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Development of texture and seismic anisotropy during the onset of subduction

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[1] How reliable are shear wave splitting measurements as a means of determining mantle flow direction? This remains a topic of debate, especially in the context of subduction. The answer hinges on whether our current understanding of mineral physics provides enough to accurately translate between seismic observations and mantle deformation. Here, we present an integrated model to simulate strain-history-dependent texture development and estimate resulting shear wave splitting in subduction environments. We do this for a mantle flow model that, in its geometry, approximates the double-sided Molucca Sea subduction system in Eastern Indonesia. We test a single-sided and a double-sided subduction case. Results are compared to recent splitting measurements of this region by Di Leo et al. (2012a). The setting lends itself as a case study, because it is fairly young and, therefore, early textures from the slab’s descent from the near surface to the bottom of the mantle transition zone—which we simulate in our models—have not yet been overprinted by subsequent continuous steady state flow. Second, it allows us to test the significance of the double-sided geometry, i.e., the need for a rear barrier to achieve trench-parallel subslab mantle flow. We demonstrate that although a barrier amplifies trench-parallel subslab anisotropy due to mantle flow, it is not necessary to produce trench-parallel fast directions per se. In a simple model of A-type olivine lattice-preferred orientation and one-sided subduction, trench-parallel fast directions are produced by a combination of simple shear and extension through compression and pure shear in the subslab mantle.

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1. Introduction

[3] Various seismological methods have shed light on the structure of the Earth’s interior. In the case of subduction zones, for example, traveltime tomography [e.g., van der Hilst et al., 1991] or the accurate locating of slab seismicity [e.g., Gudmundsson and Sambridge, 1998; Gutscher et al., 2000] can provide a first-order image of subducting slabs and—to some extent—the surrounding mantle (see Lay [1994], for a review). These methods do not, however, constrain mantle convection as such.

[3] Currently, our best diagnostic tool for determining in situ mantle flow direction is seismic anisotropy: the directional dependence of seismic wave speed. This is due to the fact that in a dry upper mantle, olivine deformation is permitted mainly by the motion of dislocations belonging to the (010)[100] slip system. For progressive simple shear, this leads to the development of lattice-preferred orientation (LPO) of olivine-rich rocks, with the a axes aligned parallel to the mantle flow direction and the b axes perpendicular to the shear plane [e.g., Ribe, 1989; Babuška and Cara, 1991; Mainprice, 2007]. This is known as A-type LPO, which is observed both in LPO development models [e.g., Wenk et al., 1991; Tommasi et al., 2000] and experimentally deformed peridotites [e.g., Nicolas et al., 1973; Avé-Lallemant, 1975; Zhang and Karato, 1995; Bystricky et al., 2000]. The strain-induced mineral textures affect seismic wave propagation, a fact that manifests itself in shear wave splitting. When traversing an anisotropic medium (e.g., the convective upper mantle), a shear wave splits into two orthogonally polarized shear waves traveling at different speeds. The two parameters describing shear wave splitting are the delay time between those two shear waves (δt) and the polarization of the faster wave (ϕ), which is determined by the symmetry axis of the medium. For A-type olivine LPO, ϕ is parallel to the olivine a axes for vertically traveling shear waves and, therefore, parallel to the direction of (horizontal) mantle flow.

[4] Measurements of shear wave splitting have frequently been used to infer mantle flow in subduction zones. Source-side S wave splitting has proven especially useful in constraining anisotropy in the subslab mantle [e.g., Russo and Silver, 1994; Müller et al., 2008; Di Leo et al., 2012a, 2012b; Lynner and Long, 2013]. A topic of debate, however, is the predominance of trench-parallel fast directions, which most authors ascribe to trench-parallel subslab mantle flow. This interpretation seems counterintuitive in light of the classic model of 2-D mantle flow in subduction systems [e.g., McKenzie, 1969].

[5] Furthermore, it has often been pointed out that caution needs to be exercised when directly inferring mantle flow direction from shear wave splitting fast orientations [e.g., Ribe, 1989; Dawson and Wenk, 2000]. This is especially the case in regions of density-driven mantle flow, such as subduction zones, where mantle flow velocities and trajectories do not necessarily parallel those of the overriding plate due to partial decoupling of plate and mantle, and sharp changes in flow direction may occur [e.g., Jadamec and Billen, 2010, 2012; Di Leo et al., 2012b].

[6] One approach to testing whether the prevalent translation between seismic anisotropy observations and mantle flow direction through mineral physics are correct is to simulate strain-induced LPO development and subsequently predict the resultant shear wave splitting. This technique has been successfully applied to subduction settings in a number of previous studies [e.g., Hall et al., 2000; Blackman and Kendall, 2002; Lassak et al., 2006; Faccenda and Capitanio, 2012, 2013].
With the marked exception of recent work by Faccenda and Capitanio [2012, 2013], these earlier models have two significant shortcomings: (1) they are two-dimensional and (2) they only consider instantaneous, steady state mantle flow solutions.

