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Approximate Message Passing Reconstruction of Quantitative Acoustic Microscopy Images

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***Abstract*—A novel framework for compressive sensing (CS) data acquisition and reconstruction in quantitative acoustic microscopy (QAM) is presented. Three different compressive sensing patterns, adapted to the specifics of QAM systems, were investigated as an alternative to the current raster-scanning approach. They consist of diagonal sampling, a row random and a spiral scanning pattern and they can all significantly reduce both the acquisition time and the amount of sampled data. For subsequent image reconstruction, we design and implement an innovative technique, whereby a recently proposed approximate message passing (AMP) method is adapted to account for the underlying data statistics. A Cauchy *maximum a posteriori* (MAP) image denoising algorithm is thus employed to account for the non-Gaussianity of QAM wavelet coefficients.**

The proposed methods were tested retrospectively on experimental data acquired with a 250-MHz or 500-MHz QAM system. The experimental data were obtained from a human lymph node sample (250 MHz) and human cornea (500 MHz). Reconstruction results showed that the best performance is obtained using a spiral sensing pattern combined with the Cauchy denoiser in the wavelet domain. The spiral sensing matrix reduced the number of spatial samples by a factor of 2 and led to an excellent PSNR of 43.21 dB when reconstructing QAM speed-of-sound images of a human lymph node. These results demonstrate that the CS approach could significantly improve scanning time, while reducing costs of future QAM systems.

Index Terms – Quantitative Acoustic Microscopy, Compressive Sensing, Approximate Massage Passing, Cauchy distribution

I. Introduction

Although introduced more than 30 years ago, quantitative acoustic microscopy (QAM) is still a "new" imaging technology employed to investigate soft biological tissue at microscopic resolution by eliciting its mechanical property when irradiated with very high frequency ultrasound [1]. Specifically, by processing RF echo data, QAM yields two-dimensional (2D) quantitative maps of the acoustical and mechanical properties of soft tissues (*e.g.*, speed of sound, acoustic impedance, and acoustic attenuation). Therefore, QAM provides a novel contrast mechanism compared to histology photomicrographs and optical and electron microscopy images [4]. To date, our group and others have successfully used QAM to investigate a wide range of soft biological tissues such as liver samples, lymph nodes, retina, and even living cells [1]–[5]. Several of these recent studies were performed using QAM systems equipped with spherically focused single-element transducers having center frequencies of 250 MHz or 500 MHz which yielded 2D maps of acoustic properties with spatial resolutions of 7 and 4 μm, respectively [2], [3]. Currently, QAM requires a complete 2D raster scan of the sample to form images, thus yielding a large amount of RF data when using a conventional spatial sampling scheme (*e.g.*, 2 and 1 μm steps at 250 and 500 MHz, respectively). Likewise, sonography techniques exploiting ultrasound need to acquire considerable amount of data (thus significantly exceeding the Nyquist rate) in order to perform high resolution digital beamforming. Therefore, compressive sensing (CS) has been intensively studied as a breakthrough to overcome the limitation of contemporary technology [13].

From this perspective, this paper presents a novel approach to improve the efficiency of QAM RF data acquisition and reconstruction by developing a dedicated CS scheme.

Traditionally, statistical signal processing has been centered in its formulation on the hypotheses of Gaussianity and stationarity. This is justified by the central limit theorem and leads to classical least square approaches for solving various estimation problems. The introduction of various sparsifying transforms starting with the penultimate decade of the last century, together with the adoption of various statistical models that are able to model various degrees of non−Gaussianity and heavy−tails, have led to a progressive paradigm shift [7]. At the core of modern signal processing methodology sits the concept of sparsity. The key idea is that many naturally occurring signals and images can be faithfully reconstructed from a lower number of transform coefficients than the original number of samples (*i.e.* acquired according to Nyquist theorem) [8]. In this sense, CS could prove to be a powerful solution to decrease the amount of data in QAM and to accelerate the acquisition process at potentially no cost to image quality. In terms of reconstruction, most CS methods rely on l_1-norm

minimization using a linear programming algorithm. All these approaches do not exploit the true statistical distribution of the data and are motivated by the inability of the classical least-squares approach to estimate the reconstructed signal.

