently melted in a new location. The $\delta_{O_{18}}$-salinity relationship can thus become nonlinear (Rohling and Bigg, 1998; Strain and Tan, 1993). The effects of changing sea ice regime on the $\delta_{O_{18}}$-salinity relationship can be seen around the coast of Antarctica and, more clearly, Greenland for both the LGM and LIG climate (Figure 7).

4.2.3. Ocean reorganisation

For periods with significant changes in boundary conditions (e.g. large ice sheets associated with glacial periods) ocean reorganisation can introduce large advective changes. Changes in the location of water mass boundaries or the position and magnitude of upwelling/downwelling fluxes will cause local salinity changes that may not reflect a change in the hydrological cycle. Additionally, because $\delta_{O_{18}}$ and salinity in subsurface waters behave conservatively (Paren and Potter, 1984; Frew et al., 1995), a change in oceanic source characteristics will not only affect the $\delta_{O_{18}}$-salinity relationship of local seawater, but also in waters remote from the initial change (Rohling and Bigg, 1998). Thus Rohling and Bigg (1998) argue that the $\delta_{O_{18}}$-salinity relationship in many regions is determined by advection rather than the local water balance.

Our simulations show the largest reorganisation of surface ocean currents during the LGM, when changes in orbit and ice volume increase the meridional temperature gradient. The North Atlantic in particular is a key region of interest for salinity and wider paleoceanographic reconstruction over the last glacial cycle due to its dynamic role in the global thermohaline circulation (CLIMAP Project Members, 1976; Pflaumann et al., 2003; Sarnthein et al., 2003; Broecker, 1989; MARGO Project Members, 2009). However, advective changes in the North Atlantic cause large uncertainties in the $\delta_{O_{18}}$-salinity relationship. Consequently, during periods of significant climate change such as glacial-interglacial transitions, these results suggest that large salinity biases preclude traditional paleosalinity in locations of sharp gradients, unless it is concerned with reconstructing the past migration of oceanic fronts themselves or assessing large-scale patterns of change (Schmidt, 1999a; Caley and Roche, 2013).
5. Conclusion

We present isotope-enabled simulations using HadCM3 covering the Late Holocene, the Last Glacial Maximum and the Last Interglacial. A model-data comparison suggests that the model captures the general spatial pattern of planktonic $\delta_{Oc}$ during the Late Holocene and the Last Glacial Maximum, and we calculate a model ‘best-fit’ glacial enrichment of $1.08 \%_{oo}$. The simulations are used to investigate how the relationship between surface ocean $\delta_{Ow}$ and salinity varies in response to past climate change. Modelled changes in $\delta_{Ow}$ are closely coupled to changes in the hydrological cycle and thus correlate with changes in salinity. However, our simulations show that the interpretation of $\delta_{Ow}$ as purely diagnosing changes in surface hydrology can be over-simplistic, especially on glacial-interglacial timescales.

Our results suggest that the relationship between $\delta_{Ow}$ and salinity can vary significantly over small spatial scales. This has implications when generalising a single value of $\alpha$ (the $\delta_{Ow}$-salinity gradient) across large ocean regions, as is typically done for the $\delta_{Ow}$ residual method. Our results also suggest that the $\delta_{Ow}$-salinity relationship has varied significantly through the past, i.e. $\delta_{Ow}$-salinity spatial relationships do not necessarily equal $\delta_{Ow}$-salinity temporal relationships. We show that spatial gradients are generally shallower but within $\sim$50% of the actual simulated LH to LGM and LH to LIG temporal gradients. Temporal gradients calculated from each simulations multi-decadal variability are generally shallower than both spatial and actual simulated gradients.

Changes in sea ice regime, ocean circulation, and the isotopic terms in a regions freshwater budget clearly influence $\delta_{Ow}$ independent of salinity and can lead to uncertainties in salinity estimates exceeding $\pm4$ psu in regions that are sensitive to these processes. These results show that the relative importance of each control varies between glacial and interglacial climates. During the LIG, the different orbital configurations lead to changes in atmospheric moisture pathways and thus changes in regional $\delta_{Ow}$-salinity relationships. During the LGM, larger changes in boundary conditions lead to significant sea ice and oceanic reorganisation, which add to salinity biases driven by orbital forcing alone.

Our results identify regions where spatial and temporal $\delta_{Ow}$-salinity gradients overlap, providing confidence in paleosalinity reconstruction in these locations. The most robust paleosalinity reconstructions are achieved in the South Atlantic, Tropical Pacific and Indian Oceans where glacial-interglacial variability in the $\delta_{Ow}$-salinity relationship is smallest.

Our results question whether reliable paleosalinity estimates can be derived in the North Atlantic or in high latitude regions due to glacial-interglacial variability in the $\delta_{Ow}$-salinity gradient. For regions with
large uncertainties, additional constraints on the past freshwater budget or circulation, as well as multi-proxy approaches are recommended to achieve accurate records of past salinity (e.g. Rohling, 2007; LeGrande and Schmidt, 2011).

