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Detecting seismic anisotropy above the 410 km discontinuity using reflection coefficients of underside reflections

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Abstract

We investigate the effect of various types of deformation mechanisms on the reflection coefficients of P and S waves underside reflections off the 410 km discontinuity, to develop a diagnostic tool to detect the style of deformation at boundary layers. We calculate the reflection coefficient for P and SH underside reflections using velocity perturbations resulting from aligned minerals above the 410 km discontinuity for different deformation scenarios. The results show that in the case of an anisotropic olivine layer above an isotropic wadsleyite layer, the P wave reflection coefficient amplitudes are only slightly influenced by the joint effect of angle of incidence and the strength of imposed deformation, without any polarity reversal and for all deformation styles. For the SH wave underside reflections the incidence angle for which a polarity reversal occurs, changes with distance for all scenarios and in addition changes with azimuth for shear deformation scenarios. These differences in amplitude and polarity patterns of reflection coefficients of different deformation geometries, especially for S wave at shorter distances potentially provide a possibility to distinguish between different styles of deformation at a boundary layer. We also show a first test using currently available elastic constants of anisotropic wadsleyite beneath anisotropic olivine.

Keywords

410 km seismic discontinuity, Underside reflections, Reflection coefficient, Deformation style, Anisotropy

1. Introduction

Seismic anisotropy, the intrinsic property of elastic materials that produces the directional dependence of seismic wave speed and polarization has been observed in many regions of the Earth's interior. A wide range of seismic studies inferred the anisotropic structure of the Earth
for example near the surface (e.g., Crampin, 1994) and in the lower crust (e.g., Savage, 1999) and seismic anisotropy in the upper mantle is now well established by SKS splitting and surface waves (e.g., see Yu et al., 1995; Silver, 1996; Montagner, 1998; Savage, 1999; Kendall, 2000; Gaherty, 2004; Long and van der Hilst, 2005; Long, 2009; Eakin et al., 2015). To a lesser extent anisotropy is detected in the lowermost mantle and the D" layer (e.g., Kendall and Silver, 1998; Lay et al., 1998; Ritsema, 2000; Thomas and Kendall, 2002; Nowacki et al., 2010) and in the inner core (e.g., Song, 1996; Morelli et al., 1986; Niu and Chen, 2008; Deuss, 2014).

Seismic anisotropy at mid-mantle depths is not well understood. Indeed, some studies report evidences for little to no anisotropy (e.g., Kaneshima and Silver, 1992; Fischer and Wiens, 1996), while others show the presence of anisotropy on a global scale (e.g., Trampert and van Heijst, 2002; Panning and Romanowicz, 2006) or in the top ~200-250 km of the mantle (e.g., Montagner and Kennett, 1996; Debayle et al., 2005; Yuan and Romanowicz, 2010). In addition, some studies indicate the presence of anisotropy in the mantle transition zone (MTZ) between 410 and 660 km depth (Fouch and Fischer, 1996; Montagner and Kennett, 1996; Beghein and Trampert, 2003; Beghein et al., 2006; Panning and Romanowicz, 2006; Visser et al., 2008; Yuan and Beghein, 2013) as well as below the 660 km discontinuity both regionally (e.g., Tong et al., 1994; Wookey et al., 2002; Chen and Brudzinski, 2003; Wookey and Kendall, 2004) and globally (e.g., Montagner and Kennett, 1996; Trampert and van Heijst, 2002). A mechanism to produce seismic anisotropy is deformation due to mantle flow (see Kendall, 2000 for a review). In this paper, we focus on anisotropy in the upper part of the mantle transition zone and test a method that could potentially be used to detect seismic anisotropy independently of surface waves and shear wave splitting.

The seismic discontinuity at 410 km depth is attributed to a pressure-induced phase transformation of olivine to wadsleyite (e.g., Helffrich and Wood, 1996; Akaogi et al., 1989;
Katsura and Ito, 1989; Katsura et al., 2004). Olivine is volumetrically the most important mineral in the upper mantle. Moreover, olivine-single crystals display a large shear wave anisotropy of up to ~18% (e.g., Mainprice, 2007). Alignment of olivine anisotropic crystals is thus interpreted as the primary source for upper mantle anisotropy (e.g., Kumazawa and Anderson, 1969; Chastel et al., 1993; Abramson et al., 1997; Tommasi, 1998; Stein and Wyssession, 2003). Wadsleyite is the high pressure-temperature polymorph of olivine and the primary mantle transition zone mineral constituent between 410 and 520 km depth. Ambient temperature calculations and measurements show that it exhibits a strong intrinsic elastic anisotropy (~10-14% for shear and compressional waves at 410 km depth pressures, e.g., Zha et al., 1997; Mainprice et al., 2000). This anisotropy is stronger than that of ringwoodite and majorite-garnet but weaker than that of olivine (e.g., Pacalo and Weidner, 1997; Sinogeikin et al., 1998; Mainprice et al., 2000).

