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Bénard-Marangoni dendrites upon evaporation of a reactive ZnO nanofluid droplet: Effect of substrate chemistry

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ABSTRACT

Evaporation of a particle laden sessile drop can lead to complex surface patterns with structural hierarchy. Most commonly the dispersed particles are inert. We have recently reported that, when the sessile drop contains reactive ZnO nanoparticles, solidified Bénard-Marangoni (BM) cells with dendritic micromorphology were formed in the residual surface pattern from in situ generated nanoclusters. Here we report the effect of substrate chemistry on the residual pattern from evaporation of nanofluids containing ZnO particles dispersed in a mixture of cyclohexane...
and isobutylamine, by comparing three different substrates: glass, silicon and hydrophilized silicon. In particular, we performed a quantitative analysis of the BM cell size distribution and the cell morphological characteristics via the fractal dimension analysis. We find that the size dimension $\lambda_{BM}$ of the dendritic Bénard-Marangoni cells varied on the different substrates, attributed to their different hydrophilicity and affinity for water molecules, evident from the different polar components $\gamma^p$ in their surface free energy from the Owens-Wendt analysis. The average BM cell size was the smallest for the glass substrate ($\lambda_{BM} = 289 \mu m$), and comparable for the unmodified and UVO treated silicon wafers (with $\lambda_{BM} = 466 \mu m$ and $423 \mu m$, respectively). The fractal dimension analysis provided a quantitative description of the BM cells with complex structural hierarchy, highlighting the differences in the geometric features of the surface patterns resulting from different substrate chemistry. We also found that the fractal dimensions depended on the BM cell size, attributing it to two different regimes: the growing fractals and the maturing fractals.

KEYWORDS
Evaporation Induced Self-Assembly, nanoparticles, zinc oxide, dissolution, Bénard-Marangoni instabilities, coffee ring effect, fractal dimension analysis

INTRODUCTION

The Bénard convection, also known as the Bénard-Marangoni convection, was first observed by Henri Claude Bénard in 1900 as ordered hexagonal cells formed in a melted paraffin with graphite dusts (1-2). Intrigued by the observation, he performed comprehensive studies of such cellular vortices in a horizontal layer of different volatile liquids such as ethanol, diethyl ether, and benzene at room temperature, as well as non-volatile wax or spermaceti (whale oil), on a metallic plate heated to 50 – 100 °C (3-4). In 1916, Lord Rayleigh published first theoretical explanation of Bénard's results based on the stability analysis, which implicated buoyancy as
the driving force for the convective motion (5). However, it has been later shown, both experimentally (6) and theoretically (7), that the convective cells in Bénard’s system were induced by variations in the surface tension caused by temperature fluctuations at the free fluid surface. Many studies on Bénard convections have since been reported (8).

Due to localized fluctuations in the droplet surface temperature, multiple Bénard cells can be induced, and dispersed solutes may form corrugated residual patterns of connected polygons templating the convective cells (9). This has been explored in the evaporation induced self-assembly (EISA) process (10-11) to produce various surface patterns. Some examples include porous films with a knotted-rope structure from zeolite silicalite nanoparticle suspensions dried on silicon (12), and honeycomb patterns from various suspensions, such as silver, cobalt, copper and barium ferrite nanocrystals dispersed in hexane or decane (13-14), polystyrene microspheres in aqueous solutions with added pentadecanoic acid (15-16), toluene solutions of poly(styrene-ran-butadiene) copolymer (17) or calcium carbonate particles (18), and polymethyl(methacrylate) dissolved in chloroform (19). In addition, the Bénard-Marangoni convection has also been employed to produce other types of structures, such as sol-gel derived titania (TiO₂) films using surface tension changing co-solvents (20), hexagonal and stripe-like patterns by varying substrate wettability (21), nanoporous TiO₂ films (22), and single-walled carbon nanotubes (23).

In these previous studies (1-2, 5-8, 10-19, 21), the dispersed particles were inert, and the residual pattern formation was governed by inter-particle forces and evaporation-induced solvent flows, which in turn could be influenced by particle size, concentration, solvent composition, or evaporation rate. We have recently shown (24-25) that rapid evaporation of a reactive ZnO nanofluid sessile drop can lead to the formation of hierarchical residual, and the mechanism was elucidated and described in some detail in Ref. (24) to account for the structural hierarchy on nano-/micro-/maco-scopic levels, combining video microscopy
observations of the capillary waves at the droplet surface and time-resolved transmission
electron microscopy (TEM) and cryo-TEM observations of the constituent nanostructures
inside the droplet at different stages of the evaporation process. Briefly, as a mixed solvent
(chloroform/methanol/isobutylamine or cyclohexane/isobutylamine) droplet containing ZnO
nanoparticles evaporates on a solid substrate, ZnO particles undergo rapid dissolution. The in
situ generated molecular and particulate species collude with and modify the solvent flows in
the evaporating droplet, which further self-assemble and self-organize into clusters. As the drop
thins upon evaporation, Bénard-Marangoni (BM) instabilities are triggered, and the in situ self-
assembled clusters track the BM convections. Such BM convections manifest as multiple
vortices with liquid flowing upward in the center and subsequently outward to the edge of the
convection cells. Further removal of solvent upon evaporation leads to solidification and
crystallization of the polycrystalline cellular pattern in the drop center with dendritic
micromorphology.

The initial moisture-assisted dissolution of isobutylamine-coated ZnO nanoparticles was
recognized as a key step in this process. We have shown that different crystallinity of the ZnO
nanoparticles led to different dissolution rates, which in turn resulted in different surface
patterns (26). These results may open up new routes for facile fabrication of functional surface
patterns with hierarchical structures via self-assembly induced by evaporation of reactive
nanofluids.