Isotope enabled coupled climate models can help disentangle the multiple signals recorded in paleoclimate archives, such that due to the glacial effect, changes in Southern Ocean sea ice, North Atlantic ocean currents and surface E-P balance. These results show that the $\delta_{Ow}$ residual method helps in tracking major oceanic fronts and depicting large-scale patterns of change. With additional constraints, $\delta_{Ow}$ can also provide elusive information on past sea ice regimes, ocean circulation, and abrupt meltwater inputs, in addition to its established role of informing on variability in the past hydrological cycle.

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References


URL http://www.sciencemag.org/content/298/5599/1724.short


URL http://www.geosci-model-dev.net/6/1505/2013/


URL http://linkinghub.elsevier.com/retrieve/pii/S02777319114003382


URL http://linkinghub.elsevier.com/retrieve/pii/S0012821X0000073X


URL http://www.sciencedirect.com/science/article/pii/030442039500003A


URL http://dx.doi.org/10.1175/2008JCLI2415.1


URL http://dx.doi.org/10.1007/s00382-002-0272-6


URL: http://www.ncbi.nlm.nih.gov/pubmed/20016591


URL: http://linkinghub.elsevier.com/retrieve/pii/S0033589401923166


URL: http://linkinghub.elsevier.com/retrieve/pii/S0012821X12006887


URL: http://doi.wiley.com/10.1029/2008PA001610

URL http://doi.wiley.com/10.1029/2010PA002043


URL http://dx.doi.org/10.1038/45204

URL http://www.clim-past.net/7/1041/2011/

URL http://journals.ametsoc.org/doi/abs/10.1175/2007JCLI2139.1

URL http://doi.wiley.com/10.1029/2008GC002035

URL http://doi.wiley.com/10.1029/2012PA002297

URL http://linkinghub.elsevier.com/retrieve/pii/S0967063798000703


URL http://www.sciencemag.org/content/191/4232/1131.abstract

URL http://dx.doi.org/10.1038/ngeo411

URL http://scitation.aip.org/content/aip/journal/jcp/51/12/10.1063/1.1671982

URL http://link.springer.com/10.1007/s00382-003-0324-6

URL http://dx.doi.org/10.1029/JC089iC01p00749

URL http://dx.doi.org/10.1146/annurev.earth.32.082503.144359


URL http://dx.doi.org/10.1029/2002PA000774


URL http://linkinghub.elsevier.com/retrieve/pii/S0025327999000973


Quaternary Research 21 (2), 123–224.

URL http://www.clim-past.net/9/1543/2013/

URL http://dx.doi.org/10.1029/2002PA000769


URL http://linkinghub.elsevier.com/retrieve/pii/S027737910100110X


URL http://dx.doi.org/10.1038/215015a0


URL http://linkinghub.elsevier.com/retrieve/pii/S0033589401923129

URL http://dx.doi.org/10.1029/2006GL026923


URL http://linkinghub.elsevier.com/retrieve/pii/S0277379109003564


URL http://ipcc-wg1.ucar.edu/ wg1/wg1-report.html


URL http://www.sciencemag.org/content/310/5752/1317.abstract


URL http://dx.doi.org/10.1029/93JC01182


URL http://linkinghub.elsevier.com/retrieve/pii/S0012821X10000130


URL http://linkinghub.elsevier.com/retrieve/pii/S0921818111000312


Table 1: List of isotope-enabled HadCM3 simulations and prescribed boundary conditions. We adopt the same boundary forcing as applied by Singarayer and Valdes (2010): orbital parameters are taken from Berger and Loutre (1991); atmospheric CO$_2$ is derived from the Vostok ice core (Petit et al., 1999; Loulergue et al., 2008); and CH$_4$ and N$_2$O from the EPICA Dome-C ice core (Spahni et al., 2005).

<table>
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<th>Exp</th>
<th>Orbit</th>
<th>CO$_2$</th>
<th>CH$_4$</th>
<th>N$_2$O</th>
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<td>ppmv</td>
<td>ppmv</td>
<td>ppmv</td>
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<td>0.37</td>
<td>0.25</td>
<td>21</td>
</tr>
<tr>
<td>LIG</td>
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<td>275</td>
<td>0.64</td>
<td>0.26</td>
<td>0</td>
</tr>
</tbody>
</table>
Figure 1. Modelled surface ocean δ$_{Oc}$, calculated from the equation of Shackleton (1974). Superimposed coloured dots represent individual planktonic foraminifera calcite δ$_{Oc}$ data. Model and data for the LH (top left), LGM (middle left), and LIG (bottom left). The LGM-LH δ$_{Oc}$ anomaly, with a 1.0 ‰ glacial enrichment subtracted from the data (middle right), and LIG-LH δ$_{Oc}$ anomaly (bottom right). Data for the Late Holocene is from the Waelbroeck et al. (2005) dataset, defined as 0-4 ka, and LGM anomalies are from the compilation of Caley et al. (2014), with the LGM defined as 19-23 ka and LH as 0-3 ka.

