The effect of voids on matrix cracking in composite laminates as revealed by combined computations at the micro- and meso-scales

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Abstract

Voids are an important type of manufacturing defects in fiber-reinforced composites. Matrix cracking is sensitive to the presence of voids. Although this cracking occurs at the ply scale, its dynamics is strongly affected by ply’s microstructure, in particular, fiber distribution, fiber content, and the presence of voids. In the current study, a computational approach to simulate the influence of intra-laminar voids on cracking in composite laminates is developed. The approach combines finite element models of two scales: a micro-scale model, where the fibers and voids are modeled explicitly, and a meso-scale model, where the cracking phenomenon is captured on the ply scale. The micro-scale model, incorporating plasticity and damage in the matrix, provides input for the meso-scale model, which simulates the progressive cracking by means of the extended finite element method. The methodology is applied to investigate the effect of voids on the density of transverse cracks in cross-ply laminates in function of the quasi-static tensile load. Different sizes and contents of voids, which are chosen based on experimental micro-computed tomography data, are simulated. The numerical experiments show that the presence of voids leads to earlier start of the cracking, with the crack density evolution less sensitive to voids.

Keywords: B. Porosity; B. Transverse cracking; C. Finite element analysis (FEA); Multiscale modeling

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1 Introduction

Being defined as “regions unfilled with polymer and fibers” [1], voids are an important type of manufacturing defects in Fiber-Reinforced Composites (FRCs). Although there is a vast amount of research on voids and their effects on the mechanical behavior of FRCs, starting from the 1960s, it remains an intensively studied topic. A detailed review of the state-of-the-art on the voids’ formation, characteristics, and effects on
mechanical performance of FRCs can be found in [1]; early research is summarized in [2]. According to [1], voids are still important due to 1) the remaining unknowns about their mechanical influence, 2) being a central issue in modern manufacturing techniques, such as out-of-autoclave curing and automated prepreg laying, 3) becoming a point of concern in manufacturing of modern aeronautical parts with ever increasing geometrical complexity and modified resins, and 4) high costs associated with their removal during or repair after production, while a “void-free” composite is often not needed. As stressed in [3], modeling methods are needed to quantify the influence of voids on mechanical behavior of composites, which would allow definition of adequate allowance limits for design with “as manufactured” materials.

Voids are found to significantly degrade the matrix- and interface-dominated mechanical properties, whereas fiber-dominated properties show lower sensitivity to their presence [4-6]. Void content, a manufacturing quality parameter, is traditionally used for evaluation of the mechanical effects of voids. Nevertheless, recent studies, including [7-10], have shown that solely evaluating void content is not sufficient in the analysis of voids’ effects because it is a global parameter and provides no data on locally critical voids that can lead to (premature) failure. Hence, other void characteristics, i.e. shape, size, location, and distribution, also must be taken into account. This is mainly achieved by performing simulations [11] and micro-scale experiments, using such tools as X-ray micro-Computed Tomography (micro-CT) [8] and micro-scale digital image correlation [12, 13], which are increasingly popular in the investigation of voids’ effects.

One of the first damage modes occurring in composite laminates under thermo-mechanical loading is formation of matrix cracks running through the ply thickness and width (in the fiber direction). Although the cracking in off-axis plies is not the final failure mechanism in FRCs, it does induce other failure modes such as inter-laminar cracks (delamination) and fiber breakage, leading to the final failure of the laminate [14]. In cross-ply laminates, the matrix cracks in the 90° plies are called “transverse” cracks. The onset strain, the density growth rate, and the saturation density level are controlled by many parameters including ply thickness, laminate stacking sequence, properties of the fibers, matrix, and interface as well as by the volume fraction and distribution of the fibers. The transverse cracking is also sensitive to the presence of manufacturing defects such as intra-laminar voids, i.e. the subject of the present paper.

In the last five years, the interest in understanding the effect of voids on matrix cracking in FRCs has increased. For cross-ply carbon/epoxy laminates [15] and quasi-isotropic laminates of non-crimp-fabric carbon/epoxy plies [16], it was reported that voids have a more significant effect on the initial stages of cracking than on the final (saturation) stage. According to [15], this is because voids trigger the formation of...
initial matrix cracks in off-axis plies, but with the increase of the global loading, their effect on further cracking diminishes since fewer and fewer voids remain without cracks. This can be a reason for the random formation of initial cracks (from random voids) and a more uniform distribution with the increase of the loading [17]. It was observed that voids have a larger influence on matrix cracking in 90° plies than in 45° plies [16], which motivates the investigation of voids’ effect on matrix cracking in cross-ply laminates.

Performing a micro-scale digital image correlation in [12], the authors noted that voids create strain concentrations, leading to local plastic deformation of the matrix, causing earlier matrix failure. The strain concentration factor around a real-shape void was calculated numerically in [9] and correlated with the global strain to crack initiation. The initiation of cracks from voids in a cross-ply carbon/epoxy laminate was confirmed by a micro-scale in-situ analysis performed inside an electron microscope in [18], where the combined effect of voids and matrix cure degree on evolution of transverse cracking was investigated, using digital image correlation, also at the meso- and macro-scales.

Despite many noteworthy results, the available studies focus either on local analysis of voids or on their global influence and miss the link between the two. This link is, however, important as intra-laminar voids are micro-scale features, which interact with other heterogeneities in the material both at lower and higher scales such as fibers at the micro-scale and cracks at the meso-scale (the ply/laminate scale). Therefore, in evaluation and prediction of the effect of voids on statistically controlled properties, such as matrix cracking, one is confronted with the scale issue and needs an approach that would combine both scales.

Modeling of damage in laminated composites (the scale of millimeters) with direct representation of fibers (the scale of micrometers) requires significant computational resources and is feasible only in 2D formulation [19]. Today, such an approach in 3D would be difficult to realize even with the help of high-performance computer clusters. Attempts to bypass the challenge of scales may lead to unphysical representation of modeled phenomena, which is the case in [20] where meso-scale damage parameters are identified using micro-scale models without considering the important scale difference. The approach in [20] may be acceptable for materials exhibiting distributed micro-damage (like fiber/matrix debonding) but loses its adequacy for laminates with discrete damage such as ply cracking.