The solvent flow in an evaporating droplet is affected by several other factors, which will
consequently affect the BM convection and the residual pattern. In this work, we have
investigated how the substrate surface chemistry would affect the morphology of the surface
patterns produced. Three different substrates, i.e. a glass coverslip, a silicon wafer, and a UVO
treated silicon wafer, were compared. Their surface chemistry was assessed with the static
contact angle (CA) measurement and their roughness by atomic force microscopy (AFM). In
addition, three types of ZnO particles with different sizes and crystallinities (26) were dispersed in a mixture of cyclohexane and isobutylamine, which were used to form the evaporating sessile drops. The resulted hierarchical surface patterns were analyzed by scanning electron microscopy (SEM). We found that the dimensions of the solidified Bénard cells depended on the substrate used due to different BM flows on these substrates. To go beyond a descriptive account of the surface pattern, the quasi-2D BM convection cells were analyzed using the box counting fractal dimension (FD) analysis (27) that provided a quantitative description of the BM cells with complex structural hierarchy, highlighting the differences in the geometric features of the surface patterns resulting from different substrate chemistry. We show that the surface chemistry of the substrate influences the dimension of the solidified BM cells during the ZnO nano/microfluid evaporation, and we discuss this effect in terms of the substrate-water interactions, as water is crucial to the ZnO nanocrystal dissolution in the pattern formation mechanism from such reactive nanofluids.

MATERIALS AND METHODS

ZnO nano/microparticles

Three different types of zinc oxide (ZnO) particles were used: in-house synthesized ZnO nanoparticles, and commercially acquired ZnO nanopowder (Sigma-Aldrich, <100 nm particle size, ~80% Zn basis), and ZnO powder (Sigma-Aldrich, ACS reagent, ≥99.0% (KT)). The in-house ZnO nanoparticles were synthesized using a modified procedure from Sun et al. (28). Transmission electron micrographs of the ZnO particles can be found in Supplementary Information, SI.01, also shown as insets in Figure 5. Detailed characterization of ZnO particles including transmission electron microscopy, particle size distribution, X-ray diffraction, and energy-dispersive X-ray spectroscopy as well as synthesis of the in-house ZnO nanoparticles is reported elsewhere (26).
ZnO nano/microfluid preparation

ZnO nano/microfluids were prepared by dispersing ZnO particles in a mixture of cyclohexane (Fisher Chemicals, assay 99%) and isobutylamine (Sigma-Aldrich, assay 99%), in a 5:1 volume ratio to 1 mg/mL concentration. As prepared suspensions were sonicated for 2 h to form homogeneous dispersions prior to evaporation experiments. Dynamic light scattering data of ZnO nano/microfluid has been reported in (26), which indicated formation of clusters (1 - 2 μm in size) in all ZnO nano/microfluids, as the suspensions were not inherently stable.

Substrates

Evaporation of the ZnO nano/microfluids sessile drops were performed on three different substrates cut into 1×1 cm² squares, including standard microscope glass slides (type 7101, 0.8 - 1.0 mm thick), and silicon wafers (UniversityWafer Inc., ID 452, 100 mm diameter, P type, B dopant, <100>, 0-100 Ω·cm, 500 μm thick, single-sided polish, test grade), either unmodified or treated by UV/ozone (UVO) exposure for 10 min. The substrates were cleaned by sonication in acetone and ethanol sequentially for 10 min each, rinsed three times with Milli-Q water (18.2 MΩ·cm at 25 °C), then sonicated in Milli-Q water for 10 min and dried using a stream of nitrogen prior to the experiment. For the UVO treatment, a 42-220 UVO-Cleaner (Jetlight Company, Inc.) was used to modify the surface chemistry of the Si substrates, making them more hydrophilic by increasing the amount of -OH groups on the surface (29-30) (see SI.02). Both the contact angle measurements and evaporation experiments were performed within 1-2 h of the UVO treatment.

The wettability of the substrates was characterized using sessile droplet static contact angle measurements of probing liquids such as Milli-Q water (18.2 MΩ·cm at 25 °C), diiodomethane (Alfa Aesar, 99%), ethylene glycol (Fluka Analytical, ≥ 99.5%), n-hexadecane (Acros Organics, 99%, pure), n-dodecane (Acros Organics, 99%, pure), cyclohexane (Fisher Chemicals, assay 99%), and a mixture of cyclohexane and isobutylamine (Sigma-Aldrich,
assay 99%) in a 5:1 volume ratio, in addition to ZnO nano/microfluids prepared from the in-house synthesized ZnO nanoparticles and commercially acquired ZnO nanopowder and ZnO powder (see SI.01) dispersed in the mixture of cyclohexane and isobutylamine 5:1 volume ratio to 1 mg/mL concentration (see the main text). The measurements were performed at room temperature of 24.5 ± 0.5 °C and relative humidity of ~45% (monitored with a humidity/temperature pen (Tracable)) using a Drop Shape Analyzer – DSA100 (KRÜSS) operated with the KRÜSS ADVANCE 1.9.0.8 software. In a typical measurement, a 5 µL droplet of the measurement liquid (30 µL for cyclohexane/isobutylamine mixture) was pipetted onto a 1×1 cm² substrate, and the image of the drop was recorded for 60 seconds in one second intervals. The value of the contact angle was obtained by tangent fitting method to the drop shape using the software. The errors in mean CA values are quoted as the standard deviations from: 20, 37, and 26 separate measurements for the in-house ZnO nanofluid on glass, unmodified Si, and UVO exposed Si, respectively; 12, 62, and 35 for ZnO nanopowder nano/microfluid on glass, unmodified Si, and UVO exposed Si, respectively; and 8, 25, and 6 for ZnO powder nano/microfluid on glass, unmodified Si, and UVO exposed Si, respectively. Surface free energies were calculated according to the Owens-Wendt method (31), based on the sessile droplet CA measurements of Milli-Q water and diiodomethane (see SI.03). Substrate topography was characterized with the atomic force microscopy (AFM) using MultiMode Nanoscope III (Bruker) operated in the tapping mode (see SI.04)

Evaporation of reactive ZnO nanofluid droplets

An air displacement pipet was used to drop-cast 30 µL of ZnO nano/microfluids onto the surface of the substrates, which were placed inside compartments of an uncovered polystyrene Petri dish (Sterilin, 25 compartment sterile 100 mm box). The evaporation took place at room temperature and RH ~45%. The substrates were covered with white deposits within several
minutes of evaporation. In the case of UVO-Si, the evaporation experiments were performed within 1-2 h after the UVO treatment.