In this work, an approximate message passing (AMP)-based algorithm was designed to reconstruct QAM images from spatially undersampled measurements. AMP is a simplified version of MP (message passing) derived from belief propagation in graphical models [9], and is characterised not only by dramatically reduced convergence times but also by a reconstruction performance equivalent to l_p-based methods. AMP uses an iterative process consisting of a sparse representation-based image denoising algorithm performed at each iteration. Hence, selection of a robust denoiser and of the most efficient sparsifying basis are essential issues to address in order to achieve fast convergence and high recovery quality [10]. Our proposed AMP-based QAM imaging framework consists of two major modules: (i) In the data acquisition component of our system, we propose novel techniques for QAM data sampling, by choosing sensing matrices that simultaneously meet CS requirements and take into account the peculiarities of practical QAM acquisition devices, instead of. (ii) In the image reconstruction component, we design and test a wavelet domain AMP-based approach, which exploits underlying data statistics through the use of a Cauchy-based MAP algorithm[1].

The paper is structured as follows: Section II covers the essential, necessary background on QAM, CS and AMP. Section III introduces the main theoretical contributions of this work. Specifically, in Section III-A, we present the derivation of the wavelet-based Cauchy denoiser and in Section III-B we describe three different sensing patterns for QAM. Section IV compares the performance of our proposed method with that of existing CS reconstruction techniques, including previously proposed AMP algorithms. Finally, conclusions and future work directions are detailed in Section VI.

II. THEORETICAL BACKGROUND

A. Quantitative Acoustic Microscopy

In QAM, a high-frequency (*e.g.*, > 50 MHz), single-element, spherically-focused (*e.g.*, F-number < 1.3) transducer transmits a short ultrasound pulse and receives the RF echo signals reflected from the sample which consists of a thin section of soft tissue affixed to a microscopy slide (Fig. 1). The echo RF data is composed of two main reflections (S_1 and S_2 in Fig. 1): S_1 originates from the interface between the coupling medium (degassed saline) and the specimen and S_2 from the interface between the specimen and the glass substrate interface as illustrated in Fig. 1. At each scan location, the RF data is digitized, saved, and processed offline to yield values of speed of sound (c), acoustic impedance (z) and attenuation (α) [14]. Signal processing also requires the use of a reference signal obtained from a region devoid of sample (S_0 in Fig. 1). Briefly, the ratio of the Fourier transform of a sample signal, S and S_0, is computed and fit to a forward model to estimate the time of flight differences between S_1 and S_0 and S_2 and S_0. These time differences are used to estimate c in the sample as well as the tissue thickness (*i.e.*, d in Fig. 1) at that location. The forward model fit also provides the amplitude of S_1, which is used to estimate z of the sample. Finally, the amplitude of S_2, its frequency dependence, and the previously-estimated tissue thickness are used to estimate α [14]. The transducer is raster scanned and the values obtained at each scan location are then combined to form quantitative 2D parameter maps. Fig. 2 shows the working principle of QAM as well as the 500-MHz QAM system used in this

[1] An intial version of this algorithm was presented in [11], but the work therein was focused on natural images.