The presence of anisotropic minerals in the medium does not necessarily produce seismic anisotropy. As suggested by Montagner (1998), four conditions are required in order to detect large-scale mantle LPO (Lattice Preferred Orientation) seismic anisotropy: a) presence of intrinsic anisotropic materials, b) efficient mechanisms of crystals orientation, c) anisotropy of an assemblage of minerals which is usually less than the anisotropy of the pure mineral and d) coherent strain field due to effective deformation field. Anisotropic minerals in the presence of plastic deformation related to mantle flows can potentially develop a Crystallographic Preferred Orientation (CPO) (Karato and Wu, 1993) that gives rise to seismic anisotropy. Due to the direct link between the CPO of mantle minerals and mantle deformation, the study of seismic anisotropy can be used as a marker for the style of mantle flow in different tectonic regions which provides valuable information for our understanding of dynamic processes at depth (e.g., Nicolas and Christensen, 1987; Mainprice and Silver, 1993; Karato et al., 2008; Long and Silver, 2009). However, the interpretation of the MTZ...
seismic anisotropy in terms of flow geometry is not yet clear, due to little information provided on the CPO of minerals under mantle transition zone pressure and temperature conditions. Furthermore, the interpretation of seismic anisotropy in terms of deformation mechanisms becomes more complicated with the effect of water content of the rocks, deviatoric stress, strain, pressure and temperature on the directional characteristics of anisotropic minerals (e.g., Zhang and Karato, 1995; Bystricky et al., 2000; Zhang et al., 2000; Jung and Karato, 2001a; Durinck et al., 2005; Mainprice et al., 2005; Jung et al., 2006; Katayama and Karato, 2006; Warren and Hirth, 2006; Raterron et al., 2007; Jung et al., 2009; Skemer et al., 2010; Demouchy et al., 2011; Kawazoe et al., 2013; Ohuchi et al., 2014; Raterron et al., 2014).

In addition to the constraints provided by experimental mineral physics, seismological observations and geodynamical modelling, insight into the nature of anisotropic structures in the mantle can be gained by measuring and modelling of reflection coefficients from waves reflected at seismic interfaces (e.g., Thomas et al., 2011). In this study, we extend the method used by Thomas et al. (2011) to establish whether it allows us to detect anisotropy at the 410 km discontinuity. We test whether this approach applied to P and S waves that reflect off the underside of 410 km discontinuity (\(P_{410}P\) and \(S_{410}S\)) potentially provides information on the elastic wave speeds and deformation geometry of the olivine and wadsleyite aggregates deformed by a strain field. Our intent is not to fully cover all the aspects of seismic anisotropy in the mantle transition zone, but rather to provide and test a method that relates PP and SS underside reflections to the style of deformation occurring at the MTZ depths.

2. Methodology

The amplitude and polarity of reflected seismic waves at a given interface are dependent on the impedance (product of velocity and density) contrast between of the two media above and
below the interface. A numerical measure of the amplitude and polarity of a reflected wave is
given by reflection coefficient and can be computed using Zoeppritz’s equations (Zoeppritz, 1919). In the case of isotropic materials the velocities and density do not vary with direction
and, as a consequence, the reflection coefficient of the reflected wave does not change as a
function of azimuth.

The alignment of anisotropic crystals however, may influence the observed velocities such
that the reflection coefficients will vary with azimuth, depending on fast and slow axes of
aligned polycrystals. For reflections from the top of the D' layer, Thomas et al. (2011) showed that the azimuthal variations of P and S reflection coefficients can be used as a
marker of mineral alignment and the anisotropy above and below the interface.

We compute the reflection coefficients of P and S wave underside reflections using the
crystal preferred alignment predictions of olivine produced for different deformation
geometries above the 410 km discontinuity. We combine the deformed olivine with non-
deformed, isotropic wadsleyite to test whether the reflection coefficient pattern for underside
reflections can be used as a diagnostic tool for determining the deformation mechanism
occurring at mantle transition zone boundaries (Figure 1). This is the first step, intended to
show the validity of the approach but it has to be extended to other cases in the future.

2.1. Elastic constants of single-crystal olivine at high pressure and temperature

The olivine to wadsleyite phase transformation in the average Earth's mantle occurs at
pressures around 13.8 GPa (e.g., Bina and Helffrich, 1994) and a temperature of 1760±45 K
(e.g., Katsura et al., 2004). The detailed knowledge of the single-crystal elasticity of major
mantle minerals such as olivine at relevant pressure-temperature (P-T) conditions is required
in order to interpret the observed seismic properties (see Mainprice, 2000 for a review) and
especially seismic anisotropy. The elastic moduli of olivine have been investigated at mantle
pressures by methods such as impulsive simulated scattering (Abramson et al., 1997), Brillouin scattering (Zha et al., 1996, 1998; Mao et al., 2015; Zhang and Bass, 2016) ultrasonic interferometry (Chen et al., 1996; Liu et al., 2005), and first-principles calculations (e.g., Núñez-Valdez et al., 2013). But, due to experimental and computational difficulties, the full elastic tensor of single-crystal olivine has, to our knowledge, not been provided at simultaneous P and T conditions of the 410 km discontinuity. Mao et al. (2015) used in-situ Brillouin spectroscopy and single crystal X-ray diffraction in externally-heated diamond anvil cells and, reported the elasticity of single-crystal olivine up to 20 GPa and 900 K, which was completed by the study of Zhang and Bass (2016) up to 13 GPa and 1300 K.

In order to obtain the elastic moduli of olivine at P-T conditions relevant to 410 km depth, we compute the P-T derivatives of the elastic constants of olivine by fitting polynomial functions to the experimentally derived elastic moduli reported by Mao et al. (2015). The fitted polynomial functions are characterized by the first order derivative in temperature and second order derivative in pressure. The choice of such polynomials is based on a study by Isaak (1992) which shows that under high-pressure conditions, despite having two different slopes of elastic moduli of olivine versus temperature below and above 800 K, the temperature dependence of $C_{ij}$ can be described by a linear expression. We then extrapolate the polynomial to the relevant pressure of 13.3 GPa and temperature of 1750 K. The obtained values for elastic constants of olivine are listed in Table 1. These values have been used as the olivine single-crystal elastic constants to calculate the polycrystalline elastic properties of olivine and for further calculations of P and S wave reflection coefficients.