That mantle flow is far more complex (i.e., three-dimensional) beneath subduction zones has been demonstrated in numerous analogue experiments [Buttles and Olson, 1998; Kincaid and Griffiths, 2003; Schellart, 2004; Funicello et al., 2006; Druken et al., 2011], numerical models [Piromallo et al., 2006; Stiegemann et al., 2006; Lowman et al., 2007; Kneller and van Keken, 2007; Capitanio and Morra, 2012; Capitanio and Faccenda, 2012], and seismic observations (see Long [2013] for a recent review), and this should therefore be taken into account. Equally important is the need to consider the entire strain history of the deformed mantle, as LPO textures are a function of the accumulated finite strain, but also the variation of flow velocity gradients along the path a volume of rock has traveled [e.g., Kaminski and Ribe, 2002].

Here, we present an integrated model simulating subduction-history-dependent upper mantle LPO evolution and the resulting shear wave splitting. We compare results to observations from the Sangihe subduction zone in the Sulawesi-Philippine region.

A shear wave splitting study was recently conducted on the Sangihe subduction zone (Figure 1) [Di Leo et al., 2012a]. This subduction zone is unique in that it is the western dipping part of the only present-day double-sided subduction system; the Molucca Sea microplate is also subducting eastward at the Halmahera trench. Through a combination of local $S$, SKS, and source-side

Figure 1. (left) Map of the Sulawesi-Philippine region in SE Asia. Subduction zones are marked by lines with barbs pointing in the direction of slab dip (redrawn after Hall and Nichols [1990]; Hall [1997]; Macpherson et al. [2003]; Djajadihardja et al. [2004]). (right) Shear wave splitting results for the Sangihe subduction zone from Di Leo et al. [2012a]. Bars are oriented in the fast direction, their length is proportional to the delay time. Source-side results (gray) are plotted at the source, SKS results (black) are plotted at station MNI (inverted triangle). Slab contours (gray) [Gudmundsson and Sambridge, 1998] are in 50 km depth intervals. Both SKS and source-side splitting measurements predominantly show trench-parallel fast directions.
S-splitting observations, Di Leo et al. [2012a] inferred trench-perpendicular flow in the wedge above the subducting slab. The trench-parallel fast directions measured on the seaward side were attributed to trench-parallel escape flow beneath the slab in response to a volume decrease in the subslab mantle due to the double-sided subduction.

[10] In the following, we investigate whether shear wave splitting patterns observed in the mantle wedge and subslab region of the Sangihe subduction zone can be simulated in our model. For example, we test whether it is possible to produce trench-parallel fast directions from subslab mantle flow in a simple one-sided subduction model, where deformation is dominated by the motion of dislocations belonging to the (010)[100] slip system. We then compare these results to a two-sided subduction model to see how large an effect the unique double-sided geometry has.

[11] Unlike previous studies, we consider the entire subduction history, from initiation to stagnation at the 660 km discontinuity. This approach is appropriate for the Sangihe subduction zone, because it is fairly young (~25 Ma) [Jaffe et al., 2004] and the slab has only just reached the bottom of the mantle transition zone [Tatsumi et al., 1991; Gudmundsson and Sambridge, 1998]. In older subduction zones, where the slab has either been stagnating at the 660 km discontinuity for several million years or penetrated into the lower mantle, early textures developed during the slab’s initial descent may eventually be destroyed by subsequent continuous mantle flow.

2. Methodology

[12] Our model to determine shear wave splitting due to strain-induced olivine LPO in a subduction setting consists of four steps: (1) we simulate mantle flow in a subduction zone that is designed to resemble the Sangihe subduction zone. Here, we test a single-sided and a double-sided subduction case, (2) texture evolution in the resulting subduction strain field is then modeled, (3) the corresponding aggregate elastic constants are determined, and (4) the resulting effective shear wave splitting is estimated.

2.1. The Mantle Flow Model

[13] To simulate mantle flow in a subduction zone, we use the 3-D numerical boundary element model (BEM) of Li and Ribe [2012]. The subducting plate is represented by a dense fluid sheet sinking in a horizontally infinite ambient mantle of lower viscosity. The model setup is similar to that of an analogue laboratory experiment [e.g., Funiciello et al., 2006]. However, an advantage of the boundary element method is that it allows for a laterally infinite mantle medium (i.e., without any sidewalls). In contrast, side boundaries always play a role in both laboratory experiments and numerical methods with finite-element or finite-difference approaches.