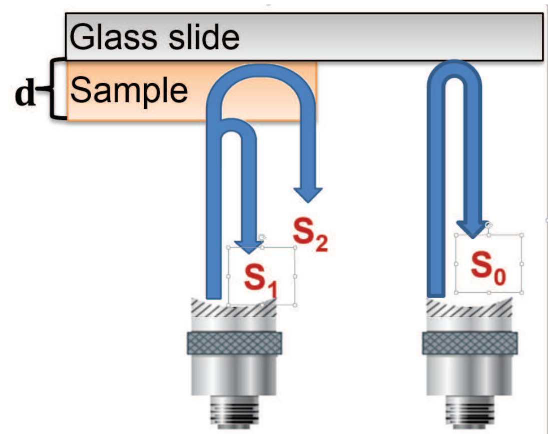

Fig. 1. Illustrative working principle of QAM: RF data from above a sample location is composed of two reflections while RF data from above glass slide is composed of only one reflection. Many QAM systems operate in the so called upside-down configuration, because holding the transducer from the top usually generate too much vibration at the tip of transducer creating blurring artifact in the reconstructed QAM images.

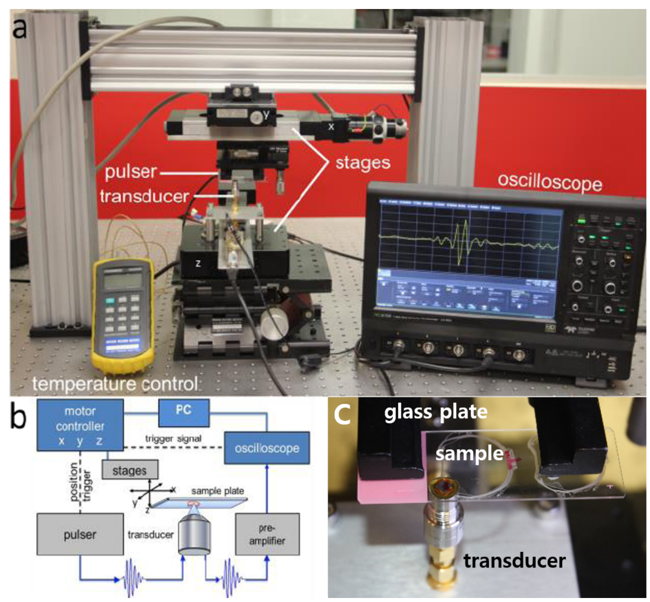

Fig. 2. (a) Photograph of the 500-MHz SAM system. (b) Block diagram of working principle. (c) Magnification of sample mounting and transducer. A eye bank eye sample is visible on the microscopy glass slide: Our QAM system does not currently employ a temperature controller, rather, we measure the coupling fluid temperature at the beginning and the end of the scanning, linearly interpolate between the two values, and use these values to estimate a speed of sound in water at each location. Typically, the variation of temperature is less than 0.5 degrees Celsius.

study (Fig. 1), namely the transducer and the thin sample affixed to a microscopy slide. Samples are obtained from fixed or frozen samples sectioned using a microtome or a cryotome. In the case of fixed samples, the paraffin is removed and the sample is rehydrated before imaging. In the case of frozen samples, the sample is thawed and rehydrated before imaging. These protocols are common and used in histopathology. Following QAM data acquisition, the samples can be stained and imaged using optical microscopy approaches and histology photomicrographs can easily be coregistered with QAM images. Therefore, successfully applying a CS approach to QAM acquisition could significantly reduce the amount of RF data recorded compared to conventional raster scanning without significantly degrading the quantitative 2D maps of acoustic properties. In this study, a new CS scheme is proposed for QAM and to test it, it was applied retrospectively to decimated 2D quantitative maps directly.