**Residual surface pattern characterization**

Residual surface patterns formed from ZnO nano/microfluids were analyzed with scanning electron microscopy (SEM) using a JSM-IT300 SEM, JEOL. Microfocus grazing incidence X-ray diffraction (XRD) characterization has confirmed (26) that the residual surface patterns produced from the in-house ZnO nanofluid were composed almost entirely from layered complexes of zinc hydroxide with anionic interlayer species (interplanar spacing of 1.37 nm and 0.68 nm, indexed as (001) and (002) planes), and brucite-type zinc hydroxide (interplanar spacing of 0.27 nm and 0.52 nm, indexed as (100) and (110) planes) structures. There were also partial contributions (∼5% of diffraction signal) of a ZnO phase. For the residual patterns produced from the commercially sources ZnO particles, the diffraction profiles were dominated by ZnO patterns from undissolved ZnO nano/microcrystals forming aggregates that were deposited across the fibrous network of the residual patterns.

**Bénard-Marangoni (BM) cells size distribution analysis**

Size distribution analysis of the BM cells was performed using ImageJ (version 1.51j8) software. First, the individual BM cells were outlined on their SEM images using the Serif DrawPlus X6 software, then manually separated to eliminate overlaps for analysis. The size distribution of the BM cells was fitted with the lognormal distribution function (see SI.06).

**Fractal dimension analysis**

The complex structural hierarchy of BM cells was analyzed using the box counting fractal dimension (FD) analysis, as described in detail in (27). Briefly, in the box counting algorithm, a grid of equal boxes of a side-length $\varepsilon$ is laid over an image, and then the number of non-empty boxes, $N(\varepsilon)$, is counted. This number varies with the box size, $N(\varepsilon) \sim \varepsilon^{-D}$, and the
procedure is performed for a range of $\varepsilon$ values. The box counting fractal dimension, $D$, is obtained from the slope of the $\ln(N)$ vs. $\ln(\varepsilon)$ plot (32-33). Specifically for the analysis of the BM cells, the SEM images of the pattern were converted to the binary format in ImageJ, and then circular selections containing BM cells were analyzed using FracLac (version 2015Sep090313a9330) plugin (34). The analysis process is schematically displayed in Figure S12. For completeness, we also include in SI.07 a description of the analysis, which is also described in the SI section of Ref. (27).

RESULTS AND DISCUSSION

Substrate characterization: Surface energy and roughness

The surface energy of the three different substrates, microscope glass slide, silicon wafer and UVO hydrophilized silicon (UVO-Si) wafer, was assessed with the static contact angle (CA) measurement using different solvents (see SI.03 for details). The results are presented in Table 1. The mean CA values measured with a 5 μL droplet of three ZnO nano/microfluids were similar across the substrates, $ca. \theta = 5.5 - 6.5^\circ$, with the in-house ZnO nanofluid showing a slightly higher CA on glass ($\theta = 8.6 \pm 2.0^\circ$) and ZnO powder nano/microfluid a slightly lower CA on UVO-Si ($\theta = 4.1 \pm 1.9^\circ$).

The mean water CA was $\theta = 21.7 \pm 3.5^\circ$ on the microscope glass slide, $\theta = 56.5 \pm 1.2^\circ$ on the silicon wafer, and $\theta = 9.8 \pm 1.6^\circ$ on UVO-Si. These broadly agree with the literature values, $i.e. \theta \sim 31^\circ$ for glass, $\theta \sim 58^\circ$ for silicon with native SiO$_2$ (35), and $\theta \sim 10^\circ$ for UVO exposed silicon, respectively (36). Thus, all the substrates exhibited a certain degree of hydrophilicity, with the UVO-Si most hydrophilic, and untreated Si least.

For the evaporation experiment, the 30 μL droplets would become pinned at the edge with an apparent pinned CA of $\theta \sim 26 - 27^\circ$ on all the substrates. This is comparable to the pinned CA of the control droplets of cyclohexane/isobutylamine mixtures on the substrates ($\theta \sim 26 -$
27°) also shown in Table 1. The pinned CA values are higher than those for the static CA. As the evaporation took place, the pinned droplet would thin, and the apparent CA at the pinned periphery would decrease to the values of respective nano/microfluids, before the contact line receded upon further evaporation.

The calculated surface free energies (SFE) of the substrates based on the Owens-Wendt method (31) using droplets of Milli-Q water and diiodomethane (see SI.03 for details) were \( \gamma = 74.4 \pm 1.5, 50.3 \pm 1.6, \) and \( 75.5 \pm 0.5 \) \( \text{mN/m} \) for the microscope glass slide, Si, and UVO-Si, respectively. The UVO-Si had the largest polar SFE contribution (\( \gamma^p = 36.4 \pm 0.3 \) \( \text{mN/m} \)), consistent with its smallest water CA. The unmodified Si had the lowest values of disperse and polar components in the surface energy, \( \gamma^D = 33.1 \pm 0.8 \) and \( \gamma^P = 17.2 \pm 0.8 \) \( \text{mN/m} \), respectively.

We note that slightly different surface energy values of diiodomethane exist in the literature, e.g. \( \gamma^D = 48.5 \) (or 49.5) \( \text{mN/m} \) and \( \gamma^P = 2.3 \) (or 1.3) \( \text{mN/m} \) in Ref. (37). The values of \( \gamma^D = 50.8 \) \( \text{mN/m} \) and \( \gamma^P = 0 \) \( \text{mN/m} \) have been used in this study as in Refs. (38-40). Resolving this small controversy is beyond the scope of this study. However, the small differences in the surface energy values (cf. Table S6) do not affect the discussions presented here, as discussed in SI.03.