It should be noted that the experimental measurements uncertainties of elastic moduli given by Mao et al. (2015) are not taken into account for calculation of P-T derivatives. However, to investigate the possible effect of different elastic moduli values of olivine on the reflection coefficients of P and S waves, a second order polynomial for both pressure and temperature
derivatives was also tested. These elastic moduli differ by up to 25 GPa from those of Table 1. Nevertheless, reflection coefficients obtained for P and S waves using this set of elastic constants exhibit a negligible difference compared to those produced from the first set of elastic moduli of olivine and we therefore focus on the results associated with the first class of elastic constants.

2.2. Elastic constants of single-crystal wadsleyite at high pressure and temperature

A number of studies have been carried out to determine the polycrystalline elastic properties of wadsleyite under different pressure and temperature conditions (Li et al., 1998; Li et al., 2001; Mayama et al., 2004; Isaak et al., 2007; Liu et al., 2009; Kawazoe et al., 2013; Núñez-Valdez et al., 2013). However, the single-crystal elasticity of wadsleyite was only evaluated at ambient conditions (Sawamoto et al., 1984; Sinogeikin et al., 1998) and pressures up to 14 GPa at ambient temperature (Gwanmesia et al., 1990; Zha et al., 1997; Wang et al., 2014). Temperature effects on the single crystal elastic moduli of wadsleyite are unknown. Hence, due the lack of published single-crystal elastic properties of wadsleyite at high temperature, we decided to concentrate our analysis on isotropic properties for which the values of bulk and shear moduli are sufficient. We use the adiabatic aggregate bulk (\(K_a\)) and shear (\(G\)) moduli and their pressure derivatives reported by Wang et al. (2014) for an anhydrous iron-bearing wadsleyite with \([\text{Fe}]/([\text{Fe}+\text{Mg}]\) molar ratio of 0.075, and the temperature derivatives of Mayama et al. (2004). We then derive effective elastic properties for an isotropic aggregate of wadsleyite at the conditions of 410 km depth (Table 1). Finally, note that the elastic parameters we obtain differ from those proposed by Liu et al. (2009) by up to 20 GPa, which is the best resolution one can hope for at present.

2.3. Deformations style
With imposed deformation, crystallites in the polycrystal will orient and generate Lattice Preferred Orientations (LPO), also known as texture. LPO evolution is essentially controlled by the macroscopic deformation, the initial texture, and the active plastic deformation mechanisms (Mainprice et al., 2005).

As mentioned above, we concentrate on cases with anisotropy in the olivine stability field, above 410 km, and isotropy in the wadsleyite stability field, below 410 km. According to experimental data, the olivine to wadsleyite transformation may not preserve LPO across the 410-km discontinuity (e.g., Smyth et al., 2012; Rosa et al., 2016). Indeed, although wadsleyite can nucleate at intracrystalline sites in olivine with well-defined orientation relationships, the lamellae act as nucleation sites for faster-growing incoherent wadsleyite grains with no orientation memory of the parent olivine grains (e.g., Rosa et al., 2016). Thus, in regions of downwelling, assuming LPO in olivine above the 410 km discontinuity and random texture (i.e. isotropy) below the 410 km discontinuity is a proper first-order approximation.

We test two different classes of deformation geometries. First, we test the effect of axial compression applied to the olivine polycrystals above the 410 km discontinuity and the second class includes deformation in shear for both cases where the shear direction is horizontal (parallel to the discontinuity) or vertical (perpendicular to the discontinuity). In each case we assume an isotropic starting texture and let the LPO evolve with the imposed deformation.

2.4. Calculation of olivine LPO

Polycrystal LPO are simulated using polycrystal plasticity simulations utilizing the second-order self-consistent model, initially proposed by Ponte Castañeda (2002) and extended by Detrez et al. (2015). This mean-field micromechanical model accounts for the slip systems at
the grain level and an isotropic relaxation mechanism. Olivine is lacking four independent
slip systems at the grain level, which is necessary to accommodate any arbitrary plastic
deformation in the aggregate. Hence, an additional relaxation mechanism is required but the
microscopic origin of this additional relaxation mechanism is not known at this time although
it could relate to mechanisms such as grain boundary sliding (e.g., Ohuchi et al., 2015) or
disclinations (Cordier et al., 2014). The isotropic mechanism allows removing the fictitious
<110>{111} slip system used in previous computations (e.g., Tommasi, 1998; Castelnau et
al., 2008). Simulations are performed for a 1000 grains random starting aggregate. In
compression, calculations are performed in steps of 1.25% axial strain up to a final strain of
100%. Polycrystal LPO’s are saved at the start of the simulation, 25%, 50%, 75%, and 100%
axial strain (Figure 2). Shear simulations are run in steps of 2.5% shear, up to a final shear
strain of $\gamma = 4$ (400%). Textures are saved at the start of the simulation, and at $\gamma = 1, 2, 3, 4$.

The dominant plastic deformation mechanism of olivine tends to change with the effect of
water content, deviatoric stress, pressure and temperature (e.g., Mainprice et al., 2005; Jung
et al., 2006; Raterron et al., 2014). Here, we hence design two plastic models for olivine at
the conditions of 410 km. The first model is that of Raterron et al. (2014), at the conditions of
405 km, with dominant slip along [001](010) (Table 2). In shear this model leads to B-type
textures according to the classification of Jung et al. (2006). The second model is that of
Tommasi (1998) with dominant slip on [100](010) (Table 2). In shear this model leads to A-
type textures. While the second model is typical for olivine deformed under low stress, low
pressure, and low water content conditions the model from Raterron et al. (2014) is
appropriate for how we believe olivine behaves deeper in a dry mantle.

A number of studies suggest a different plastic behaviour between hydrous and anhydrous
olivine (e.g. Jung et al, 2006, Ohuchi et al, 2017). Ohuchi et al (2017), for instance, showed
that hydrous olivine is much weaker than dry olivine and that a significant portion of the
strain could be accommodated by dislocation accommodated grain boundary sliding, in conjunction with dominant [100] slip or on the [001](100) slip system. Simulations with dominant [001](100) slip system will result in other elastic constants than the two models above. Investigating this, however, goes beyond the goal of this paper and will require further future investigations.