B. Compressive Sensing

CS is based on measuring a significantly reduced number of samples than what is dictated by the Nyquist theorem. Given a correlated image, the traditional transform-based compression method performs the following steps: (i) acquires all N samples of the signal, (ii) computes a complete set of transform coefficients (*e.g.*, DCT or wavelet), (iii) selectively quantizes and encodes only the K≪N most significant coefficients. This procedure is highly inefficient, because a significant proportion of the output of the analogue-to-digital conversion process ends up being discarded. CS is concerned with sampling signals more parsimoniously, acquiring only the relevant signal information, rather than sampling followed by compression. The main hallmark of this methodology is that, given a compressible signal, a small number of linear projections, directly acquired before sampling, contain sufficient information to effectively perform the processing of interest (signal reconstruction, detection, classification, etc). In terms of signal approximation, Candès *et al.* [8] and Donoho [16] have demonstrated that if a signal is K-sparse in one basis (meaning that the signal is exactly or approximately represented by K elements of this basis), then it can be recovered from $M = \mathrm{cst} \cdot K \cdot log(N/K) \ll N$ fixed (non-adaptive) linear projections onto a second basis, called the measurement basis, which is incoherent with the sparsity basis, and where $\mathrm{cst} > 1$, is a small overmeasuring constant. The CS measurement model is

$$\mathbf{y} = \mathbf{\Phi x} + \mathbf{n}, \tag{1}$$

where $\mathbf{y} \in \mathbb{R}^M$ is the measurement vector, $\mathbf{x} \in \mathbb{R}^N$ is the signal to be reconstructed, $\mathbf{\Phi} \in \mathbb{R}^{M\times N}$ is the measurement matrix and $\mathbf{n} \in \mathbb{R}^M$ is an additive white Gaussian noise.

In terms of reconstruction, using the M measurements in the first basis and given the K-sparsity property in the other basis, the original signal can be recovered by taking a number of different approaches. The majority of these approaches solve constrained optimization problems. Commonly used approaches are based on convex relaxation (Basis Pursuit [8]), non-convex optimization (re-weighted l_p minimization [17]) or greedy strategies (Orthogonal Matching Pursuit (OMP) [18]). As another alternative, iterative thresholding approaches to CS recovery problem have attracted significant interest, owing to faster reconstruction than what can be achieved by convex optimization. [19], [20] proved that correct solution could be obtained via soft or hard thresholding of observations measured from sparse signals.

C. Approximate Message Passing Reconstruction

In the context of CS, AMP reconstructs an original image from a reduced number of linear measurements by performing elementwise denoising at each iteration. Indeed, the AMP algorithm can be interpreted as recursively solving an image denoising problem. Specifically, at each AMP iteration, one observes a noise perturbed original image. Reconstructing the image amounts to successive noise cancellations until the noise variance decreases to a satisfactory level. The algorithm can be succinctly summarised mathematically through the following two steps:

$$\mathbf{x}^{t+1} = \eta_t\left(\mathbf{\Phi}^T\mathbf{z^t} + \mathbf{x^t}\right), \tag{2}$$

$$\mathbf{z^t} = \mathbf{y} - \mathbf{\Phi x^t} + \frac{1}{\delta}\mathbf{z^{t-1}}\langle\eta'_{t-1}\left(\mathbf{\Phi}^T\mathbf{z^{t-1}} + \mathbf{x^{t-1}}\right)\rangle, \tag{3}$$

where $\mathbf{x}, \mathbf{y}, \mathbf{z}$ and δ denote a sparse signal, observation, residual and undersampling ratio (M/N) respectively. $\eta(\cdot)$ is a function that represents the denoiser, $\eta'(\cdot)$ is its first derivative and $\langle\mathbf{x}\rangle = \frac{1}{N}\sum_{i=1}^{N}(x_i)$. The superscript t represents the iteration number and $(\cdot)^T$ is the classical conjugate transpose notation. Given $\mathbf{x} = \mathbf{0}$ and $\mathbf{z} = \mathbf{y}$ as an initial condition, the algorithm iterates sequentially (2) and (3) until satisfying a stopping criterion or reaching a pre-set iteration number. The last term of the right hand side in (3) is referred to as the Onsager reaction term and is also acknowledged to contribute to balancing the sparsity-undersampling tradeoff [9], [21].