[14] We start with a small initial dip at one end of the plate, then the slab sinks under its own weight, i.e., due to slab pull (Figure 2). We define a rigid lower boundary at \( H \approx 660 \) km to represent the bottom of the mantle transition zone, at which the slab stagnates (Figure 2). The trench rolls back as the slab subducts. The upper boundary of the mantle medium is free-slip and impermeable. A thin lubrication layer (of the same viscosity \( \eta_1 \) as the mantle) prevents the entire plate from sinking. The initial geometry of the sheet is given by its width \( w \), thickness \( h \), the lengths of the plate \( L \), and slab \( l \), as well as the dip of the slab’s leading edge. We define plate length as \( (L + l) \approx 2040 \) km and plate width as \( w \approx 1020 \) km. We choose these parameters to approximate the geometry of the Molucca Sea plate and Sangihe subduction zone.

[15] The mode of free subduction (i.e., trench advance or retreat, slab folding, etc.) depends on several factors, as previous numerical and experimental studies have shown [e.g., Bellahsen et al., 2005; Di Giuseppe et al., 2008; Funiciello et al., 2008; Schellart, 2008; Ribe, 2010; Stegman et al., 2010; Li and Ribe, 2012]. These factors include the plate/mantle viscosity ratio, \( \gamma = \eta_2/\eta_1 \), and the mantle depth/plate thickness ratio, \( H/h \). Since we assume that \( H \approx 660 \) km and that the slab has a dip of \( \sim 60^\circ \) [Tatsumi et al., 1991], then the preferred BEM solution has \( \gamma = 200 \) and \( H/h = 7.8 \), resulting in \( h \approx 85 \) km, which is a reasonable estimate of slab thickness in the Sangihe subduction zone [Di Leo et al., 2012a].

[16] The flow field evolves through time as the slab sinks. Figure 3 shows instantaneous flow at the final time step for the single-sided and the double-sided model.

2.2. Polycrystal Pathlines

[17] Since the mineral texture of a polycrystalline aggregate (hereafter referred to as “polycrystal”) is the result of its entire strain history, we need to
follow the polycrystal’s path from the beginning of the deformation phase to the point where we measure its texture. For our subduction model, this means that we need to trace the polycrystal from subduction initiation to stagnation of the slab at the lower boundary (“the 660”). We choose a number of passive tracer particles that end up in vertical columns at the end of the model run (i.e., at slab stagnation). These particle columns will represent vertically incident raypaths for the synthetic SKS waves in the subsequent calculation of shear wave splitting. The initial locations of the particles, however, are unknown. Therefore, we run the model backward to find these initial conditions (based on the reversibility of Stokes flow), and then forward again to calculate the textures.

In each model (single-sided and double-sided), we consider 18 columns. The spacing between columns in a row is ~80 km. For the single-sided subduction case, we choose nine columns on the wedge side and nine on the seaward side to study anisotropic conditions above and below the slab, respectively. In the double-sided case, we choose one row of nine in the axial plane of the “anticlinal fold” of the plate and one row just off-center. The conditions in the wedge are the same in the single-sided and in the double-sided case. We only examine columns for half of the slab—from the center outward—as the model has mirror symmetry across the central vertical plane. Furthermore, the columns only extend down to \( x_3 \approx 410 \) km, since we are only examining texture development in olivine.

We discretize each pathline into 150 steps of equal traveltime. At each step, we calculate the velocity gradient \( L \) (the change in velocity \( v \) with position \( x \)):

\[
L_{ij} = \frac{dv_i}{dx_j},
\]

which is the essential quantity for the following calculation of mineral textures, because it contains information about both macroscopic strain rate and rotation rate. \( L \) comprises a symmetric part, which is the strain rate tensor \( \mathbf{E} \), and a skew-symmetric part, which is the rotation rate tensor \( \mathbf{W} \):
where

\[ L = E + W, \]  

respectively, and \( R \) is a transformation matrix with columns containing the three eigenvectors of the strain rate tensor.

### 2.3. Textural Evolution: The Viscoplastic Self-Consistent Approach

LPO textures form when, due to externally imposed deformation, a significant number of crystals rotate and preferentially align within a polycrystalline aggregate (e.g., olivine crystals in a convective upper mantle). To calculate deformation-induced olivine textures, we use the anisotropic viscoplastic self-consistent (VPSC) model of Lebensohn and Tomé [1993]. The key idea is that each grain is treated as an ellipsoidal inclusion in a homogeneous effective medium (HEM), the properties of which are given by the average properties of the entire polycrystalline aggregate. Inputs to this model are the macroscopic strain rate tensor, \( \dot{E} \), and parameters.