An alternative approach that is physically sound and yet computationally affordable is the one where models of different scales are linked together. This multiscale computational approach [21] relies on already developed models for each individual scale. For example, the transverse cracking (in the absence of voids) can be modeled using fracture mechanics approach [22] or eXtended Finite Element Method (XFEM) [23-25]. The
latter requires knowledge of the cohesive behavior of damaged elements, often linked to physical
characteristics such as strength and fracture toughness of the ply material. The strength and fracture toughness
can be evaluated experimentally or predicted using micromechanical models [26, 27]. In [28], the two scales
are bridged by assessing crack initiation using stress concentrations at the micro-scale, and calculating the
cracking evolution under fatigue loading using an empirical Paris-like law for the crack growth.

All the studies, referenced in the last two paragraphs, deal with materials free of voids. When voids are
present, and the aim is to understand correlations between the void characteristics and the crack density
evolution, the link between the micro- and meso-scale analyses becomes even more critical. This is because of
an additional scale factor, namely the characteristic length related to the voids’ size and spatial distribution (as
mentioned above). Therefore, a multiscale approach is required to predict the effect of voids on the cracking
evolution.

The present study proposes a numerical two-scale modeling approach to analyze the effect of intra-laminar
voids on the evolution of transverse cracks with applied strain. This approach accounts for the complexity of
different length scales being present and interacting. In the micro-model, these length scales are related to the
fiber size, density of the fiber packing, and void size; in the transition to the meso-model, the length scales are
related to the void content and voids’ spatial distribution; and in the meso-model, the length scale is linked to
the crack spacing and its evolution.

2 Combined two-scale approach

2.1 Methodology

A [0°/90°/0°] laminate, consisting of unidirectional (UD) fibrous plies with a given fiber volume fraction,
and under tensile loading in the 0° direction is modeled. The 90° ply (called also “transverse ply”) contains
voids. Based on the void characterization results (Section 2.2), the voids are assumed to have an elongated
shape and to be oriented in the fiber direction. This is because in this type of materials, voids are typically the
remaining dry volumes between the fibers. The void content, voids’ spatial distribution, and statistics of the
voids’ size and aspect ratio are given (either varied or assumed constant). The aim of the calculation is
simulation of the effect of voids on the cracking process in the 90° ply. The focus of this study is on challenges
in prediction of void-sensitivity of transverse cracking and the subsequent damage mechanisms such as
delamination are not considered at this stage.

Fig. 1 illustrates schematically the steps of the modeling methodology:
Step 1. Micro-scale modeling. A 3D Representative Defective Volume (RDV) of a transverse ply with a
void (“defective” ply) is modeled at the micro-scale, along with the Representative Volume Element (RVE) of
the “pristine” (reference) ply. The fibers are assumed transversely isotropic elastic bodies, all aligned in one
direction, and randomly distributed within the plane of isotropy. The matrix is modeled to account for
plasticity and pressure-dependent progressive damage [26]. The effective properties of the defective and of the
pristine material are computed using Finite Element (FE) method: stiffness matrix, strength under transverse
tensile loading, and Mode I fracture toughness. These properties are also referred to as “effective properties”
of the defective and pristine materials.

Step 2. Scale transition. The effective properties are transferred to a 3D meso-scale FE model of the cross-
ply laminate, serving as material parameters for “weak volumes”, which represent voids’ loci. The weak
volumes are distributed randomly in the transverse ply, according to a given void content, size, and aspect ratio
as well as voids’ spatial distribution and orientation. The cross-sectional size of the weak volume corresponds
to the size of the study region in the micro-scale model, for which effective properties are calculated.

Step 3. Meso-scale modeling. XFEM is utilized to model the onset and development of transverse cracking
in the 90° ply of the laminate under tensile loading.

2.2 Identification of typical void characteristics

For acquiring realistic data on void characteristics to be used in simulations, micro-CT was performed on a
[0/90]₄s carbon/epoxy laminate, produced through automated tape laying and autoclave curing at SABCA
Limburg NV, Belgium. Intra-laminar voids suitable for this study were intentionally introduced to the laminate
by means of the “low pressure cured debulked” processing, as described in [29]. The micro-CT was performed
with the HECTOR system [30], from Ghent University Centre for X-ray Tomography (UGCT). The images
were captured with a resolution of 6.55 µm/pixel, reconstructed in Octopus software and segmented via
VoxTex software [31]. The post-processing was performed in a volume of ~ 10 mm × 10 mm × 3 mm inside
the sample. Micro-CT analysis of a similar material, only with a different cure cycle (the manufacturer’s
recommended cycle), does not show any voids, as investigated in [32].

The detected voids have elongated shapes (Fig. 2a), and their cross-sectional shape is irregular. For
analysis of void characteristics, each void is fitted to an ellipsoid with three size parameters: major axis,
middle axis, and minor axis. The cross-section size is evaluated with the geometric mean of the transversal
axes, which are the middle and minor axes, as defined in Fig 2b. Moreover, for each void, a “roundness
factor”, i.e. the ratio of the minor and middle axes, and an “elongation factor”, i.e. the ratio of the major and
the geometric mean of the transversal axes, is defined. The orientation of the voids is quantified with the angle
between their major axis and the scan direction. The latter is close (within few degrees) to the 0° direction of
the laminate. There are some detected features, of which the minor axis is below 8 µm and the orientation is an
exact number. They seem to be false features due to creating non-physical clusters in the frequency
distribution graphs, so they are filtered out. Relative frequency distribution graphs of all the described
parameters are illustrated in Fig. 2. Around half of the voids have a geometric mean of the transversal axes
between 20 and 60 µm and a major axis (length) between 100 and 1000 µm. The results show that more than
half of the voids have a roundness factor above 0.6 (Fig. 2d) and an elongation factor above 6 (Fig. 2e).
Furthermore, most of the voids are aligned with the fibers in each UD ply (Fig. 2f).