3. Reflection coefficient modelling across the 410 km discontinuity

For a given deformation style, we calculate the polycrystalline elastic tensor of olivine in the Hill average (Hill, 1952) using the modeled texture and the single crystal elastic moduli of Table 1. Since we use an isotropic model for wadsleyite, the polycrystal elastic tensor is the same as that of the single-crystal. Densities for each phase are taken from the study of Inoue et al. (2004) and are listed in Table 1.

We compute the reflection coefficient of the P and S waves reflected at the underside of the 410 km discontinuity using the anisotropic raytracer ATRAK (Guest and Kendall, 1993) and the matlab toolkit MSAT (Walker and Wookey, 2012). The output of this tool is the velocity perturbations and the reflection coefficients across the discontinuity as a function of azimuth. Reflection coefficients of P and S waves depend strongly on the angle of incidence, i.e., on distance (Zoeppritz, 1919) and should therefore be computed for a range of incidence angles and as a function of azimuth. For each macroscopic deformation style and each olivine plastic model, we start the simulations with a random orientation for both olivine and wadsleyite crystals, and we then increase the alignment of the olivine grains with deformation.

The reflection coefficients for isotropic olivine and wadsleyite are given in Figure 2.e (white circles) as starting texture and the results indicate that the P-wave reflection coefficient is negative for all incidence angles while the SH reflection coefficient is positive for incidence angles smaller than 53 degrees (epicentral distances larger than approx. 39 degrees) and
negative for larger incidence angles (epicentral distances smaller than approx. 39 degrees). In the following we focus especially on the results of the reflection coefficients modelling of P and S waves for the cases of axial compression, horizontal shear, and vertical shear and compare the deformed (anisotropic) cases to this isotropic reference case.

4. Results

4.1. Vertical compression

The texture of CPO of olivine induced by the vertical compression is symmetric around the axis of applied deformation (see Figure 2.c). The calculation of P and SH wave reflection coefficients for the axial compression deformation hence leads to reflection coefficients that do not depend on azimuth (Figure 2.d). This is due to the symmetry of the deformation, which induces a symmetry on the polycrystalline texture and a hexagonal symmetry in the polycrystalline elastic tensor, whatever the plastic model used for olivine.

We observe an overall constant negative reflection coefficient for P underside reflections with small amplitude variations depending on the applied deformation intensity for the two plastic models used for olivine and therefore similar to the isotropic reference case. Precursors would therefore have the same polarity as PP waves reflected off the surface. For SH underside reflections the level of applied deformation changes the incidence angle at which the polarity reversal occurs, and generally moves the polarity reversal for the reflection coefficient to larger incidence angles and therefore even shorter epicentral distances (Figure 2.e).

4.2. Horizontal shear deformation

In a second step we investigate shear deformation in the form of horizontal and vertical shear. Figure 3 shows the textures associated with this deformation for two plastic models of olivine
based on Tommasi (1998) and Raterron et al. (2014) at 405 km depth, as explained before. While the textures for compression deformation exhibit similar strength for both models (Figure 4), in the case of shear deformation textures resulting from the plastic model of Tommasi (1998) are much stronger than those obtained with the model of Raterron et al. (2014) at 405 km (Figure 3). In both cases, the (010) planes align with the plane of shear. For the model of Tommasi (1998), the [100] directions align sub-parallel to the shear direction whereas for the model of Raterron et al. (2014) at 405 km, the [001] directions align sub-parallel to the shear direction.

The results of reflection coefficient modelling for the case of horizontal shear using the B-type slip system (Raterron et al., 2014, 405 km) are described in Figure 5. As before, we vary the incidence angles from 15° to 65° (Figure 5) and calculate reflection coefficients for varying azimuths. Since variations of the reflection coefficients of P and SH underside reflections with azimuth are visible (Figure 5.a), we display the reflection coefficients for three different directions: parallel to the direction of deformation (angle of 0 degrees), with an angle of 45 degrees to the direction of deformation and perpendicular to the deformation direction (90 degrees).

Our results for the horizontal shear deformation again show negative P-wave reflection coefficients for the whole range of incidence angles with only slight variations with azimuth for different shear deformation. For the SH wave reflection coefficients we find a more pronounced behaviour: the variations of velocities due to applied deformation leads to a larger variation of the reflection coefficients of the SH wave with azimuth. Compared to the undeformed case we find reduced values in the direction of shear (azimuth of 0 degrees) and elevated values in the azimuth of 45 degrees and to a lesser extent at 90 degrees i.e., perpendicular to shear (Figure 5.a). This anisotropy leads to a change of amplitudes with propagation directions and hence influences the distance at which a polarity reversal occurs.
for waves reflecting at the same point but in different propagation azimuths (Figure 5.b-d) which is not observed for the compression deformation style. This variation of azimuthally dependent reflection coefficient offers a possibility to test the presence of anisotropy using reflection coefficients of the reflected S waves from the underside of a boundary layer.