In addition, the topography of the substrate surface was characterized with AFM imaging (see SI.04). The surface roughness expressed in both \( R_a \) (arithmetic average roughness) and \( R_{rms} \) (root mean square average roughness) parameters (Table S7) increased slightly in the order from glass (\( R_a = 0.09 \) nm, \( R_{rms} = 0.11 \) nm), to unmodified silicon (\( R_a = 0.14 \) nm, \( R_{rms} = 0.17 \) nm), and UVO treated silicon (\( R_a = 0.17 \) nm, \( R_{rms} = 0.22 \) nm). All the substrates were however all relatively smooth, manifesting in a very low (\(< 0.2 \) nm) arithmetic average roughness, \( R_a \).

Table 1. Surface free energies (SFEs) and wettability of the substrates. The mean contact angle (CA) measurements between different substrates and droplets (5 \( \mu \text{L} \)) of Milli-Q water,
diiodomethane, ZnO nano/microfluids (in cyclohexane/isobutylamine 5:1 mixtures), and pinned CA of the control mixture (30 μL droplet, pinned CA). The SFEs were calculated using the Owens-Wendt method (31) (see SI.03, in which we note other methods also exist (e.g. Neumann, Fowkes, Owens-Wendt-Rabel-Kaelble, van Oss-Chaudhury-Good, and Zisman).

<table>
<thead>
<tr>
<th>Testing fluids</th>
<th>Microscope glass slide</th>
<th>Silicon wafer (Si)</th>
<th>UVO silicon wafer (UVO-Si)</th>
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<tr>
<td>In-house ZnO nanofluid</td>
<td>8.6 ± 2.0°</td>
<td>5.7 ± 1.2°</td>
<td>6.5 ± 1.7°</td>
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<tr>
<td>ZnO nanopowder nano/microfluid</td>
<td>5.5 ± 1.0°</td>
<td>6.0 ± 1.9°</td>
<td>5.5 ± 2.0°</td>
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<tr>
<td>ZnO powder nano/microfluid</td>
<td>5.6 ± 1.1°</td>
<td>5.9 ± 1.8°</td>
<td>4.1 ± 1.9°</td>
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<tr>
<td>Milli-Q water</td>
<td>21.7 ± 3.5°</td>
<td>56.5 ± 1.2°</td>
<td>9.8 ± 1.6°</td>
</tr>
<tr>
<td>Diiodomethane</td>
<td>29.6 ± 0.5°</td>
<td>52.0 ± 1.3°</td>
<td>41.1 ± 0.9°</td>
</tr>
<tr>
<td>Cyclohexane/isobutylamine mixture (pinned)</td>
<td>29.4 ± 4.3°</td>
<td>26.7 ± 1.5°</td>
<td>27.2 ± 2.4°</td>
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<table>
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<tr>
<th>Surface free energy (mN/m)</th>
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<tr>
<td>Total $\gamma$</td>
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<tr>
<td>Dispersive component $\gamma^D$</td>
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<tr>
<td>Polar component $\gamma^P$</td>
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**Descriptive account of the BM cells on three different substrates from ZnO nanofluid sessile drops**

An example of the residual surface pattern formed from the in-house synthesized ZnO nanoparticle (diameter ~ 9 nm) dispersion on hydrophilized UVO-Si is shown in Figure 1. (Figure 1a, d, and f are adapted from Ref. (27), which focused on the fractal dimension analysis. These results are included here to compare with the results on two other substrates shown in Figure 2 and Figure 3 below, for clarity and completeness.) It was composed of a central region with packed cellular structures surrounded by a coffee ring around the perimeter of the droplet.
(Figure 1b-c), comprising a dense network of intercalating fibers (Figure 1c). The central region of the residual surface pattern consisted of circular patches or cells – identified as solidified Bénard-Marangoni (BM) convection cells, with their diameters corresponding to the BM wavelength ($\lambda_{BM} = 200 - 800 \mu m$). The micromorphology of the cells resembles spoke-like patterns with a bow-tie projection (Figure 1d). Their appearance was also similar to the BM flow pattern observed during the evaporation of toluene from polystyrene/toluene solution [14]. One of the well-defined cells is shown in Figure 1f (whose fractal dimension analysis has been shown in detail in (27). The Marangoni number, $B$, which gauges the balance between the surface tension and the viscous force in a fluid, depends on the parameters such as the temperature gradient across the drop thickness, and the thermal diffusivity, dynamic viscosity, thermal conductivity, density, and specific heat capacity in the drop (7). For the fluid conditions with $B > 80$, spontaneously generated surface-tension driven flows will result in the formation of BM cells. For a drop of thickness $d$, the ultimate BM cell size or wavelength, $\lambda_{BM}$, is related to the Marangoni number by:

$$B = 32 \left( \frac{\pi d}{\lambda_{BM}} \right)^2.$$  

(1)

Wu and Briscoe (24) estimated that, in their ZnO nanofluid (ZnO nanoparticles dispersed in a mixture of chloroform, methanol and isobutylamine), the Marangoni number was much larger ($B \sim 300 - 2000$) than the critical value of 80 (24). They attributed the formation of the BM cells to the fluctuations in the fluid viscosity due to the variation in the local particle concentration during evaporation. It was also shown (24) that slow evaporation would not lead to the BM cell formation, which could be attributed to the insufficient temperature gradient across the thickness of the drop required to initiated the BM flow. Here we have observed $\lambda_{BM} = 200 - 800 \mu m$, giving a critical thickness range $d = 100 – 400 \mu m$ at which the BM instabilities were triggered. This variability is consistent with the interpretation that the concentration of the in situ generated molecular clusters and particulate species in the reactive ZnO nanofluid
was inhomogeneous inside the drop, leading to BM being triggered at different evaporation stages.