The results of the micro-CT characterization were used to guide the choice of void characteristics and to
motivate simplifications in the simulations. For the sake of simplicity, the voids are assumed to have circular
cross-sections. The fact that more than half of the voids have a roundness factor above 0.6 makes this
assumption justifiable. Of course, once the modeling methodology is established, the effect of void’s shape can
be investigated, but it is out of the scope of the current study. The typical voids morphology is characterized
by large elongation factor. Therefore, the voids in the micro-model are assumed sufficiently long to the extent
that the plain strain condition can be applied. The actual length of the voids is assumed to be 1000 µm (as an
upper bound estimate) and is introduced in the meso-model. In order to study the effect of void cross-section
size, two cases are investigated based on the micro-CT results of the transversal axes mean: small (30 µm) and
large voids (60 µm). The former is close to the average transversal axes mean of the measured voids (i.e. 27
µm) and the latter represents the case of the largest voids. 95% of voids have a transversal axes mean below 60
µm.

### 2.3 Micro-scale modeling

The purpose of the micro-scale modeling is to evaluate the local effect of voids on the behavior of the UD
ply and to obtain input material parameters for the meso-scale model. To this end, 3D FE models of a UD
composite in the presence and absence of a single void are created. The carbon fibers in the models have a
radius of 3.5 µm, are aligned in the same direction, and randomly distributed in the isotropy plane (details in
Section 2.3.2).

For each void size, an RDV, which is a cuboid with a square cross-section, a small dimension in the third
(fiber) direction, and a void with circular cross-section in the center, is created. Additionally, for each void
size, a model for the pristine (reference) material without a void (an RVE) is built. Therefore, four models in
total are created, which are called hereafter “Micro-Ref-S”, “Micro-Void-S”, “Micro-Ref-L”, and “Micro-Void-L”, where Ref means Reference, and S and L stand for Small and Large void size, respectively. The micro-scale modeling is performed using the commercial FE software Abaqus 6.13 and its implicit solver. Although a higher number of RVEs and RDVs would provide more data for statistical analysis of the strength, one RVE and RDV for each case would be sufficient for this study since the statistical variation of strength caused by difference in fiber distribution is negligible when compared to the variation caused by voids, as seen in Table 1.

2.3.1 Model size

The two void sizes selected in Section 2.2 are considered for the diameter of the circular void in micro-modeling. For each void-size case, the void is placed in the center of the RDV, and the RDV cross-sectional size is chosen such that the void is sufficiently far from the RDV edges. This ensures that interaction between the void and the model edges is negligible. This distance is estimated using an analytical solution for tension of a homogenous plate with a circular hole in the center. Based on this solution, at a distance of 3.5 times the hole diameter from the hole center, the stress concentration caused by the hole is less than 5%. Thus, the RDV size is chosen as 7 times of the void diameter for each case. For the sake of computational cost, only one half of each RDV is modeled and symmetric Boundary Conditions (BCs) are applied. To further reduce the computational cost, the size of the RDV in the fiber direction is selected as a small value, i.e. 0.15 times the fiber radius, where fiber radius is 3.5 µm. Applying symmetric BCs in the fiber direction, plane strain conditions are simulated (Section 2.3.4). The RVE size is the same as its corresponding RDV size for each void size. Therefore, the RVE and RDV size for the 30-µm-diameter void is 210 µm × 105 µm × 0.525 µm, and for the 60-µm-diameter void is 420 µm × 210 µm × 0.525 µm. The RVEs and RDVs with their sizes are shown in Fig. 3.

2.3.2 Fiber distribution

The fibers are uniformly randomly distributed inside each model, using the algorithm developed in [33] and investigated versus real microstructures in [34]. The target fiber volume fraction is 58%, and the low and high bounds for minimum distance between the centers of fibers are 2.05 and 2.2 times the fiber radius, respectively. All the fibers that fall on the model edges are manually repositioned to have them exactly halved. This is performed to allow a physically correct application of symmetric BCs. Such fiber repositioning has a negligible effect on the modeling results since three of the four edges are excluded in post-processing. In addition to this, for the cases with a void, i.e. Micro-Void-S and Micro-Void-L, the fibers, overlapping the void,
are either removed or manually repositioned to fill the area surrounding the void, depending on the size of the
unoccupied matrix region around the void. In some cases, there was a need for small repositioning of the
neighboring fibers as well. Although the overall fiber volume fraction remains similar for the cases with and
without a void, this adjustment of the fiber positioning causes a small increase in the local fiber volume
fraction around the void, which can also occur in reality since voids may push the surrounding fibers away [5].
The final fiber volume fraction of all the cases is within 57-58% (shown for each model in Table 1).

2.3.3 Material models for the constituents

There are three constituents modeled in the micro-modeling: carbon fibers, epoxy matrix, and voids.
Carbon fibers (AS4 from Hexcel) are modeled as a transversely isotropic material, with properties taken from
[19]. Their longitudinal elastic modulus, transverse elastic modulus, in-plane Poisson’s ratio, out-of-plane
Poisson’s ratio, and in-plane shear modulus are respectively 232 GPa, 13.0 GPa, 0.30, 0.46, and 11.3 GPa.
Voids are modeled as an isotropic material with extremely low mechanical properties (not zero to avoid
instability in computations), namely $10^{-6}$ for both Young’s modulus (in GPa) and Poisson’s ratio.

Matrix is simulated with a continuum model for an epoxy material as characterized in [35] and used in [26,
27]. Its elastic modulus, Poisson’s ratio, plastic Poisson’s ratio, tensile strength, and fracture toughness are 3.9
GPa, 0.39, 0.30, 93.0 MPa, and $90 \ J/m^2$ ($0.09 \ N/mm$), respectively. The continuum model, developed in [26]
and applied in [27], is a constitutive pressure-dependent model, and accounts for linear elasticity, plasticity,
and progressive damage of the matrix. The yield is described by the paraboloid yield criterion presented in
[36]. Hardening is considered with an increase in equivalent plastic strain both under tension and compression.

For this, experimental stress-strain data from [35] are fed to the model. The matrix damage is considered to be
isotropic and modeled based on the thermodynamics approach. Damage input parameters are tensile strength
and Mode I fracture toughness. More details of the matrix model can be found in [26]. This model is
implemented as a User-defined MATerial model (UMAT) user subroutine in the Abaqus software.

The interface between fibers and matrix is assumed to be perfect. The focus of this study is development of
a methodology for analysis of the effect of voids, and the number of influencing parameters is intentionally
kept to a minimum. Of course, once the methodology is established, one can explore the effect of many
parameters including interfacial strength and fracture energy.