Figure 3. Instantaneous flow in the (left) single-sided and (right) double-sided model at the final time step. (c and d) Vertical cross-sections and (e and f) horizontal cross sections.
describing how individual slip systems permit single crystal deformation in response to grain-scale stress, \( \sigma \). The strain rates for each crystal, \( \dot{\varepsilon}_g \), the macroscopic stress, \( \Sigma \), and the interaction tensor, \( M \), are calculated iteratively for each time step along each pathline to yield a self-consistent solution to the equation:

\[
\dot{\varepsilon}_g = \frac{-\alpha M_{ijkl}(\sigma_{kl} - \Sigma_{kl})}{2}
\]

where the parameter \( \alpha \) describes the interaction between the HEM and the grains. In the upper bound or Taylor [1938] model \( \alpha = 0 \), whereby strain is equal in each grain and hence homogeneous throughout the polycrystal, meaning that each crystal deforms identically, irrespective of its orientation. For this to be viable without opening any voids at grain boundaries, a crystal requires a minimum of five independent slip systems [von Mises, 1928], which is not the case for olivine. We therefore add two auxiliary slip systems with extremely high critical resolved shear stresses (Table 1). Texture development is not affected by these extra slip systems. With increasing \( \alpha \), stresses in each grain become more similar. We here choose \( \alpha = 1 \) in agreement with Lebensohn and Tomé [1993] tangent model. Once the self-consistent solution is found and the shear rate for each slip system in each grain is known, it is possible to compute the rate of rotation of each crystal due to dislocation accommodation by plastic deformation. Differences in this plastic rotation rate lead to the development of an LPO, while adding the macroscopic rotation allows the texture to rotate as a whole.

Each polycrystal in our model consists of 500 initially randomly oriented grains. The orientations are denoted by three Euler angles \( (\varphi_1, \Phi, \varphi_2) \), which give the rotation of the crystal lattice from the external Cartesian frame used for the flow modeling. The corresponding velocity gradient is applied to each polycrystal at each step along its pathline. At its final point in the vertical column the polycrystal has therefore recorded the entire strain history of the subduction process. The potentially active olivine slip systems, their critical resolved shear stresses (CRSS), and stress exponent \( (n) \) used here are listed in Table 1. Starting with a random distribution, the textures develop gradually along the 150 points of the pathline. The textures obtained from the VPSC calculations are represented by crystal orientations for each of the 500 grains. At the finishing point of the pathline, these new Euler angle triplets are then used to calculate the effective elastic constants for the textured polycrystalline aggregates by Voigt-Reuss-Hill averaging the single crystal olivine elasticity tensors over all the crystal orientations [e.g., Mainprice et al., 1990; Walker et al., 2011; Walker and Wookey, 2012].

A limitation of the VPSC model is that it assumes crystallographic axes rotations (which lead to LPO development) to result exclusively from slip on a number of fixed slip planes. Other potentially texture-producing or texture-modifying processes such as diffusion creep, grain boundary sliding, grain boundary dislocation climb, or dynamic recrystallization are not taken into account.

Recrystallization—through grain growth (boundary migration) and/or grain nucleation—is likely to occur at high temperatures and high strains [Carter, 1976; Karato, 1988]. Several experimental and numerical studies have focused on how recrystallization may affect LPO of olivine and enstatite, the two dominant upper mantle minerals [e.g., Nicolas et al., 1973; Karato, 1988; Zhang and Karato, 1995; Wenk and Tomé, 1999; Kaminski and Ribe, 2001; Blackman et al., 2002]. Natural and experimental samples appear to indicate that at large strain, recrystallization produces local misorientations, which can dilute the overall LPO [e.g., Nicolas et al., 1973; Karato, 1988; Bystricky et al., 2000; Zhang et al., 2000; Falus et al., 2011]. At modest strain, recrystallization can accelerate LPO formation [e.g., Zhang and Karato, 1995; Zhang et al., 2000]. However, Tommasi [1998] noted that by disregarding dynamic recrystallization, VPSC simulations tend to overestimate LPO intensity for high strains, but correctly predict LPO patterns. Moreover, Wenk and Tomé [1999] came to the conclusion that although there are differences between dislocation glide and recrystallization textures, the effects on seismic wave propagation are negligible.

![Table 1. Olivine Slip Systems, Their critical Resolved Shear](image)

Table 1. Olivine Slip Systems, Their critical Resolved Shear [from Wenk et al., 1991]*

<table>
<thead>
<tr>
<th>Slip System</th>
<th>CRSS</th>
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<tbody>
<tr>
<td>(010)[001]</td>
<td>0.4</td>
<td>3</td>
</tr>
<tr>
<td>(001)[001]</td>
<td>0.4</td>
<td>3</td>
</tr>
<tr>
<td>(010)[001]</td>
<td>1.0</td>
<td>3</td>
</tr>
<tr>
<td>(110)[100]</td>
<td>5.0</td>
<td>3</td>
</tr>
<tr>
<td>(021)[110]</td>
<td>5.0</td>
<td>3</td>
</tr>
</tbody>
</table>

*Note that two auxiliary slip systems must be invoked to fulfill von Mises’ criterion.
2.4. Estimating Shear Wave Splitting

From the obtained elasticity tensors, we can now determine the effective shear wave splitting arising from upper mantle olivine LPO that one would measure if seismometers were installed at the surface. Since a variation of splitting parameters with backazimuths can be indicative of multiple layers of anisotropy [Silver and Savage, 1994], we measure shear wave splitting for vertically incident SKS phases with polarizations (corresponding to backazimuth) between 0° and 180° in steps of 5° for each column.