Figure 2. Regional relationships between spatial sea surface salinity and δ$_{Ow}$ for a selection of ocean regions. Top left panel shows all observations from the GISS Global Seawater Oxygen-18 Database (Schmidt, 1999b; Bigg and Rohling, 2000, http://data.giss.nasa.gov/o18data/), coloured by degrees latitude. Subsequent panels show individual observations in black. All model grid points within each region are shown in orange, after being re-gridded to an equal area 100km grid. The modelled values taken from the closest ocean grid point to each observed value are shown in red. The least squares linear regression for observed data (Obs), all model grid points within each region on an equal area grid (All Mod) and the model grid points where observations are available (Mod) are also shown.

Figure 3. Comparison of spatial and temporal δ$_{Ow}$-salinity gradients; $\alpha^{SPACE}$ (the relative co-variability of δ$_{Ow}$ and salinity over a region), $\alpha^{DECADAL}$ (the decadal co-variability of δ$_{Ow}$ and salinity at a given point in space), and $\alpha^{SLICE}$ (the actual relationship between δ$_{Ow}$ and salinity between the Last Glacial Maximum and Late Holocene [LGM-LH] or Last Interglacial and Late Holocene [LIG-LH] at a given point in space). Top panels show the LGM gradients as filled triangles (far left panel also shows LH gradients as filled circles). Bottom panels show the LIG gradients as filled squares. Left panels: difference between $\alpha^{SPACE}$ and $\alpha^{DECADAL}$ for each ocean region, representing the difference between the δ$_{Ow}$ residual method, based on modern spatial gradients, and decadal δ$_{Ow}$-salinity co-variability. Middle panels: as left but between $\alpha^{SPACE}$ and $\alpha^{SLICE}$, representing the comparison between the δ$_{Ow}$ residual method and the actual modelled δ$_{Ow}$-salinity gradient. Right panels: as left and middle but between $\alpha^{DECADAL}$ and $\alpha^{SLICE}$. Regional values of $\alpha^{SLICE}$ for the LGM-LH and LIG-LH which lie outside the axis limits on the middle and right panel are
quoted below the figure. Filled colours denote each region that the gradient has been averaged over and are shown in the legend on the far right. The one-to-one line, representing perfect agreement between gradients, is also plotted (black dashed line).

Figure 4. Multi-decadal co-variability of salinity and $\delta_{Ow}$ at each model grid point. Top: Gradient of the local linear regression on multi-decadal variability between sea surface salinity and sea surface $\delta_{Ow}$ over the last 100 years of the LH simulation ($\alpha_{LH}^{DECADAL}$). Middle: Difference in $\alpha^{DECADAL}$ between the LGM and LH simulations ($\alpha_{LGM-LH}^{DECADAL}$). Bottom: Difference in $\alpha^{DECADAL}$ between the LIG and LH simulations ($\alpha_{LIG-LH}^{DECADAL}$).

Figure 5. Modelled temporal $\delta_{Ow}$-salinity gradient ($\alpha^{SLICE}$) between the LGM and LH (top; $\alpha_{LGM-LH}^{SLICE}$) and LIG and LH (bottom; $\alpha_{LIG-LH}^{SLICE}$). Regions are masked where the change in salinity is small using a threshold of 0.1$\sigma$ for the LGM-LH (0.24 psu) and 0.14$\sigma$ for the LIG-LH (0.11 psu). A filled black circle, triangle, and square represent the locations plotted in the left, middle and right panels of Figure S3 respectively (see Supplementary Information).

Figure 6. Variability between $\delta_{Ow}$-salinity gradients across selected ocean regions. Filled circles represent decadally averaged $\delta_{Ow}$ and salinity values for the LH (black), LGM (blue) and LIG (red). Filled squares represent average $\delta_{Ow}$ and salinity values calculated over the final 100 years of the LH (green), LGM (mauve) and LIG (orange) simulations. Lines show the linear relationships between multi-decadal data (solid lines), centennially averaged data (dashed lines), and spatially averaged data (light grey, light blue and light red for LH, LGM, and LIG respectively, dot-dashed lines). The values of $\alpha^{SPACE}$, $\alpha^{DECADAL}$, and $\alpha^{SLICE}$ are also shown on the figure with the associated $r^2$ values for $\alpha^{DECADAL}$ and $\alpha^{SPACE}$.

Figure 7. The $\delta_{Ow}$ residual method. Top panels: Salinity anomalies between a) the LGM-LH and b) the LIG-LH. Middle panels: Inferred salinity anomalies using the $\delta_{Ow}$ residual method for c) the LGM and d) the LIG (calculated by applying the LH spatial slopes to the LGM-LH and LIG-LH $\delta_{Ow}$ anomalies respectively). Bottom panels show the difference between the modelled salinity anomalies (top panels) and inferred salinity anomalies using the $\delta_{Ow}$ residual method (middle panels) for e) the LGM-LH and f) the LIG-LH. For subplots e-f, spatial slopes are calculated regionally over the North Atlantic, South Atlantic, Tropical Atlantic, extratropical Pacific, Tropical Pacific, Indian, Southern and Arctic Ocean (see...
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