2.3.4 Mesh and boundary conditions

The 3D micro-models are discretized with Hex-dominated control, which causes ~ 4% of the elements to
become wedge elements (C3D6), and the rest to have hexahedral shape (C3D8R). In order to have a finer
mesh on the fiber/matrix interfaces, they were seeded with a size half of that on the model edges. The element size on the fiber/matrix interfaces is ~ 0.4 µm. The models have only one element in the fiber direction. The total number of elements in the small models (Micro-Ref-S and Micro-Void-S) is ~ 111000, and in the large models (Micro-Ref-L and Micro-Void-L) is ~ 472000. The mesh independency of the micro-scale model is explored in [26].

To calculate effective elastic properties ($E_L$, $E_T$, $v_{LT}$, $v_{TT}$, $G_{TT}$), which will be used in the meso-modeling, elastic homogenization is performed, considering no damage and plasticity for the matrix. Assuming transverse isotropy, three separate sets of BCs (tensile loading in three directions) are applied to each micro-model, as described in [37]. Then, the uniaxial transverse tension problem is considered to model failure. Transverse tension is applied to the models by exerting constant displacements to the left and right edges. In the other two directions, i.e. fiber direction and the other transverse direction, Poisson’s contraction is prescribed through constant displacements, calculated based on the effective elastic properties of the ply, using analytical formulas of Chamis [38] for each case. For example, the effective properties calculated for Micro-Ref-S with a fiber volume fraction of 57.6% are as follows: the longitudinal elastic modulus, transverse elastic modulus, in-plane Poisson’s ratio, out-of-plane Poisson’s ratio, and in-plane shear modulus are respectively 135 GPa, 8.3 GPa, 0.34, 0.42, and 4.2 GPa. To help with the convergence of the damage models, stabilization and automatic damping are applied. Since only the local properties of the material, in the presence and absence of voids, are calculated using the micro-scale models (and not the global properties), periodic BCs (of which some examples can be found in [33, 39, 40]) could also be applied instead of symmetric BCs.

2.3.5 Post-processing: calculation of the effective properties

The results of the micro-modeling include (a) stress-strain fields in the elastic regime of loading and (b) stress-strain history during loading until full formation of the transverse matrix crack and load drop to zero. The matrix crack is seen in Fig. 3 as the elements with a “damage variable” of 1 (fully damaged). These results are processed to obtain the properties of the defective and pristine materials needed for the meso-model. This processing accounts for the size effect in the defective material: effective properties of a volume containing a void with a given size depend on the size of the volume. Therefore, three regions are defined in the micro-models for calculation of the effective properties. The regions’ sizes are referred to below as rectangles $X \times Y$ around half a void (Fig. 3), which correspond to $X \times 2Y$ rectangles around the full void (due to symmetric BCs).
Regions for calculation of elastic properties (E-regions in Fig. 3). The micro-model resulting elastic properties will be used in the meso-models to represent effective properties of the pristine material and reduction of elastic properties of the defective material. The homogenization is performed on different regions of the micro-models with different fiber and void volume fractions. For the pristine material, this region is E-Ref-S, which comprises the full volume of Micro-Ref-S (Fig. 3a). For the defective material, two regions are defined to represent two values of the void content (1.6% and 5%) in each of the Micro-Void-S and Micro-Void-L models. The full volume of the micro-models corresponds to the void content of 1.6%; it has a size of 210 µm × 105 µm (region E-S-Low%) in Micro-Void-S and 420 µm × 210 µm (region E-L-Low%) in Micro-Void-L (Fig. 3b and e, respectively). Regions, corresponding to the void content of 5%, have dimensions of 119 µm × 59.5 µm (region E-S-High%) and 238 µm × 119 µm (region E-L-High%) respectively in Micro-Void-S and Micro-Void-L and are respectively shown in Fig. 3b and e as red rectangles.

Regions for calculation of damage-related properties (D-regions in Fig. 3). These properties are transverse strength and Mode I fracture toughness to be used as parameters of the cohesive law, used for prediction of ply cracking. The region has the size 100 µm × 35 µm, corresponding (accounting for the symmetry) to a 100µm×70µm rectangle around the void. It is called D-Ref-S, D-S, and D-L in Micro-Ref-S, Micro-Void-S, and Micro-Void-L, respectively (dashed and solid black rectangles in Fig. 3a, b, and e respectively). Fig. 3c and f show the micro-model resulting tension diagrams, presenting dependency of the transverse effective stress on the transverse effective strain calculated for all the micro-scale models and different post-processing regions. Further processing of these curves and extraction of the material properties used in the meso-scale modeling is described in Section 2.4.3. If the void content is high enough to have significant interaction of the neighboring voids, affecting the damage development in their vicinity, the micro-model should include multiple voids to reflect this interaction. However, the current model does not account for this effect, which is an approximation based on the relatively low void contents.

2.4 Meso-scale modeling

Five meso-scale models, all with [0°/90°/0°] stacking sequence, are created for analysis of transverse cracking: the reference model without voids, the models with small (30-µm transversal axes mean) and large (60-µm transversal axes mean) ellipsoidal voids, with the global void content, in each case, at two levels: 1.6% (low) and 5% (high). The meso-models are called hereafter: “Meso-S-Low%”, “Meso-S-High%”, “Meso-L-Low%”, “Meso-L-High%”, and “Meso-Ref”, where S and L stand for Small and Large void sizes, respectively,
and Ref for the case without voids. The meso-scale modeling is performed in *Abaqus 2017*, using its implementation of the XFEM, and its implicit solver.

The XFEM allows modeling of initiation and propagation of multiple cracks in certain areas of the model, where elements are enriched by adding extra degrees of freedom to the nodes. Those areas are referred to hereafter as “enriched” regions. *Abaqus 2017* imposes restrictions on the definition of the enrichments: there should be at least two non-enriched elements between two successive enriched regions, and the total number of enriched regions in the model cannot exceed 100. For more detailed discussion on how the XFEM works in application to cracking in composites, the reader is referred to [25].