We use two approaches. First, we follow the method of Silver and Savage [1994] for shear wave splitting in the case of multilayer anisotropy [see also Walker and Wookey, 2012]. When an incident shear wave traverses multiple layers of anisotropy along its path to the receiver, every layer will cause that wave to split. However, the frequency is most likely too low to produce identifiable pulses for each layer. What is observed instead is apparent or effective splitting, which is a combination of all the individual splitting operators. In the case of our model, that means that every textured olivine aggregate in the final column (e.g., Figure 4) represents a layer of anisotropy. Splitting operators are determined for each layer, and the effective splitting operators are retrieved for each column, i.e., each SKS wave.

In the second method we use to calculate the effective splitting parameters, the individual splitting operators along the vertical column (i.e., the SKS raypath) are applied in sequence to an unsplit first-derivative Gaussian wavelet; then the effective splitting operator that minimizes the second eigenvalue of the covariance matrix of the result is determined [Silver and Chan, 1991]. This ray theory approach is similar to that implemented by Bonnin et al. [2012]. The average difference between these results and those obtained with the Silver and Savage [1994] method is 9.10° for fast direction and 0.37 s for delay time, which is within typical error of shear wave splitting measurements of nonsynthetic data. Hereafter, we show results obtained with the second method.

3. Results

3.1. Textures

3.1.1. Single-Sided Subduction: The Mantle Wedge

Figure 5 shows textures in the center of the mantle wedge at the end of the model run. Near the surface, there are well-developed textures with strong orientation of olivine a axes horizontal and perpendicular to the trench (i.e., parallel to the x direction). The b and c axes show a girdle distribution. The textures are indicative of axial extension in the x direction. Simple shear textures are clearly evident at the bottom of the wedge, nearest the slab, with the shear plane dipping approximately parallel to the slab. In the interior of the wedge, however, textures are more dispersed without any clear distribution maxima. The resulting picture approaches, perhaps unsurprisingly, that of 2-D mantle wedge corner flow.

Textures at the wedge-side edge of the slab (Figure 6) are most clearly developed near the surface: The a axes show a strong maximum that is
nearly trench parallel, with a slight dip toward the slab, and the $b$ and $c$ axes are both exhibiting a girdle distribution. The reason for the upper part of the particle column being more strongly textured is that throughout the subduction process (i.e., the slab’s descent from the near surface to the “660”) it has been subjected to more deformation than the lower part of the mantle.

3.1.2. Single-Sided Subduction: The Subslab Mantle
[32] Figure 7 shows textures in the center of the subslab mantle. For the most part, there is no clear trench-parallel trend. Only toward the bottom of the column (above the 410 km discontinuity) do the $a$ axes exhibit a trench-parallel maximum. In the rest of the column, there is a great dispersion of olivine $a$ axes, but a maximum of weak $b$ axes in the in the $z$ direction. The textures indicate a combination of simple shear—with a horizontal, x-y shear plane—and compression.

[33] Textures at the seaward-side edge of the slab (Figure 8) also do not show a strong trench-parallel LPO. The $a$ axes have a maximum that is trench oblique, with a 90$^\circ$ rotation occurring from the top to the bottom of the column.

3.1.3. Double-Sided Subduction: The Subslab Mantle
[34] Textures developed during double-sided subduction, on the other hand, show very strong
trench-parallel $a$ axes maxima. Beneath the center of the plate (Figure 9), textures have a clear $a$ axes maximum parallel to the two trenches. The maximum of the $b$ axes is in the $x$ direction, i.e., perpendicular to the trench. Since we impose a model that is designed to generate A-type olivine LPO for simple shear, this means that the shear plane is the $y$-$z$ plane (i.e., the axial plane of the “anticlinal fold” of the plate). At the edge of the slab (Figure 11), textures are similar, albeit with less pronounced maxima.

Away from the “anticlinal fold plane” (Figure 10), trench-parallel $a$ axis maxima become more pronounced from the top of the column to the bottom, and there is a change from horizontal simple shear to pure shear and extension.