**Figure 1.** Residual surface pattern formed from a 30 μL sessile drop of the in-house synthesized ZnO nanofluid droplet dried on the UVO treated silicon wafer (UVO-Si): (a) overall optical microscopy image of the pattern; (b-c) enlarged views of an SEM image of a section close to the peripheral coffee ring; (d) a magnified view of a SEM image of the central region that reveals spoke-like patterns with a bow-tie projection, identified as solidified manifestation of Bénard-Marangoni (BM) convection cells; (e) intercalated fibers in the coffee-ring edge; and (f) a magnified view of a BM convective cell. Images in (a), (d), and (f) are adapted from Ref. (27) *J. Colloid Interface Sci.*, 2019, 536, Patryk Wąsik, Annela M. Seddon, Hua Wu, Wuge H. Briscoe, Dendritic surface patterns from Bénard-Marangoni instabilities upon evaporation of
a reactive ZnO nanofluid droplet: A fractal dimension analysis, 493-498, Copyright (2019), with permission from Elsevier.

Figure 2 shows that, similar to the residual pattern on UVO-Si, the glass surface was covered with solidified BM convection cells with overall smaller diameters, $\lambda_{BM} = 200 - 500 \, \mu m$ (Figure 2b-c). The packing density of the fibers inside BM cells appeared smaller, leading to a higher degree of interpenetration between different BM cells. Figure 2d shows the fibers constituting the BM cells, which are re-crystallized from gel-like fibers self-assembled from \textit{in situ} generated clusters, as discussed in detail in Ref (24).

Figure 2. Residual surface pattern formed from a 30 μL sessile drop of the in-house synthesized ZnO nanofluid droplet dried on a microscope glass slip: (a) overall optical microscopy image; (b) an SEM image of a section in the central region; (c) an enlarged view of the central region from (c) showing solidified manifestation of Bénard-Marangoni (BM) convection cells marked by yellow dotted circles; and (d) an enlarged view showing the fibrous structure constituting the BM cell.
An example residual surface pattern from the in-house synthesized ZnO nanofluid on an unmodified silicon wafer is presented in Figure 3. Similar to the other two substrates, the central region of the substrate was covered with solidified BM cells with a wide range of diameters, i.e., \( \lambda_{BM} = 250 - 1000 \) \( \mu \text{m} \), with the fiber-packing denser than those on the glass slide (cf. Figure 2) and also with significant interpenetrations at the BM cell peripheries.

**Figure 3.** Residual surface pattern formed from a 30 \( \mu \text{L} \) sessile drop of the in-house synthesized ZnO nanofluid droplet dried on an unmodified silicon wafer (Si): (a) overall optical microscopy image; (b) an SEM image of a section in the central region; (c) an enlarged view of the central region in (c) showing solidified Bénard-Marangoni (BM) convection cells with borders marked by yellow dotted circles; and (d) an enlarged view showing the fibrous structure constituting the BM cell.

**Bénard-Marangoni (BM) cell size \( \lambda_{BM} \) distributions on three different substrates**

The size distributions of the BM cells in the central region of the residual surface patterns were fitted with the log-normal distribution function (SI.06), with \( M \) denoting the geometric mean of the BM cell size \( \lambda_{BM} \) (i.e. the median size) by count and \( \sigma_g \) its geometric standard
deviation (i.e. the skewness and dispersion of the size distribution) (41). 68.3% of all the BM cells had the size between $M/\sigma_g$ and $M\cdot\sigma_g$ (42).

The solidified BM cells showed different size distributions on the three different substrates (i.e. glass, silicon and UVO exposed silicon), and the results from the in-house synthesized ZnO nanofluid (∼9 nm nanoparticle diameter) are presented in Figure 4. The smallest mean diameters ($M = 289\ \mu m$, Figure 4a) were observed on the glass substrate, with the smallest polydispersity ($\sigma_g = 1.25$, i.e. 68.3% of $\lambda_{BM}$ values lying in the range 252-375 $\mu m$). The BM cells on Si (Figure 4b) showed the largest mean sizes ($M = 466\ \mu m$), with a slightly higher diameter dispersion ($\sigma_g = 1.27$; 68.3% of $\lambda_{BM}$ in the range 367-592 $\mu m$). By comparison, $\lambda_{BM}$ on UVO-Si (Figure 4c) showed slightly smaller mean size values ($M = 423\ \mu m$), with the highest dispersion parameter $\sigma_g = 1.30$ (i.e. 68.3% of $\lambda_{BM}$ in the range 325-550 $\mu m$).

**Figure 4.** Size distributions of $\lambda_{BM}$ as the probability density function (PDF) of the BM cells in the central region of the residual surface patterns from the in-house synthesized ZnO nanofluid on the three different substrates: (a) microscope glass slide, (b) Si, and (c) UVO-Si. BM cell sizes distributions were fitted with the log-normal distribution function (dashed lines) (SI.06). Red vertical lines indicate the geometric mean $M$. BM cell sizes between $M/\sigma_g$ and
\( M \cdot \sigma_g \) (68.3% of all values) are shaded in the golden-yellow color under the size distribution curves.

Residual patterns were also studied using the commercially acquired ZnO nanopowder and ZnO powder (cf. Figure S1 in SI.01; at the same particle concentration of 1 mg/mL in the same solvent mixture, cyclohexane and isobutylamine in 5:1 volume ratio), which exhibited a wide range of sizes and morphologies. Figure S8 shows the SEM images of the central regions of the residual surface patterns from ZnO nanopowder and ZnO powder nano/microfluid droplets on glass, Si, and UVO-Si. The central regions of these patterns were also composed of solidified BM cells, with the dendritic fibers radiating from the cell center. In contrast to the results obtained for the in-house synthesized ZnO nanofluid (Figure 1 - Figure 3), the overall surface coverage and the fiber density in the BM cells were much higher, and there was also more significant inter-cell penetration. The optical microscopy of the overall patterns with the droplet footprints are shown in Figure S9 and Table S6.