### 2.4.1 Geometry, mesh, and boundary conditions

Each 3D meso-scale model simulates a [0°/90°/0°] specimen that is 20 mm in both width and length and made of plies with 0.21 mm thickness (Fig. 4a). The coordinates’ notation is as follows: Z coordinate corresponds to the 0° direction, X to the 90° and Y to the thickness direction. The model is meshed such that each ply has 3 elements through the ply thickness, 100 elements along the width, and 300 elements along the length direction (Fig. 4b). The transverse ply has 100 enriched regions (the maximum admissible number), each occupying one element in the laminate length direction, the full width, and the full thickness of the middle ply. They are aligned in the width direction and evenly spaced along the laminate length with two non-enriched elements in between (Fig. 4b). There are two sizes of elements: 100 μm × 70 μm × 200 μm and 50 μm × 70 μm × 200 μm respectively in the Z, Y, and X directions. All elements of the XFEM-enriched regions have the former size, while the latter size is used for the elements between the enriched regions. Mesh sensitivity for XFEM solution was studied in [25]. For convergence of the model, viscous regularization is applied to stabilize the response during damage. The numerical viscosity value is chosen such that it has negligible influence on the XFEM cohesive behavior.

The BCs for the meso-model are as follows. Tensile displacement along the Z-axis, equivalent to 1.8% of strain, is applied using constant displacement on one side and zero displacement (symmetry) on the other. A single node from the latter is pinned to avoid rigid body motion. The rest of the boundaries are left free.

### 2.4.2 Voids representation

The presence of voids in the laminate is modeled by introducing “weak volumes”, which represent zones where the material behavior is influenced by the presence of a void. The material outside of the weak volume is referred to as “pristine” material. The size of the weak volume, 100 μm × 70 μm × 1000 μm (Z × Y × X), corresponds to the size of the D-region used for calculation of the effective properties in the micro-model.
(Section 2.3.5), and weak volume properties correspond to the effective properties of that region. A weak volume then includes a virtual ellipsoidal void, as illustrated schematically in Fig. 5, and includes a row of five meso-elements in an enriched region (in the X direction) and two adjacent rows of five meso-elements in a non-enriched region (in the Z direction). The size of the void does not affect directly the weak volume size, but has an influence on its material properties as further discussed in Section 2.4.3. For a given void content in the 90° ply, the lower bound for the number of the weak volumes can be calculated by dividing the target void volume by the volume of the virtual void in the weak volume. It is the lower bound because weak volumes are truncated if they cross the ply boundaries.

The weak volumes are distributed within the transverse ply of all meso-models except Meso-Ref. The location of a weak volume is determined by its centroid. A distribution algorithm randomizes the location of a new weak volume using uniform probability distribution in all three directions. Overlapping of the new volume with previously positioned ones is not allowed. This process repeats until the desired void content (1.6% or 5%) is reached. The number of weak volumes distributed in the Meso-S-Low% and Meso-S-High% models is 2878 and 9023 and in the Meso-L-Low% and Meso-L-High% is 718 and 2246, respectively. In all the models, about half of the distributed weak volumes appear in the enriched regions. Having all the weak volumes in the enriched regions asks for enrichment of the entire transverse ply, which is not possible in the current XFEM implementation in Abaqus 2017. The distribution of weak volumes in each model is represented in Fig. 4 c-f. One can notice longer weak volumes in Fig. 6-4d, which are a result of agglomeration of the normal-size weak volumes. This is further discussed in Section 3.2.

2.4.3 Material properties

The material within weak and pristine volumes outside the enriched regions is assumed to be elastic, while inside them it follows a bilinear cohesive law. The latter governs the damage behavior in the enriched elements and requires knowledge of the peak stress (interpreted as transverse strength) for activation of damage, and the area under the traction-separation curve (interpreted as intra-laminar Mode I fracture toughness) for damage evolution. Both elastic and damage related properties for these different regions are extracted from micro-scale models (as discussed in Section 2.3.5 and shown in Fig. 3). Only the in-plane shear modulus \( G_{12} \) is calculated using analytical formulas of Chamis [38]. The extracted properties from the micro-models are reported in Table 1.

More specifically, elastic properties of the reference material Meso-Ref are taken from region E-Ref-S. In the models with voids, the transverse stiffness of the entire middle ply (both in weak and pristine volumes) is
reduced, while other elastic constants are kept the same as those taken from \textit{E-Ref-S}. The reduced transverse stiffness is obtained from the micro-scale models with the corresponding void content: homogenization in regions \textit{E-(S/L)-(Low/High)\%} results in the transverse stiffness for \textit{Meso-(S/L)-(Low/High)\%}, respectively. Properties of the $0^\circ$ plies are left without change, i.e. taken from \textit{E-Ref-S}. The initial stiffness of the bilinear cohesive law is automatically assigned by the software based on the stiffness of the material in enriched regions.

The transverse strength is obtained as the maximum stress in the effective stress-strain curve for a certain region (Fig. 3c and f). More specifically, the strength to be used in pristine elements is obtained from \textit{D-Ref-S} region. The strength in weak elements is obtained from \textit{D-S} region for \textit{Meso-S-(Low/High)\%} and from \textit{D-L} region for \textit{Meso-L-(Low/High)\%}. The strength values are reported in Table 1. The void content for analysis of the transverse stiffness is calculated at the element-level (in the micro-models) and the effect is applied at the ply-level, while void content for analysis of the strength is analyzed at the ply-level (in the meso-models) and the effect is applied at the element-level.

The fracture toughness is found by fitting the area under the effective stress-strain curve obtained in the micro-scale model for a specific region to the results of an XFEM single-element model. More specifically, the effective stress-strain curve for the region \textit{D-Ref-S} is used to get the toughness in pristine elements, while the fracture toughness in weak elements is obtained from \textit{D-S} region for \textit{Meso-S-(Low/High)\%}, and from \textit{D-L} for \textit{Meso-L-(Low/High)\%}. This identification of the fracture toughness via the XFEM single-element modeling yields a value of 33 J/m$^2$ for the pristine material, 18 J/m$^2$ for the weak material with the small void, and 9 J/m$^2$ for the one with the large void.

There is a variation in local strength and toughness properties of a ply due to microstructural heterogeneity like fiber distribution. In order to account for the local variation, a random coefficient is taken from a normal distribution around 1 with the standard deviation of 15\% (according to [41]), and is assigned to each enriched region. The strength of both weak and pristine elements in each enriched region is then modified by multiplying it by the random coefficient. The fracture toughness of the elements in each enriched region is multiplied by the square of the coefficient of that region, as proposed in [25].