### 3.2. SKS Splitting

The resultant aggregate SKS splitting measurements (averaged over all backazimuths) are shown in Figure 12. The black bars are oriented in the fast direction ($\phi$). Their length is proportional to the delay time ($\delta t$). As previously mentioned, delay times are slightly higher than they would occur in nature due to the absence of enstatite and dynamic recrystallization in our models. However, of greater importance here are the relative differences in $\delta t$ between the different regions of mantle flow (e.g., between the wedge and the subslab mantle) and between the two subduction models.

In the mantle wedge, delay times are between 2.2 and 4.9 s. In the center of the slab, fast directions are trench perpendicular, which is in accordance with the calculated textures at that column (Figure 5). Toward the edge of the slab, however, there is a clockwise rotation in $\phi$ until, at the outermost column, $\phi$ is nearly trench parallel.

What is immediately noticeable are the stark differences in splitting measurements of the subslab mantle. In the single-sided model, time lags are markedly smaller (0.3–1.5 s) than in the double-sided model (2.2–4.9 s). Furthermore,
although there is a trench-parallel trend in $\phi$ in the single-sided case, it is much more pronounced in the double-sided case, as expected from the associated textures (Figures 7 and 9).

[39] In some regions of the model there is a strong variation of splitting parameters with backazimuth. For example, in the subslab mantle of the single-sided model, there is a 90° periodicity (supporting information Figure S2), which is indicative of two or more layers of anisotropy [Silver and Savage, 1994]. It is not surprising when looking at the change in texture throughout the column (Figure 7), from trench-perpendicular $a$ axis maxima at the top to trench-parallel $a$ axis maxima at the bottom. This is noteworthy. In real data, we rarely have complete backazimuthal coverage—be it due to an unfortunate arrangement of sources or paucity of high-magnitude earthquakes during temporary station deployments—and it may be that some of the global variation we see in subduction zone splitting results from a combination of imaging geometry and multilayer anisotropy. For example, in the case of the seaward-side station, for which textures are shown in Figure 7, trench-parallel or trench-perpendicular backazimuths would both result in perfectly trench-perpendicular fast directions (supporting information Figure S2). However, for a backazimuth of 60°, for example, the resulting fast direction would be approximately $-45^\circ$ and, therefore, trench oblique.

4. Discussion

[40] The modeling of history-dependent textures in an evolving subduction zone provides several important insights, and although the Molucca Sea is—to the best of our knowledge—currently the only locality of two-sided subduction, the comparison with subslab textures developed during double-sided subduction yields interesting implications.
4.1. Seismic Anisotropy in the Mantle Wedge

The calculated textures in the central part of the wedge (Figure 5) show strong horizontal axes maxima perpendicular to the trench in the upper 150 km of the mantle. Moving downward in the olivine aggregate column, one can observe a rotation of axes maxima toward a strong slab-dip-parallel maximum in the lower 100 km, just above the slab. In other words: shear is strongest in the upper 150 km of the mantle wedge and in the slab dip at the bottom. The simple shear component stems from divergent flow of the mantle escaping slab rollback horizontally, whereas the compression-extension component is due to the slab collapsing onto the mantle in the vertical direction.

That shearing is strong near the surface becomes clear when looking at the flow field (Figure 3c) and the pathlines for the midwedge in Figure 4. As the slab subducts, mantle material is only being drawn in horizontally. The material finishing closest to the slab, on the other hand, has been dragged down a significant distance. Nonetheless, the textures at the bottom of the column are parallel to the slab dip, not the traveled path. This is perhaps due to the fact that the immediate layer of mantle above the slab is dominated by progressive simple shear parallel to the slab, where shear stress and strain are extremely high and, thus, strong dip-parallel LPO can develop. Supraslab anisotropy due to progressive simple shear has been predicted by McKenzie [1979], Ribe [1989], and Kendall and Thomson [1993], observed in analogue models [e.g., Buttles and Olson, 1998] and, recently, in shear wave splitting data: Di Leo et al. [2012a] interpreted trench-perpendicular fast directions of local S splitting as being due to such shear layers of strong LPO atop the Molucca Sea slab in the Sangihe subduction zone.

A common observation in shear wave splitting studies of subduction zones is that the interior of the wedge appears to be largely isotropic [e.g., Polet et al., 2000; Morley et al., 2006; Piñero-Feliciangeli and Kendall, 2008; Hammond et al., 2010; Di Leo et al., 2012a]. Buttles and Olson

Figure 7. Textures in the center of the subslab mantle. Only toward the bottom of the column (above the “410”) do the axes exhibit a trench-parallel maximum. In the upper part of the column, there is a dispersion of olivine axes, but a maximum of b axes in the z direction. The textures indicate a combination of simple shear (with a horizontal, x-y shear plane) in the upper part of the column and a compressional/extensional regime at the bottom. The simple shear component stems from divergent flow of the mantle escaping slab rollback horizontally, whereas the compression-extension component is due to the slab collapsing onto the mantle in the vertical direction.
[1998] made similar observations in their analogue models; fast directions in the wedge interior were extremely variable, especially for steeply (>45°) dipping slabs. This is in good agreement with the textures we have calculated here (Figure 5): textures for the wedge interior (i.e., the middle of the column) show no strong preferred orientation. 