A trend in the BM cell size distribution with respect to the substrate was similar to that observed with the in-house ZnO nanofluid. Specifically, the geometric mean BM cell size, \( M \), and the geometric standard deviation coefficient, \( \sigma_g \), increased in the order of glass, unmodified silicon and UVO treated silicon, confirming that the BM cell size depended on the substrate (Figure 5). The smallest \( M \) value was observed for the commercially acquired ZnO powder dried on glass \((M = 106 \, \mu m)\), and the biggest BM cells were created from the commercially acquired ZnO nanopowder on UVO-Si \((M = 515 \, \mu m)\).
Figure 5. Geometric mean size $M$ of Bénard-Marangoni cell size $\lambda_{BM}$ distribution produced from different nano/microfluids: (a) the in-house synthesized ZnO, (b) ZnO nanopowder, and (c) ZnO powder; formed on different substrates: glass (blue bars with cross “X” pattern), Si (orange bars with star “★” pattern), and UVO-Si (green bars with circle “O” pattern). The corresponding TEM images of the ZnO particles in the droplet dispersions are shown at the top. The error bars are calculated as $M/\sigma_g$ and $M\cdot\sigma_g$ for lower and upper errors, respectively, showing the distribution of $\lambda_{BM}$.

Box counting fractal dimension (FD) analysis of Bénard-Marangoni (BM) cell micromorphology

The results of the box counting fractal dimension (FD) analysis of the solidified BM cells on different substrates are presented in Figure 6, and all the FD values were in the range $D \approx 1.66$.
The fractal dimension of a pattern reflects its geometrical properties, i.e. how much space it fills when it is scaled up or down or the prominence of its irregularities (43). It can also be used to quantify the ruggedness of particle boundaries (44). Fractal dimensions, in contrast to topological dimensions, can take non-integer values. For reference, a line is 1-dimensional, a surface is 2-dimensional, and a cube is 3-dimensional object. Classical fractals such as the Koch snowflake or the Sierpiński triangle have dimensions of $D \approx 1.262$ and $1.585$, respectively (45). If these structures are scaled up, the Sierpiński triangle would cover more area than the Koch snowflake. However, both of them would cover less area than a scaled up square ($D = 2$), which would fill the entire area; but more than a scaled line ($D = 1$), which would not fill any area at all (43). The distribution of the $D$ values for the BM cells was calculated as a probability density function (PDF) as shown in Figure 6a, c and d (left hand side). The fitting parameters, $\mu$ and $\sigma$, the mean value and its standard deviation respectively, are also listed in the figure for the normal distribution fits, shown as dashed lines $h_1$, $h_2$ and $h_3$, respectively for glass, Si and UVO-Si and for different ZnO nano/microfluids. In addition, the apparent trends in the mean value and its standard deviation of fractal dimension distribution are shown in Figure 7.

The BM cells formed from the in-house ZnO nanofluid on the glass substrate ($h_1$ in Figure 6a) had the lowest average $D$ value of $\mu = 1.77$ with the highest dispersion of $\sigma = 0.04$, amongst all samples (Figure 7). BM cells formed on both unmodified and UVO treated silicon resulted in higher and less dispersed $D$ values, with $\mu = 1.84$ ($\sigma = 0.02$) and $1.82$ ($\sigma = 0.03$), respectively ($h_2$ and $h_3$ in Figure 6a). The scatter in the $D$ values is qualitatively consistent with our interpretation that there were local inhomogeneities in the viscosity and thermal properties in a drying droplet. The various flow rates and solute concentrations involved in the self-assembly process in different BM flow cells would result in a different packing in the dried cell, and in turn different fractal dimension values.
The $D$ values for the BM cells from the other ZnO particles exhibited a smaller scatter ($D \sim 1.82 – 1.84$). For the ZnO nanopowder BM cells, these values were, $\mu = 1.83\, (\sigma = 0.01), 1.83\, (\sigma = 0.03)\), and $1.84\, (\sigma = 0.02)$, on glass, Si, and UVO-Si ($h_1, h_2,$ and $h_3$ in Figure 6c, and Figure 7c), respectively. Similarly for the BM cells produced from the ZnO powder nano/microfluid, the corresponding values are $\mu = 1.82\, (\sigma \approx 0.02), 1.84\, (\sigma = 0.03),$ and $1.84\, (\sigma = 0.02)$, on the three substrates ($h_1, h_2,$ and $h_3$ in Figure 6e, and Figure 7b).

### Variation of BM cell fractal dimension with its size: Growing fractals vs. maturing fractals

The fractal dimension values are also plotted against BM cell diameters ($D$ vs. $\lambda_{BM}$) on the right hand side of Figure 6 (b, d and f). There appears a general trend that $D$ increases with $\lambda_{BM}$ for all the conditions investigated, a trend that has also been observed from a benchmark FD analysis of classic fractals such as a hexaflake and the Sierpiński carpet (27) (also see SI.07). The rate of increase is much higher for small BM cell diameters of $\lambda_{BM} < 200\, \mu$m, before a plateau is reached for higher $\lambda_{BM}$ values. The data for different substrates is enveloped in colored areas for comparison. This trend is consistent with the observation that the BM cells had a more open structure (and thus smaller surface coverage) towards the cell centre, leading to smaller $D$ values for smaller $\lambda_{BM}$. As a result, the BM cells with bigger diameters exhibited larger $D$ values, and thus had more rugged structures. This is an interesting result. A fractal is characterized by its constant FD value as it is scaled up or down. Here we show that the solidified BM cells and the classical fractal patterns all display a smaller $D$ value for smaller fractals, and their fractal dimensions then reached a plateau value that is consistent to what has been reported in the literature. We suggest that the FD analysis has revealed two regimes of the fractal growth: an initial stage of growing fractals with a more open structure and a subsequent stage of maturing fractals, and this trend has not been reported previously.
The trend may be fitted to a logarithmic function, \( y = a \ln(\lambda_{BM}) + D_0 \), shown as the dashed lines in the figure labelled as \( y_1, y_2 \) and \( y_3 \) for the patterns on glass, Si, and UVO-Si, respectively (Figure 6b, d and f). It should be acknowledged that the choice of the function is arbitrary, mostly as a guide for the eye. We discuss the physical meanings of the fitting parameters in a qualitative manner to compare different conditions. A different fitting function would have equally described the trend (e.g. a polynomial), but the discussion below is qualitatively valid and internally consistent.