\subsection*{2.4.4 Post-processing: determining the crack density}

The outcome of the meso-scale modeling is the predicted crack density evolution in function of the applied strain. In the XFEM, damage occurs on “cohesive surfaces” across the enriched-region elements (Fig. 4g), and the damage progression is expressed by a status variable, called cohesive scalar damage variable (CSDMG). It
is 0 for cohesive surfaces before or at the initiation stage, and reaches 1 for the fully-developed damage, which corresponds to a traction-free state of the cohesive surface in the element and is interpreted as a physical crack. Together with the traction-free cohesive surfaces in the neighboring elements a continuous surface can form, which is referred to as a “traction-free crack”. In [25], the reader can find a detailed discussion on identification of cracks in XFEM calculations. The predicted crack density at progressive simulation stages is calculated based on the traction free cracks. For the sake of brevity, they are referred to simply as “cracks” hereafter. The position, direction, and length of each of the cracks is defined at every step of the simulation, as illustrated in Fig. 4g.

It is assumed in the software that the crack surface is normal to the loading direction (global 0°) since the normal traction on this surface is at its maximum in comparison to any other possible crack surfaces. This is a valid assumption especially for rather thick plies such as that being modeled in the current study.

The crack density in calculations can be determined based on two methods. The first method (called here “Half-Span Method”) counts the number of “well-developed” cracks, while just initiated short cracks are not counted. In experiments (for example in [42]), it is common to count well-developed cracks, protruding through more than half of the width of the specimen. Therefore, the crack density is determined as the number of cracks, which are longer than half of the specimen width, divided by the specimen length. The shorter cracks are then ignored in this counting method. With the presence of voids, this method neglects the initiation of cracks originated on one side from a void inside the 90° ply, connecting to the nearest ply boundary, and counts the crack only when it propagates from the other side of the void to the mid-width of the specimen. Hence, the effect of voids on the cracking initiation and development would be underestimated.

Another way to calculate the crack density (called here “Surface Area Method”) is to divide the total surface area of all cracks by the volume of the ply. With this method, all cracks, regardless of their length, are taken into account. If all cracks span the width of the ply immediately, then the two methods are equivalent.

3 Results and discussion

3.1 Effect of voids on properties at the micro-scale

The elastic constants obtained from elastic homogenization of the four micro-scale models are presented in Table 1. Volumes with different sizes are chosen in the RVEs and RDVs (as indicated in Fig. 3). This allows studying the local effect of the voids on elastic constants as well as calculating effective degraded properties to be fed into the weak volumes of the meso-scale models. According to the results in Table 1, there are two parameters affecting the elastic constants: the fiber volume fraction and void content. The highest sensitivity is
noted for transverse elastic moduli and out-of-plane shear moduli, while longitudinal elastic moduli and
Poisson’s ratios are negligibly sensitive to the void content, but dependent on the fiber volume fraction.

The micro-scale models show that voids initiate transverse cracks as shown in Fig. 3b and e, and the
transverse strength and the strain to failure are reduced in the presence of voids (Fig. 3c and f). For the same
void content, the reduction caused by the larger void is higher. Moreover, the influence of void content on
transverse strength is less significant than that of void size. The abrupt drops in the effective stress-strain
curves correspond to the full volume of the micro-models, where a sudden crack leads to the total loss of the
load carrying ability of the modeled material. For the smaller regions, the curves do not show abrupt drops.
This is because the crack opening is more significant when compared to the length of the smaller regions and
therefore causes a significant increase in strain. In the full volume of the micro-models, the crack opening is
negligible compared to the length of the region, causing negligible increase in strain.

Although the homogenized elastic constants obtained from either of the reference micro-models, i.e.
Micro-Ref-S and Micro-Ref-L, are sufficient as input for the pristine material in the meso-scale models, the
homogenization results of both models are reported (in Table 1) to show the small statistical variation caused
by the variation in the fiber distribution. Moreover, having a reference model for each void-size case allows
qualitative comparison of crack initiation and propagation in the absence and presence of the voids.

3.2 Effect of voids on transverse cracking

Fig. 6 shows the crack density predictions in all meso-models, using the Half-Span Method (Fig. 6a) and
Surface Area Method (Fig. 6b). The results of both methods are close to each other and show the same trend.
The Surface Area Method produces smoother growth of the crack density with the applied load. As explained
in Section 2.4.4, it considers all cracks regardless of their length and hence provides a more precise analysis of
crack density. It is used in the discussion below.

The crack density vs. applied strain curves (Fig. 6b) demonstrate that the presence of voids influences the
cracking onset threshold and the crack density at the progressive stages of the loading. Comparing the two
extreme cases, the reference case and the case with 5% of small voids (having the largest number of voids), it
is seen that the onset of the steady progressive cracking (indicated with an arrow in Fig. 6b and explained
below) is shifted from ~0.6% in the reference model down to ~0.5% in the model with voids. The crack
density during the loading is consistently (about 0.3 to 1.0 cracks/mm) higher in the model with voids; for
instance, the difference at 0.6% applied strain is ~0.75 cracks/mm, at 0.9% is ~0.5 cracks/mm, and at 1.2% is
~0.6 cracks/mm. The maximum crack density in both cases is ~5 cracks/mm, which is due to a limitation of
the model (as explained in the end of the section).

The cracking onset can be defined in two ways: the appearance of the very first crack and the onset of the
steady progressive cracking. The first type is predicted to happen at 0.5% applied strain in the reference case.
Presence of voids, regardless of their content percentage or their size, reduces the “strain at first crack” to
0.2%–0.4%, as tabulated in Fig 5b. Early stages of loading in meso-scale models are illustrated in Fig. 7,
where cracks are initiated mainly from weak volumes. Further on cracks propagate rapidly through the
specimen’s width. The finding that voids influence the initial stages if cracking is consistent with experimental
observations, e.g. in [15-17]. The strain at first crack can be expected to depend strongly on the particular
instance of the stochastic realization of the void position and of the strength distribution in the 90° ply. Thus,
analysis of the strain at first crack for different variants of the voids, as simulated and presented in Fig. 6b,
should be performed with caution. However, the lowest strain at first crack of 0.2% for Meso-L-High% and
0.3% for Meso-L-Low% (two cases with large voids) can also have a physical explanation: large voids with a
transversal axes mean of 60 µm, or about 1/3 of the ply thickness, create larger stress concentrations leading to
a crack across the ply, than smaller 30-µm voids.