[44] Overall, the anisotropy could be interpreted as “2-D corner flow.” However, that term is misleading. “Corner flow” suggests a continuous, roughly triangular flow in the mantle wedge. Such a flow can be expected in an older subduction zone that has been stagnating at the bottom of the mantle transition zone for a prolonged period of time. What we calculate here are the early textures that develop as the slab subducts. A look at the pathways of mantle material (Figure 4) shows that the flow during the early stages of subduction is not perfectly triangular, but rather more complex. Furthermore, Figure 4 shows flow in the central mirror plane of the slab. Moving toward the edges of the slabs, flow becomes even more complex and trench oblique, as evidenced by the textures (Figure 6) and shear wave splitting results (Figure 12).

4.2. Slab Edge Effects

[45] Toroidal flow around slab edges (from the underlying and surrounding mantle toward the wedge) has been observed in the immediate vicinity of slab terminations in numerical models [e.g., Zhong et al., 1998; Piromallo et al., 2006; Stegman et al., 2006; Lowman et al., 2007; Faccenda and Capitanio, 2013] and analogue laboratory experiments [e.g., Kincaid and Olson, 1987; Buttes and Olson, 1998; Schellart, 2004] and has been inferred from shear wave splitting data [e.g., Civello and Margheriti, 2004; Currie et al., 2004; Di Leo et al., 2012b]. Such return flow around the slab’s edge is also evident in our models: in the flow field (Figure 3), in the textures (Figure 6), and in the fast directions (Figure 12). The toroidal flow develops very early in the subduction process, long before the slab reaches a lower boundary. Our modeling results suggest that, given the right source-receiver configuration, shear wave splitting can be employed as a tool for detecting toroidal flow.

4.3. Subslab Seismic Anisotropy

[46] We can describe the style of strain experienced by a polycrystal along its trajectory
graphically in a manner based on the “Flinn diagram” [Flinn, 1962]. This allows us to visualize the history of deformation that leads to the development of a particular texture and seismic anisotropy, and understand the importance of a changing flow field for our results. Figure 13 shows examples for subslab polycrystals of the single- and the double-sided subduction model. (See supporting information Figure S3 for a diagram of deformation in the wedge.) The horizontal axis is $x = (1 + \varepsilon_2)/(1 + \varepsilon_3)$ and the vertical axis $y = (1 + \varepsilon_1)/(1 + \varepsilon_2)$, where $\varepsilon_1$, $\varepsilon_2$, and $\varepsilon_3$ are the largest positive, intermediate, and minimum negative eigenvalues of the strain rate tensor $E$, respectively, and $\varepsilon_1 + \varepsilon_2 + \varepsilon_3 = 0$ by incompressibility. Points plotting on the line $x = y$ correspond to plane strain deformation; the vertical axis ($x = 0$) corresponds to uniaxial extension, and the horizontal axis ($y = 0$) to uniaxial compression. The points represent the 150 time steps and are color coded by the vorticity number, which is the absolute value of the vorticity vector normalized by the second invariant of the strain rate tensor. In plane strain ($x = y$), $= 0$ for pure shear, $= 1$ is consistent with simple shear, and $> 1$ signifies deformation in which vorticity dominates over shear.

[47] In the upper part of the subslab mantle (Figures 13a and 13b), the dominant type of deformation is simple shear. However, in the double-sided model, there is also a significant amount of compression. The middle of the column is where the single-sided and the double-sided model differ the most in their strain history. In the single-sided case, axial compression clearly dominates, whereas in the double-sided case, simple shear appears to be the primary type of deformation. At the bottom of the column of the single-sided model, deformation starts off with pure shear and compression and then transitions to extension. In the double-sided model, pure shear and extension are clearly the dominant type of strain.

[48] Several authors have proposed 3-D mantle flow models in subduction zones that involve trench-parallel flow beneath the slab [e.g., Russo and Silver, 1994; Piñero-Feliciangeli and Kendall, 2008; Long and Silver, 2008, 2009] to account for observations of trench-parallel fast
Figure 10. Textures in the subslab mantle (away from the "anticlinal fold plane"). From top to bottom, trench-parallel $a$ axis maxima become more pronounced, and there is a change from horizontal simple shear to pure shear extension.