A smaller \( D_0 \) and larger \( a \) can be indicative of the presence of more voids (i.e. unoccupied areas) towards the center of the dendritic pattern of a BM cell. The BM cells from the ZnO powder resulted in the highest intercept values \( D_0 \) (in the range of 1.71 - 1.80), and the lowest \( a \) values in the range of 0.01 - 0.02, for all the investigated substrates, indicating the highest fibre density in the BM cells. This is followed by patterns from the ZnO nanopowder on glass and UVO-Si, with \( D_0 \) values equal to 1.69 and 1.71, and \( a \) values ~ 0.03 and 0.02, respectively. However, the results from the patterns produced from the ZnO nanopowder nano/microfluid on Si \( (D_0 = 1.51, a = 0.06) \) are similar to those from the in-house synthesized ZnO nanofluid on all the substrates \( (D_0 = 1.42 - 1.62, \text{ and } a = 0.04 - 0.06) \).

The BM cells from the in-house ZnO nanofluids on glass exhibited the smallest FD values \( (\mu = 1.77) \) compared to the silicon substrates (\( h_2 \) and \( h_3 \) vs. \( h_1 \) in Figure 6b). This could be reconciled with the \( D \) vs. \( \lambda_{BM} \) trend, as the corresponding BM cell size was the smallest \( (M = 289 \, \mu m, \text{ Figure 4}) \). In addition, the smallest FD value on glass may also be related to the lack of interpenetration between the smaller cells. ZnO nanopowder and ZnO powder nano/microfluids produced residual surface patterns (Figure S8) with the highest fiber density and the highest level of inter-cell penetration. Even though the BM cells varied widely in diameters \( \lambda_{BM} \), from \( M = 101 \, \mu m \) for the ZnO powder patterns on glass (Figure S10g) to \( M = 558 \, \mu m \) for the ZnO nanopowder patterns on UVO-Si (Figure S10f), the fractal dimension
analysis revealed that all of them had average $D$ values between $\mu \approx 1.82 - 1.84$ (Figure 6c and e) comparable to the BM cells produced from the in-house ZnO nanofluid on Si and UVO-Si ($\mu = 1.84$ and 1.82, respectively), but much larger than the average fractal dimension for the BM cells on glass ($\mu = 1.77$) (Figure 6a). This suggests that the smallest FD value on glass was also related to the lack of interpenetration/overlapping between BM cells.

**Figure 6.** Box counting fractal dimension analysis of the solidified Bénard-Marangoni (BM) cells formed from drying ZnO nano/microfluids composed the in-house synthesized ZnO nanoparticles (a- b), ZnO nanopowder (c-d), and ZnO powder (e- f), on three different
substrates, microscope glass slide, Si, and UVO-Si. Left hand side plots (a, c and e) show fractal dimension (FD) distribution for all the samples, fitted with the normal (Gaussian) distribution function. Data fits are shown as dashed lines and labelled as $h_1$, $h_2$ and $h_3$, respectively for glass, Si and UVO-Si for each ZnO nano/microfluid. Parameters $\mu$ and $\sigma$ stand for the mean $D$ and its standard deviation. Right hand side plots (b, d, f) show the calculated box counting fractal dimension, $D$ vs. the diameter of the investigated BM cell, $\lambda_{BM}$. Dashed lines labelled $y_1$, $y_2$, and $y_3$, show logarithmic fits. The scatter in the data is indicated by the colored regions that enclose the data points.

**Figure 7.** Average fractal dimension, $\mu$, calculated for the Bénard-Marangoni (BM) cells produced from different nano/microfluids: (a) the in-house synthesized ZnO, (b) ZnO nanopowder, and (c) ZnO powder; formed on different substrates: glass (blue bars with “X” pattern), Si (orange bars with star “★” patterns), and UVO-Si (green bars with circle “O” patterns). The error bars are calculated as $\pm \sigma$, which stand for standard deviation calculated from normal (Gaussian) distribution.
Further discussion on the effect of substrate surface chemistry

As shown in Table 1, all the substrates exhibited hydrophilic character, as their water contact angles CA were smaller than 90°. However, the hydrophilicity was in the decreasing of hydrophilized UVO-Si, microscope glass slide and untreated Si, evident both from the water CA and the polar components of the SFE $\gamma_p$.

The surface of a silicon wafer is covered with a native layer of silicon oxide or silica (SiO$_2$), which forms naturally when a silicon surface is exposed to air in ambient conditions (46). The surface of silicon oxide consists mainly of silanols (Si-OH), siloxanes (Si-O-Si), and their permutations (47). Silanol groups are responsible for hydrophilic interactions due to their ability to form the hydrogen bond with water. In contrast, siloxanes and other species present on the SiO$_2$ surface, such as Si-H, Si-CH$_3$, and Si-F, are responsible for hydrophobic interactions due to their homopolar character (48). A prolonged UVO exposure of a silicon wafer in air leads to the formation of silanol groups in a reaction of chemical entities produced from bond breaking in the Si-O-Si surface structure and dissociation of water molecules (29). This in turn greatly increases the hydrophilicity of a UVO treated Si substrate.