The second definition of cracking onset is the start of steady progressive cracking, which appears as a knee
in the crack density vs. applied strain curve (indicated with an arrow in Fig. 6b). In the current calculations, the
knee point is the first data point, where one of the following statements holds true: a) at least, three new cracks
are developed, i.e. the crack density is increased by a value ≥ 0.15 cracks/mm, or (b) at least, three consecutive
points with minimum one new crack development occur, i.e. the crack density is increased at each of the
consecutive points by a value ≥ 0.05 cracks/mm. This definition of cracking onset is expected to give a more
stable characteristic of the crack density evolution due to lower sensitivity to the stochastic variability of the
void positioning and local strength in the ply.

The simulation results show that the onset of steady cracking shifts to lower strains only if the number of
voids is sufficiently large. The strain to onset of steady cracking for Meso-S-Low%, Meso-L-Low%, and Meso-
L-high% is respectively 0.65%, 0.66%, 0.61% which is close to that for the reference case, i.e. 0.63%.
However, Meso-S-High% shows a lower strain to onset of steady cracking, namely 0.50%. A high volume
fraction of small voids (in Meso-S-High%) results in a larger number of voids, compared to the other cases
(Fig. 4c-f). Larger number of voids results in their closer positioning, which can lead to void agglomeration.
The agglomeration level can be defined as the number of touching weak volumes (with no elements in
between) within enriched regions divided by the total number of weak volumes. With this definition, the
agglomeration level in *Meso-L-Low%* and *Meso-L-High%* is 29% and 64%, respectively, and in *Meso-S-
Low%* and *Meso-S-High%* it is 74% and 100%, respectively. In *Meso-S-High%*, all the weak volumes touch
each other, which create larger continuous regions with degraded properties, facilitating crack propagation.
Physically, this corresponds to cracks connecting the voids.

Once a steady cracking stage is reached, further cracking progresses with almost the same crack density
growth rate, meaning that the crack density vs. applied strain curves stay parallel. This may point out that the
crack density evolution after the onset of steady cracking is not a void-related phenomenon and is governed by
the same relations between the stress redistribution in the ply upon crack formation and the local ply strength.
The maximum crack density predicted in all the models converges to ~5 cracks/mm, which is the limitation of
the model. As stated in Section 2.4, the number of enriched regions in the model is limited to 100 by *Abaqus
2017*. Considering the length of the model (20 mm), this means that the crack density cannot exceed 5
cracks/mm. To correctly predict the crack density at saturation, one would need to increase the number of
enriched regions in the model.

A multi-scale experimental study on the effect of voids on the evolution of transverse cracking was
performed in [18], where voidy carbon/epoxy cross-ply laminates were produced with the same cure
conditions as that mentioned in Section 2.2. It was found that the chosen cure parameters led to not only the
voids but also an incomplete cure of the matrix. The meso-scale measurements revealed that the combination
of the voids and incomplete matrix cure is responsible for a dramatic decrease of the strain to onset cracking
and an increase of the crack density at saturation, both measured at the laminate’s edge. The micro-scale
analysis showed clear evidence for voids triggering the first cracks. Although results of this experimental
investigation agree in general with those of the current study, there are some barriers for a quantitative
comparison of the results. These are as follows: 1) the constituents’ properties in the micro-model do not
necessarily correspond to the experimentally tested material; 2) in the experiments, there is another factor
influencing the cracking in addition to the voids, namely incomplete matrix cure, which is not accounted for in
the modeling; 3) the voids’ characteristics are not the same in the modeling and the experiments, and are
difficult to be controlled in the latter; 4) the laminate stacking sequence is different in the modeled and tested
materials; 5) the crack density in the modeling is calculated using cracks’ surfaces in 3D, while in the
experiments, it is measured only at the laminate’s edge; and 6) the modeling approach has limitations in
prediction of the crack density at saturation. Once these issues are resolved, one should be able to compare and validate the predictions against the experimental results.

4 Concluding remarks

We have developed and presented in this paper a combined two-scale methodology for simulation of the matrix cracking in cross-ply composite laminates in the presence of voids. The micro-scale model simulates matrix cracking in a “representative defective volume” with direct representation of a random placement of unidirectional fibers around a void. The meso-scale model simulates cracking in the 90° ply of a cross-ply laminate, utilizing XFEM. The effective properties of the material at the micro-scale are used as input parameters for the meso-scale model, including weak volumes in the 90° ply, representing the material degraded by voids. The key feature of the model is a link between the micro- and meso-scales. A scale link between the micro- and meso-model is created, which adequately accounts for the influence of the micro-scale model size on its effective mechanical behavior.

Application of the two-scale modeling methodology to cracking evolution under tension loading is explored in a typical [0°/90°/0°] carbon fiber-reinforced epoxy laminate in the presence of voids for two levels of the void content (1.6% and 5%) and two levels of the void size (30-µm and 60-µm diameter). The characteristic features of the cracking evolution with increase of the applied tensile strain are as follows:

1. The maximum effect of the presence of voids is observed in the model with 30-µm voids and 5% void content. The onset of the steady progressive cracking is shifted down to ~0.5% from ~0.6% in the reference model. The crack density during the loading is consistently higher in the presence of voids, with a difference of ~20% in the middle of the loading, i.e. ~0.9% applied strain.

2. The presence of voids affects the strain corresponding to initiation of the first crack, decreasing the strain at first crack from 0.5% in the reference model down to 0.2%-0.4% in the presence of voids (depending on the voids’ parameters).

3. The onset of the steady cracking (a knee on the crack density vs. applied strain curve) changes significantly only for the case of high (5%) void content and smaller (30 µm) voids size, i.e. Meso-S-High%. For other cases, the voids do not affect this threshold. This difference in behavior is attributed to a much higher number of voids in Meso-S-High% case, causing higher degree of voids’ agglomeration.

4. The growth rate of the crack density vs. applied strain curves does not change with the presence of voids.
Generalizing these features, the present simulations suggest that the presence of voids:

- affects the onset and development of first sporadic cracks, associated with voids;
- affects the onset of the steady progressive cracking only if the void content is sufficiently high and the voids are placed with sufficient density;
- does not affect the rate of cracking.