Since the polarity change of the SH wave occurs at incidence angles between approximately 40 to 60 degrees (Figure 5), we focus on this distance range to investigate the reflection coefficient of SH waves for two different shear deformations and the two deformation models from the studies of T-98 (Tommasi, 1998) and R-14 (Raterron et al., 2014). Figure 6 shows the results: the reference case (white circles) with the change from positive to negative values for all cases at 39 degrees epicentral distance is given as comparison. For the vertical shear and for both models T-98 and R-14 the polarity reversal distances moves to smaller epicentral distances (larger angles of incidence) while still displaying directional variations. The extreme case is seen for vertical shear and the plastic olivine model T-98, for which the SH reflection coefficient remains positive over the whole range of 40 to 60 degrees 45 degrees away from the shear plane. For horizontal shear and the plastic model R-14, the polarity reversal happens at shorter epicentral distances than the isotropic case 45 degrees away from the shear direction while it does not significantly change in the other orientations. With the plastic model T-98, the polarity reversal is predicted at larger epicentral distance (smaller incidence angles) after shear deformation, which is the opposite of what is predicted for vertical shear. However, keeping in mind that SS underside reflections are usually studied at epicentral distance ranges of over 100 degrees (incidence angle of ~ 42 degrees) (e.g., Chambers et al., 2005; Schmerr and Garnero, 2006; Deuss, 2009; Zheng and Romanowicz, 2012; Saki et al., 2015), the effects that one would measure at these distances would result in amplitude changes with direction only.

5. Discussion
Flow in the mantle, through upwelling plumes and downgoing slabs, deforms mantle minerals and can lead to anisotropic behaviour (e.g., McNamara et al., 2003; Nippress et al., 2004). Detecting and discriminating between different deformation styles may help to distinguish between different styles of subduction and may help to discriminate between slabs stagnating in the mantle transition zone and those that descend into lower mantle (e.g., van der Hilst et al., 1991; Fukao et al., 1992; Fukao and Obayashi, 2013; French and Romanowicz, 2015). Surface wave analysis (e.g., Kawasaki and Kon'no, 1984; Montagner, 1998; Maupin and Park, 2007) and splitting measurements (e.g., Silver and Chan, 1991; Long and van der Hilst, 2005) have been employed to test anisotropy in the upper mantle but here we test another independent method of using body waves that reflect at a boundary layer and use directional variation of reflection coefficients to discriminate between different styles of deformation. Especially at boundary layers, where for example a mineral phase transition is generating reflected waves, this method can potentially provide useful information on anisotropy and deformation.

We test our method on the case of underside reflections generated at the 410 km discontinuity, where the phase transition from olivine to wadsleyite occurs. In the layer above the discontinuity we use deformed olivine. Investigating anisotropy in the mantle transition zone, however, has to be carried out with detailed knowledge of the evolution of the LPO of polycrystalline olivine with increasing pressure and temperature simultaneously with the available elastic moduli of single crystal olivine (Mainprice et al., 2000; Mainprice, 2007). The LPO, slip systems, and plastic mechanisms of olivine, are difficult to study at deep mantle pressures and remain a matter of current debates (e.g., Jung and Karato, 2001a; Couvy et al., 2004; Katayama et al., 2004; Faul et al., 2011; Ohuchi et al., 2011; Hilairet et al., 2012; Ohuchi et al., 2015; Bollinger et al., 2016). The choice of a dominant slip system may hence change in future works and influence the results of the reflection coefficient modelling in our
study. Here, this effect has been investigated by testing two different plastic models of olivine, as suggested by Tommasi (1998) and Raterron et al. (2014).

To test the feasibility of our method and for the simplest model, we have assumed wadsleyite to be isotropic. Some studies have discussed CPO of deformed wadsleyite (e.g., Demouchy et al., 2011; Kawazoe et al., 2013) and the nature of its dominating plastic mode (e.g., Thurel et al., 2003b; Ritterbex et al., 2016) that may contribute to transition zone anisotropy (Mohiuddin et al., 2015) and early experiments showed that wadsleyite may form a lattice preferred orientation (e.g., Thurel et al., 2003a; Tommasi et al., 2004). From a microscopic point of view, phase transformations can occur through two families of mechanisms, leading to coherent or incoherent orientations between the parent and daughter phases. Smyth et al. (2012) suggested that wadsleyite CPO can be partially inherited from pre-transformation olivine textures. Dissimilar to coherent orientation of the parent and daughter, loss of anisotropy through transformation is also discussed previously (e.g., Campbell, 2008), but since the elastic constants of wadsleyite at temperature and pressure corresponding to 410 km depth are currently not available for high shear strain, this type of transformation is difficult to test in our study. The only published values to our knowledge are by Kawazoe et al., (2013) with a shear strain of $\gamma = 0.4$.

Assuming wadsleyite to be anisotropic would offer the case of having two anisotropic layers one above and one below the 410 km discontinuity, but it would present a much more complicated first model. To make significant changes to the reflection coefficient, the alignment of wadsleyite would have to combine with the alignment of olivine to generate a reduction in velocity for one direction, which would result in a polarity change for all distances in this azimuthal direction.
Although the elastic constants of wadsleyite at pressure and temperature conditions of the 410 km depth and at high shear strain are not available, we conduct a first test here and use values provided in the literature (Kawazoe et al., 2013). They provide a table with a set of polycrystalline elastic moduli for plastically deformed wadsleyite at 17.6 GPa, 1800 K, and gamma = 0.4. Note, however, that these elastic moduli were not measured at 17.6 GPa and 1800 K. This set of elastic moduli was calculated based on the textures measured after deformation at 17.6 GPa and 1800 K and the single-crystal elastic constants measured by Zha et al (1997) at 14.2 GPa and room temperature. The effect of temperature on elasticity is, hence, not accounted for, possibly leading to a strong over-estimate of all elastic moduli and in particular for C11, C22, and C33. However, in the absence of other results on anisotropic wadsleyite at pressures and temperature of the 410 km discontinuity, we test this case to show the effect it has in our models. The results of the reflection coefficient modelling using this set of elastic constants are shown in Figure 7.

We find that the changes in the S-wave reflection coefficient are similar to the ones for isotropic wadsleyite but the place where the polarity reversal happens occurs at longer epicentral distances. The P-wave polarity, however, changes sign for this case, which perhaps could be due to the larger elastic moduli C11, C22 and C33. More test with anisotropic wadsleyite to understand the effects on P-wave reflectivity will be necessary in the future, when more data on anisotropic wadsleyite become available.