The glass surface is composed of the same SiO$_2$ tetrahedral building block as crystalline silica. However, the arrangement of these tetrahedral units is characterized by the absence of long-range order and the presence of ring-like structures, caused by network modifier ions (Ca$^{2+}$, Mg$^{2+}$, Na$^+$, or K$^+$) and non-bridging oxygens (49). Nevertheless, it is expected that the surface chemistry of the microscope slides, made of silicate glasses, is governed by the relative populations of silanol (Si-OH), siloxide (Si-O$^-$), and siloxane (Si-O-Si) surface groups, similar to amorphous silica films (50).

Taking the above into account, the three substrates used in this work, microscope glass slide, silicon wafer and hydrophilized silicon wafer exhibited different levels of hydrophilicity due to different compositions of hydrophilic (silanols, siloxides) and hydrophobic (siloxanes)
groups present on their surfaces. The hydrophilized silicon wafer possessed the highest ratio of silanols, generated by the UVO exposure, followed by microscope glass slide, and unmodified silicon wafer.

In general, the solvent evaporation dynamics proximal to the surface and at the dewetting front is affected by the surface wettability by the dispersion, and in turn the substrate surface chemistry. Upon evaporation of a droplet of radius $R$ with a contact angle $\theta$ on the substrate at the three-phase contact line, the evaporating flux $J(r)$ at a distance $r$ from droplet center scales as $J(r) \propto (R - r)\lambda$, where $\lambda = (\pi - 2\theta)/(2\pi - 2\theta)$ (51). This indicates that the evaporation flux prominent in the coffee ring formation mechanism is similar on all the three substrates, due to the similar initial pinned CA values and those for the nano/microfluids. The significant difference among the three substrates is their hydrophilicity, as indicated by the different water CA values on these substrates and different SFE polar components $\gamma^p$, which would give rise to different affinities for water molecules and also the amphiphilic molecular clusters generated in situ upon evaporation (24).

In the mechanism described in (24), reactive ZnO particles are proposed to alter evaporation induced solvent via in situ generated molecular and particulate species. ZnO nanoparticles may undergo rapid chemical transformation into isobutylamine-ZnOH molecular complexes (iZMCs) of sub-nanometer in size, which further self-assemble into nanoclusters as stimulated by the presence of polar molecules – particularly trace amounts of water. The hydrolysis of isobutylamine by water encourages the formation of iZMCs. These surface active iZMCs and clusters accumulate at the sessile drop surface and the peripheral contact line, and would also adsorb to the substrate. As the drop thins, BM instabilities are triggered, and iZMC-cluster coalescence along multiple BM flows leads to the formation of the central cellular patterns. Concurrently, this dendritic cluster growth also occurs at the receding peripheral contact line on the substrate. Further drying drives iZMC organization on the substrate into crystal lattices.
in the micro-dendrites in the final hierarchical polycrystalline surface structures. Here we show that different surface hydrophilicity of the substrate would affect its interactions with the iZMCs and their self-assembled clusters. This presumably would affect the cluster density, local viscosity, and solvent flows proximal to the substrate during evaporation. It would also influence the final recrystallization on the substrate in which the iZMCs reorganize into the crystal lattices, a process affected by the inter-cluster interactions and the cluster-substrate interactions, both of which would depend on the presence of trace amounts of water.

CONCLUDING REMARKS

We have observed that the solidified BM dendritic cells formed upon evaporation of sessile drops containing ZnO particulate dispersions in a mixed solvent on three different substrates varying in hydrophilicity. The BM cell size distribution and its fractal dimension both depended on the substrate on which evaporation occurred. The BM cells had the smallest diameters and density on the glass surface when compared to unmodified and hydrophilized silicon substrates for all the ZnO nano/microfluids studied. Meanwhile, the spoke-like radial BM cell structures formed on the UVO hydrophilized silicon had the largest diameters with the widest spread in dimensions.

Fractal dimensional analysis of the BM cells provided a quantitative description of the geometric properties of these structures, to describe their ruggedness or how much space it fills when the structure is scaled up or down (43-44). It was shown that the in-house ZnO nanofluid produced bigger BM cells with much higher degree of inter-cell overlapping on both unmodified and UVO treated silicon substrates ($D = 1.84 \pm 0.02$ and $1.82 \pm 0.03$, respectively) than on glass ($\mu \approx 1.77 \pm 0.04$). On the other hand, ZnO nano/microfluids prepared from the commercially acquired ZnO nanopowder and ZnO powder produced patterns of the highest coverage and level of overlapping of the BM cells, manifested in average $D$ in range $1.82$ - $1.84$ on all the substrates. The observed trend of the fractal dimension $D$ increasing with the
increasing BM diameter $\lambda_{BM}$ is indicative of a two stage fractal growth, with the smaller BM cells representing growing fractals with a more open structure, and the larger mature BM dendrites possessing a more complicated structure with overlapping boundaries with adjacent BM cells.

As discussed in the previous work, the presence of water molecules is crucial for the moisture-assisted dissolution of ZnO nanocrystals dispersed in a mixture of cyclohexane and isobutylamine (25-26), as well as subsequent cluster formation and recrystallization on the substrate. We attribute the observed different BM cell characteristics (size distributions and FD values) to different surface chemistry of the substrates, particularly their hydrophilicity. Conversely, this provides a mechanism for controlling the morphology of hierarchical surface patterns created after the evaporation of a ZnO nano/microfluid sessile drop.

**SUPPORTING INFORMATION**

The Supporting Information (SI) associated with this article can be found, in the online version, at https://doi.org/XXX. The SI contains: SI.01: ZnO particles; SI.02: UV/Ozone treatment of Si wafer substrates; SI.03: Contact angle (CA) characterization and surface free energy (SFE) calculations; SI.04: Atomic force microscopy (AFM) of the substrates SI.05: Characterization of the residual surface patterns; SI.06: Bénard-Marangoni cell size distribution - log-normal fitting; and SI.07: Fractal dimension analysis of the Bénard-Marangoni cells.

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REFERENCES


ZnO nanofluid droplet

Fast evaporation

Different substrates

Glass

Silicon

UVO Silicon

Solidified Bénard-Marangoni cells

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