Simulation of matrix cracking in the presence of voids allows analyses which are not always feasible to perform experimentally. For instance, it allows 1) identifying the effect of voids without a need of (a large number of) experimental tests that are typically costly and eco-unfriendly, 2) performing parametric studies on the effects of voids’ characteristics, such as size and morphology, on cracking, which is not achievable experimentally, and 3) 3D analysis of the interaction between voids and cracks, which is also possible using in-situ micro-CT, but only on small samples that may not be representative. Furthermore, the developed methodology is useful for simulation of matrix cracking in other laminate configurations as well as other types of defects.

Although promising, the developed methodology needs further work. For example, prediction of crack densities at saturation requires enhancement of the XFEM technique, particularly on the side of the enrichments. Delamination, being another important damage mechanism in composites, should be included in the analysis. For higher accuracy of predictions, one should also account for the residual thermal stresses.

Acknowledgments

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References


Figure captions

**Figure 1.** The combined two-scale approach: phenomena and features to be considered in the models – the roadmap for numerical modeling of the effect of voids on matrix cracking.

**Figure 2.** Void size characterization using micro-CT: (a) a 3D visualization of voids in the cross-ply [0/90]4s carbon fiber/epoxy laminate and definition of the void axes; relative frequency distributions of (b) the geometric mean of the transversal axes, (c) the major axis, (d) the cross-section roundness factor, (e) the elongation factor, and (f) the void in-plane orientation.

**Figure 3.** Micro-scale modeling of matrix damage under transverse tension in (a), (b) the small and (d), (e) the large model; (c), (f) their corresponding effective stress-strain curves for different regions that are indicated on the micro-models – due to symmetry, half-width models are considered.
Figure 4. Representation of the (a) lay-up and geometry of the meso-scale model, (b) laminate mesh with enriched regions (dark green) in the transverse ply; weak volumes (light green) distributed in the transverse ply of (c) Meso-S-Low%, (d) Meso-S-High%, (e) Meso-L-Low%, and Meso-L-High%; (g) cracks in Meso-S-Low% (as an example) initiated from the weak volumes (at 0.72% of applied strain) – blue represents the regions between the enriched regions in the transverse ply.

Figure 5. Schematic representation of a weak volume (a) in enriched regions (occupying five elements) and (b) in non-enriched regions (occupying ten elements) – the blocks show meso-scale elements and the ellipsoid is a virtual void inside the weak volume – the color scheme corresponds to the elements in the enriched and non-enriched regions shown in Fig. 4b.

Figure 6. Density of traction-free cracks vs. the applied strain – crack density calculated with (a) Half-Span Method: the number of cracks reached the half of the width divided by the specimen length, (b) Surface Area Method: the total surface area of the cracks divided by the transverse ply volume. The tables present the strain level at both first crack and steady cracking onset for the different models.

Figure 7. Crack surfaces as predicted in the meso-models: (a) Meso-S-Low% and (b) Meso-L-Low% both at 0.54% applied strain, (c) Meso-S-High% and (d) Meso-L-High% both at 0.45% of applied strain – CSDMG stands for cohesive scalar damage variable and red color denotes traction-free crack surfaces.
Table 1 Elastic properties and strength, obtained numerically for different regions, with different fiber volume fraction ($V_f$) and void content ($V_v$), in the four micro-models.

<table>
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<tr>
<th>Region size ($\mu$m$^2$)</th>
<th>Region ID</th>
<th>Volume fraction (%)</th>
<th>$E_i$ (GPa)</th>
<th>$E_T$ (GPa)</th>
<th>$v_{LT}$</th>
<th>$\nu_{TT}$</th>
<th>$G_{TT}$ (GPa)</th>
<th>$\sigma_T$ (MPa)</th>
<th>Region ID</th>
<th>Volume fraction (%)</th>
<th>$E_i$ (GPa)</th>
<th>$E_T$ (GPa)</th>
<th>$v_{LT}$</th>
<th>$\nu_{TT}$</th>
<th>$G_{TT}$ (GPa)</th>
<th>$\sigma_T$ (MPa)</th>
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<td>P,W, all</td>
<td>whole Meso-Ref: 0° plies, all models</td>
<td>P,W, all</td>
<td>P,W, all</td>
<td>pristine, all models</td>
<td>135 8.04 0.34 0.54 2.61 64.14</td>
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<td>E-Ref-S</td>
<td>90° ply, Meso-S-Low%</td>
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<td></td>
<td></td>
<td>Micro-Void-S</td>
<td>E-Ref-S</td>
<td>90° ply, Meso-S-High%</td>
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<td>136 0.33 0.52 2.53 47.9</td>
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Notes:  
1. The **bold** values are used as the input for the meso-models that are specified above them.  
2. “P,W, all” means “pristine and weak elements, all models”.  
3. Regions ID’s are given for regions, of which the properties were transferred to the meso-models and indicated in Fig. 3.
Step 1: micro-scale finite element model with matrix plasticity and damage
Step 2: random distribution of weak volumes with effective properties
Step 3: cracking prediction with extended finite element method

Figure(s)

Matrix cracking
Intra-laminar voids
200 μm
50 μm

Effective stress
Effective strain
Void
Representative volume element

Predicted matrix cracking in transverse plies
Weak and pristine volumes with effective properties
Representative defective volume
Figure(s)

(a) (b) (c)

In-plane orientation:
angle between a and
the scan orientation

(d) (e) (f)
Figure(s)

(a) (b)
cross-section view
cross-section view

Y
X
Z

70 μm
100 μm
200 μm
70 μm
50 μm
200 μm
**Half-Span Method**

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<th>Material</th>
<th>First Crack</th>
<th>Steady Onset</th>
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<td>0.63</td>
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<tr>
<td>Meso-S-High%</td>
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<td>0.50</td>
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<tr>
<td>Meso-L-Low%</td>
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</tr>
<tr>
<td>Meso-L-High%</td>
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<td>0.61</td>
</tr>
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**Surface Area Method**

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<th>Material</th>
<th>First Crack</th>
<th>Steady Onset</th>
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<tr>
<td>Meso-Ref</td>
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<td>0.63</td>
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