For the simplest setup model including isotropic wadsleyite, we chose the case of anhydrous iron-bearing wadsleyite in our study. Due to the high water storage capacity of wadsleyite up to 0.9%, water can be contained at 15 GPa and 1400°C (Demouchy et al., 2005), and it should be regarded as a parameter which may influence the elastic properties of wadsleyite. The effect of hydration on the elastic constants of wadsleyite is reported at ambient and high pressure conditions (e.g., Mao et al., 2008a, b). However, the existence of a significant water
reservoir in the mantle is still a matter of debate. In addition, the presence of a considerable
amount of iron in all upper mantle minerals has been shown (Agee, 1998) and large number
of studies have discussed the effect of Fe on the elasticity of olivine and wadsleyite (e.g.,
Duffy et al., 1995; Zha et al., 1996; Núñez-Valdez et al., 2011). For future work, cases with
hydrous wadsleyite and varying amounts of iron would be useful.

Results from our reflection coefficients modelling for P and SH waves at the underside of the
interface between anisotropic olivine and isotropic wadsleyite exhibit different pattern,
depending on the applied deformation geometry on olivine. Our modelling shows that
different deformation geometries do not create large amplitude variations for P wave
reflections. The reflection coefficient of underside reflections of P wave always exhibits
negative polarities without any polarity reversal for all tested deformation geometries.
However, the assumption of inheriting anisotropy through olivine-wadsleyite phase transition
for a horizontal shear deformation would likely change the results. In Figure 7, we do observe
polarity reversal of the P wave reflection coefficients at epicentral distances around 75
degrees but more work is needed to constrain this effect with elastic constants of anisotropic
wadsleyite measured at conditions of the mantle transition zone. Some polarity changes of PP
underside reflections have been observed in previous studies (e.g., Courtier and Revenaugh,
2007; Jasbinsek and Dueker, 2007; Thomas and Billen, 2009; Schmerr and Thomas, 2011)
and previous suggestions for these polarity reversals include melt or metastable olivine
wedges, but no conclusive interpretation has been given so far. Results from our modelling
suggest that anisotropy in the olivine layer in combination with isotropic wadsleyite is likely
not the cause for the observed polarity changes in PP precursors, however, more complicated
models with anisotropic wadsleyite could potentially explain the polarity reversal of PP
waves.
The results of reflection coefficient modelling for SH wave show variations of the epicentral distance, where the sign of the reflection coefficients of SH underside reflections at the 410 km discontinuity occurs. This effect is independent of having isotropic or anisotropic wadsleyite below the 410 km boundary. However, the case of deformed wadsleyite with shear strain of 0.4 shifts the epicentral distances range of polarity reversal to larger values (Figure 7). For the compressional geometry we find that the polarity reversal for the reflection coefficients of the SH wave changes with the percentage of applied compression but not with direction. For both horizontal and vertical shear deformations, however, the azimuth to the direction of imposed deformation plays an important role for the distance where the polarity of the reflected S wave changes sign, independent of the choice of the olivine dominant slip system (Figure 6). This provides a distinct difference between compression and shear deformation geometry and can act as discriminating factor for the detection of the style of deformation system at a boundary layer.

Testing the results of our study with seismological data would provide direct information on deformation for different regions in the Earth, specifically at boundary layers. Modelling results for waves reflected at the D" layer (Thomas et al., 2011) showed that P and S waves varied strongly in amplitude and also polarity and a combination of both P and S waves is necessary to distinguish between different scenarios. In our study, the combination of anisotropic olivine and wadsleyite produces considerable effect on the behavior of the reflection coefficients of the P waves. While for the case of undeformed wadsleyite the P wave reflection coefficients show only small amplitude variations, anisotropic wadsleyite leads to a polarity reversal of the reflection coefficients at epicentral distances of about 70 degrees. The S wave reflection coefficients change amplitude and the distance at which a polarity reversal occurs for both cases of deformed and undeformed wadsleyite but at larger epicentral distances for the deformed wadsleyite case. Also different deformation styles shift
the place, where polarity reversals of the reflection coefficient in SS waves occur, to shorter
epicentral distances than the isotropic case except for the case of the T-98 model and
horizontal shear where the polarity reversal occurs between 53 and 44 degrees epicentral
distance.

PP and SS underside reflections are generally studied in a distance range over 80 degrees
(e.g., Shearer, 2000; Deuss, 2009; Saki et al., 2015). Here we would need SS underside
reflections in a distance range of 30 to 40 degrees. While these reflections are in principle
possible, the wavefield exhibits triplications in this distance range, making the use of SS
underside reflections more difficult. In addition, the reflection coefficient is very small in the
vicinity of the polarity reversal and the waves would be difficult to observe in real data.

When using a deformed wadsleyite layer below an anisotropic olivine layer shifts the
epicentral distance of polarity change range to higher values (~ 50-65 degrees) even for a
small shear strain of 0.4 for wadsleyite. Considering deformed wadsleyite with high shear
strains may therefore improve our results in terms of the epicentral distance range where the
polarity reversal occur. While 65 degrees is still a low distance range for observing SS
underside reflections, we show that it is in principle possible to detect S wave underside
reflections off the 410 km boundary at epicentral distance between 50 to 60 degrees (Figure
8). The vespagram (e.g., Rost and Thomas, 2002) generated from synthetic seismograms
shows a clear S410S (including its depth phase) while the S660S precursor is partly
interfering with the S coda.