Figure 11. Textures in the subslab mantle (slab edge) in the double-sided subduction model are similar to those beneath the slab center (Figure 9), but with less pronounced maxima.
directions. Two prerequisites for such a model are a barrier to flow behind the slab and parallel to the trench as well as a barrier to flow at depth. The latter is given by the 660 km discontinuity, which, although not yet fully understood, is believed to act as a semipermeable barrier [e.g., Tackley, 2008]. In the double-sided model, the second slab acts as a trench-parallel barrier. The only escape route for the mantle between the two slabs is, therefore, outward, parallel to the two trenches. This is evident from the flow field in our models (Figure 3f). The calculated textures support this assumption (Figures 9–11), showing well-developed olivine a axes maxima parallel to the trenches. This is in agreement with shear wave splitting observations by Di Leo et al. [2012a]. However, it is also clear from the textures and the modified “Flinn diagrams” that trench-parallel extension caused by axial compression and pure shear adds to the development of trench-parallel splitting fast directions as well. The textures are, therefore, not simply a result of trench-parallel simple-shear flow of the mantle being shoved out of the way by the subducting slab.

[49] What is significant, perhaps, is the development of subslab trench-parallel $\phi$ in the single-sided case. We demonstrate that this is achievable with the simplest of models—i.e., pure dry olivine deforming so as to generate an A-type LPO in progressive simple shear—due to the combination of simple-shear strain induced by trench-parallel flow in the upper part of the subslab mantle, but also compression leading to trench-parallel extension in the lower part. Furthermore, there is no need to invoke other mechanisms such as a pressure-induced transition in the olivine slip systems to B-type LPO [Couvy et al., 2004; Raterron et al., 2007; Carrez et al., 2008; Jung et al., 2009; Raterron et al., 2009; Walker et al., 2010]. Faccenda and Capitanio [2013] have recently pointed out the importance of pure shear and extension in the development of trench-parallel subslab seismic anisotropy. Our results further show that a barrier to flow behind the slab significantly amplifies trench-parallel subslab anisotropy, but it is not a prerequisite for it.
Figure 13. “Flinn-type” diagram (inspired by Flinn [1962]) to visualize the type of deformation a polycrystal undergoes in the subslab mantle during subduction. (left) single sided; (right) double sided; (a and b) topmost polycrystal; (c and d) middle; (e and f) bottommost polycrystal in the column. The $x = y$ line corresponds to plane strain, the horizontal axis ($y = 0$) to uniaxial compression, and the vertical axis ($x = 0$) to uniaxial extension. The points represent the time steps (starting point marked by black star) and are color-coded by the vorticity number. In plane strain ($x = y$), $= 0$ for pure shear, $= 1$ is consistent with simple shear, and $> 1$ signifies deformation in which vorticity dominates over shear. Note the difference in deformation patterns between single-sided and double-sided subduction.
5. Conclusions

We present an integrated model to simulate history-dependent upper mantle LPO development and resulting shear wave splitting. We compare results to observations from the double-sided Molucca Sea subduction system. Incorporating the entire strain history of the deformed mantle is essential, as LPO textures are a function of the magnitude of accumulated finite strain, but also the variation of flow velocity gradients along the path a volume of rock has traveled. The Molucca Sea subduction system offers an ideal case study for two reasons: (1) It is fairly young and the slab has not been stagnating at the bottom of the mantle transition zone for long. Thus, early textures from the slab’s descent, which we are able to simulate in our models, have not yet been overprinted by subsequent steady state flow. (2) It allows us to test the significance of the double-sided geometry, or, in more generic terms, the significance of a rear barrier to achieve trench-parallel subslab mantle flow.

Our results show that trench-parallel fast directions can be produced without such a barrier and that this is in large part due to extension through axial compression and pure shear deformation in the subslab mantle, and not exclusively due to trench-parallel mantle flow. However, in the double-sided subduction model, trench-parallel anisotropy is significantly stronger and in no small part due to the mantle flowing outward and escaping the sinking microplate, as surmised by Di Leo et al. [2012a] in their shear wave splitting study of the Sangihe subduction zone.

The results presented here are in good agreement with most models and shear wave splitting observations of trench-perpendicular mantle wedge flow, with a horizontal flow toward the trench, supraslab shear layers of strong LPO, and an effectively isotropic mantle wedge interior. At the edge of the slab, toroidal return flow from the subslab region toward the mantle wedge accommodates subduction from an early stage onward.

Our study shows that measurements of shear wave splitting under the assumption of deformation dominated by the motion of dislocations belonging to the (010)[100] slip system may be used to study flow in the upper mantle, even in such complex settings as subduction zones, but several deformation mechanisms contribute in varying amounts, and caution is required. Additional modeling of strain-history-dependent texture development can improve our understanding of the upper mantle as it responds to subduction.

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References

Couvy, H., D. J. Frost, F. Heidelbach, K. Nyilas, T. Ungár, S. Mackwell, and P. Cordier (2004), Shear deformation


Lebensohn, R. A., and C. N. Tomé (1993), A self-consistent anisotropic approach for the simulation of plastic deformation and texture development of polycrystals: Application to