Even with the current limitations of the setup of our modelling, this study shows the
possibility of using the azimuthal dependence of reflection coefficients of the SH underside
reflections to study the deformation at the mantle transition zone boundaries. Our results,
however, motivate further research of reflection coefficient modelling including an
anisotropic wadsleyite layer with higher shear strain, effects of water and also extending the
modelling to the discontinuity at 660 km depth. While PP underside reflections off the 660 km discontinuity are less well observed (e.g., Estabrook and Kind, 1996; Deuss, 2009; Thomas and Billen, 2009; Schmerr and Thomas, 2011; Lessing et al., 2014; Saki et al., 2015), SH underside reflections of the 660 km discontinuity are generally visible (e.g., Flanagan and Shearer, 1998; Schmerr and Garnero, 2006; Gu et al., 2012) and our modelling so far suggests that the SH underside reflections are mostly affected by the deformation. Comparison of the calculated reflection coefficients with suitable seismic data would provide further insight into the mantle transition zone mineralogy and deformation and the mechanisms responsible for waveform changes of underside reflections.

6. Conclusions
To study possible processes that may affect the polarity and amplitude variation of the underside reflections off the 410 km discontinuity, we model the reflection coefficients of P and SH waves reflected off an olivine-wadsleyite phase transition. We tested different deformation geometries including axial compression perpendicular to the boundary and shear deformatons. For each, we calculate the reflection coefficients for incidence angles ranging from 15 to 65 degrees and all azimuths. The results indicate that P wave reflection coefficients always show negative values without any polarity reversal and with only weak variations in amplitude with the type and strength of applied deformation. The SH wave reflection coefficient for underside reflection undergoes a polarity reversal in the isotropic case, this polarity reversal is shifted to different epicentral distances when olivine is plastically deformed above the boundary. For shear deformation, the angle of incidence, i.e. the distance where the polarity reversal occurs changes also with azimuth. This can serve as discriminating factor and allows this method to be used as a diagnostic tool for identifying the style of deformation at boundary layers. For all deformation styles tested here the polarity change of SH waves occurs at short epicentral distances which are currently not used to
investigate upper mantle discontinuities. Further work needs to be carried out for two
anisotropic layers, however, the lack of published single-crystal elasticity of wadsleyite at
pressures and temperatures of the 410 km discontinuity is a strong limiting factor at the
moment. As a first test, using published elastic parameters of wadsleyite shows that the effect
of distance dependence for SH waves remains and shifts to larger epicentral distances while
the P wave reflection coefficient also shows a polarity reversal. Further extension of the
method to the 660 km discontinuity will help to better understand mantle dynamics and slab
descend.

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References


system Mg$_2$SiO$_4$-Fe$_2$SiO$_4$: Calorimetric measurements, thermochemical calculation, and geophysical


**Figure 1:** Schematic cartoon illustrating the effect of aligned minerals on the amplitude and polarity of the observed signals reflected off the 410 discontinuity, in different directions. This case describes an anisotropic layer of olivine which produces variable velocities in different directions (v1 and v2), above an isotropic layer of wadsleyite with the same velocity in all directions (v3). The variation of velocity in different directions in the layer above give rise to variable amplitudes and perhaps polarities (indicated by the two waveforms). The dashed line shows the P$_{410}$/S$_{410}$ path. The orange arrow represents the direction of deformation/shear that aligns the crystals above the 410 km discontinuity.

**Figure 2:** Textures and predicted reflection coefficients for P and S waves as a function of azimuth. The reflection coefficients are modeled for P-P and SH-SH waves reflected off the underside of the 410 km discontinuity. The textures are calculated using the plastic model of olivine of Raterron et al. (2014) at 405 km assuming vertical compression, perpendicular to the 410 km discontinuity. a) Macroscopic deformation in compression, with compression direction along the Z axis. b) Axes reference used for displaying textures in this Figure and in the following figures. c) Olivine textures displayed for a random starting polycrystal (top row) and after 100% deformation (bottom row) in axial compression. The left, central and right panels show distribution probability for the orientation of axes [100], [010] and [001] in stereographic projection. d) P-P and SH-SH reflection coefficients as a function of azimuth (thick black curve) for starting texture (non-deformed) (top row) and after 100% axial deformation (bottom row) of the olivine layer. The reflection coefficients are calculated for P-P and SH-SH waves at an incident angle of 45°. The reflection coefficient diagrams are colour
coded, blue and red areas indicate positive and negative reflection coefficients respectively. The thin black lines represent the size of the reflection coefficients plotted with the increment of 0.05, ranging from 0 to +0.1 for the positive reflection coefficients and from -0.1 to 0 for the negative ones. The size of the reflection coefficients are measured from the zero line between the positive (blue color) and negative area (red color). e) P wave (top panel) and S wave (bottom panel) reflection coefficients (solid circles) for different levels of deformation displayed over the incidence angle range of 15 to 65 degrees. Different levels of deformation are colour coded: white: starting texture, 25%, 50%, 75% and 100% axial deformation are shown by green, blue, yellow and red colours. Black dashed and solid curves represent the fitted polynomial to the values of the SH-SH reflection coefficients for the starting texture and the case of 100% axial deformation, respectively. The distance values corresponding to the critical incidence angle where the polarity reversal occurs are marked for the starting texture (vertical black dashed line) and for the maximum case of 100% applied deformation (vertical black solid line). The epicentral distances that correspond to the incidence angles at the 410 km discontinuity are marked by blue vertical dashed lines. Note that distances for the angles of incidence differ for P and S-waves.

**Figure 3:** Comparison of the textures calculated using two olivine plastic models taken from the study of Raterron et al. (2014), at the conditions of 405 km depth, with dominant slip along [001](010) and that of Tommasi (1998) with dominant slip on [100](010). a) Horizontal shear deformation, shear direction along X axis with Z axis normal to the shear plane. b) Pole figures representing textures for $\gamma$(shear strain)=2 (top row) and $\gamma$=4(bottom row) for olivine polycrystals for the model of Raterron et al. (2014). (c) Same as (b) but for the model of Tommasi (1998). The left, central and right panels in each section show distribution probability of the orientations of axes [100], [010] and [001] in stereographic projection.

**Figure 4:** Comparison of the textures calculated for deformation in axial compression using two olivine plastic models taken from the study of a) Raterron et al. (2014), at the conditions of 405 km depth, with dominant slip along [001](010) and b) that of Tommasi (1998) with dominant slip on [100](010). Pole figures representing textures for the case of 100% imposed deformation. The left,
central and right panels in each section show distribution probability for the orientation of axes [100], [010] and [001] in stereographic projection.

**Figure 5:** Predicted reflection coefficients of P and S waves reflected off the underside of the 410 km discontinuity when olivine is deformed in horizontal shear as a function of azimuth and using suggested dominant slip system of olivine taken from the study of Raterron et al. (2014). a) P-P and SH-SH reflection coefficients (black curve) for isotropic case (top row) and $\gamma = 4.0$ (bottom row). The incidence angle for these cases is 55 degrees. The blue and red colour and the thin black lines are the same as described in Figure 2.d. (b,c,d) P wave (left panel) and S waves (right panel) reflection coefficients (solid circles) for isotropic olivine and after $\gamma = 4.0$ deformation displayed over the incidence angle range of 15 to 65 degrees for the cases of azimuths parallel (b), 45 degrees (c) and perpendicular (d) to the direction of deformation. Different levels of deformations are colour coded: starting texture and $\gamma = 4.0$ are shown by white and red circles, respectively. Dashed and solid curves represents the fitted polynomials to the values of the SH-SH reflection coefficients for the cases of the isotropic model and $\gamma = 4.0$, respectively. The distance value corresponding to the incidence angle where the polarity reversal occurs are shown for the isotropic case (vertical dashed line) and for a shear strain of $\gamma = 4.0$ (vertical solid line).

**Figure 6:** Comparison of the S wave reflection coefficients for olivine deformed in horizontal and vertical shear using two different dominant slip systems for olivine. a) Predicted reflection coefficient of SH wave for a horizontal shear system (solid circles), modeled using Raterron et al. (2014) (R-14) plastic model of olivine shown for the incidence angle range of 15 to 65 degrees. b) SH wave reflection coefficient for a horizontal and vertical shear system displayed over the incidence angle range of 40 to 60 degrees using (R-14) and Tommasi (1998) (T-98) plastic models for olivine. Reflection coefficients are shown for the cases of azimuths parallel (top row), 45 degrees (middle row) and 90 degrees to the direction of deformation (bottom row) (horizontal shear) or normal to the shear plane (vertical shear).
Figure 7: Predicted reflection coefficients of P and S waves reflected off the 410 km discontinuity as a function of azimuth and using the dominant slip system of olivine taken from the study of Raterron et al. (2014). Olivine and wadsleyite are deformed in horizontal shear with shear strain of $\gamma = 4.0$ and $\gamma = 0.4$, respectively. a) P wave (left panel) and S waves (right panel) reflection coefficients (solid circles) displayed over the incidence angle range of 15 to 65 degrees for three cases of: isotropic olivine and wadsleyite (white circles), deformed olivine with shear strain of $\gamma = 4.0$ and isotropic wadsleyite (red circles) and for deformed olivine with shear strain of $\gamma = 4.0$ and wadsleyite with shear strain of $\gamma = 0.4$ (blue circles). The reflection coefficients are shown for the azimuths parallel (a), 45 degrees (b) and perpendicular (c) to the direction of deformation. Fitted polynomials to the values of the SH-SH reflection coefficients are shown for the cases of the isotropic model (dashed), deformed olivine with $\gamma = 4.0$ and isotropic wadsleyite (solid) and deformed olivine with $\gamma = 4.0$ and wadsleyite with $\gamma = 0.4$ (dashed-dotted). The distance value corresponding to the incidence angle where the polarity reversal occurs are shown for the isotropic case (vertical dashed line), deformed olivine ($\gamma = 4.0$) and isotropic wadsleyite (vertical solid line) and deformed olivine ($\gamma = 4.0$) and wadsleyite ($\gamma = 0.4$) (vertical dashed-dotted line). The epicentral distances that correspond to the right most and left most vertical lines are indicated.

Figure 8: Synthetic vespagram (e.g., Rost and Thomas, 2002) for the transverse component of a synthetic event in 50 to 60 degrees distance and a depth of 50 km calculated using the reflectivity method (Müller, 1985). The synthetic seismograms are computed using the velocity model ak135. The arrival times and slowness values of the S, SS, SS precursors, ScS waves as well as their depth phases, predicted for ak135 are indicated.

Table 1: Elastic parameters for olivine and wadsleyite at 410 km depth. For olivine, we use the full set of anisotropic single-crystal elastic moduli based on available literature data of Mao et al. (2015). Here, wadsleyite is assumed to be isotropic due to the lack of available data at high temperature.

Table 2: Plastic models for olivine. Model 1 is adopted from Raterron et al. (2014) at 405 km depth and model 2 is from Tommasi (1998). For each, the table indicates the relative critical resolved shear
stresses (CRSS) of each plastic deformation mechanism as well as the relative activities of each deformation mode after 50% axial compression and at a shear strain of $\gamma = 1$. For both plastic models, the CRSS of the isotropic relaxation mechanism was adjusted so that it accommodates 40 to 50% of the effective plastic activity. Stars indicate plastic modes that were not included in the simulation.

Figure 1
Figure 2
Figure 3
Figure 4
Figure 7
**Table 1**

<table>
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<th>$C_{ij}$ (GPa) $\cdot \rho$(g/cm$^3$)</th>
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Table 2