An extended wavelet-based AMP system can be generated by integrating a wavelet transform (denoted by W) into (2) and (3) using the following transformation.

$$\mathbf{y} = \mathbf{\Phi}\underbrace{W^{-1}\boldsymbol{\theta}_\mathbf{x}}_{\mathbf{x}} + \mathbf{n}, \tag{4}$$

where W^{-1} denotes the inverse wavelet transform, W and $\theta_\mathbf{x}$ becomes the sparse representation of $\mathbf{x}$ within wavelet domain. Introducing $\mathbf{\Theta}$ as the new notation for $\mathbf{\Phi}W^{-1}$, we get the following expressions:

$$\theta_\mathbf{x}^\mathbf{t+1} = \eta_t\left(\mathbf{\Theta}^\mathbf{T}\mathbf{z^t} + \theta_\mathbf{x}^\mathbf{t}\right), \tag{5}$$

$$\mathbf{z^t} = \mathbf{y} - \mathbf{\Theta}\theta_\mathbf{x}^\mathbf{t} + \frac{1}{\delta}\mathbf{z^{t-1}}\left\langle\eta'_{t-1}\left(\mathbf{\Theta}^\mathbf{T}\mathbf{z^{t-1}} + \theta_\mathbf{x}^\mathbf{t-1}\right)\right\rangle. \tag{6}$$

The subsequently defined denoising algorithms seek to denoise the elements of $\theta_\mathbf{q}^\mathbf{t} = \mathbf{\Theta}^\mathbf{T}\mathbf{z^t} + \theta_\mathbf{x}^\mathbf{t}$ corresponding to the contaminated wavelet coefficients. To simplify the following notation, the ith element of $\theta_\mathbf{q}^\mathbf{t}$ is defined as $\theta_{\mathbf{q},i}^t = v$ and the ith element

of the denoised output $\theta_{\mathbf{x}}^{\mathbf{t+1}}$ is defined as $\theta_{\mathbf{x},i}^{t+1} = \hat{w}$ (a denoised estimate of the true coefficient w).

The most important design consideration is arguably the choice of the shrinkage (denoising) function, η, in (5) above. In the following, we introduce two previsouly defined functions [6], [21], which will be later used for comparison purpose within our experimental results in Section IV-A.

Soft Threshold (ST) denoiser:

$$\begin{aligned} \hat{w} = \eta(v) &= \text{sign}(v)(|v| - \tau) \cdot \mathbb{1}_{(|v|>\tau)}, \\ \eta'(v) &= \mathbb{1}_{(|v|>\tau)}, \end{aligned} \tag{7}$$

where $\mathbb{1}_{(\cdot)}$ is the indicator function. The threshold τ is defined as the M^{th} largest magnitude value of $\theta_{\mathbf{q}}^{\mathbf{t}}$ [9].

Amplitude-scale-invariant Bayes Estimator (ABE) denoiser:

$$\begin{aligned} \hat{w} = \eta(v) &= \frac{(v^2 - 3\sigma^2)_+}{v}, \\ \eta'(v) &= \mathbb{1}_{(v^2>3\sigma^2)} \cdot \left(1 + 3\left(\frac{\sigma}{v}\right)^2\right), \end{aligned} \tag{8}$$

where σ^2 is the noise variance at iteration t and $(\cdot)_+$ is the right handed function where $(u)_+ = 0$ if $u \le 0$ and $(u)_+ = u$ if $u > 0$.

As far as the CS reconstruction of conventional ultrasound images is concerned, the denoiser in (8) was shown to achieve better performance than IRLS and l_p programming [29]. Therefore, we hypothesize that ABE should also be a successful criterion for QAM images and consequently, we shall use it for benchmarking our method. Fig. 3 illustrates the behavior of the denoising function for four different denoisers, of which ABE and the Cauchy-based denoisers that is introduced in the subsequent section can be regarded as a compromise between Soft-thresholding and Hard-thresholding [24]. The labels on the horizontal and vertical axes correspond to corrupted wavelet coefficient and their denoised version respectively. Subscript i represents the index of each element which implies element-wise denoising, as stated before.

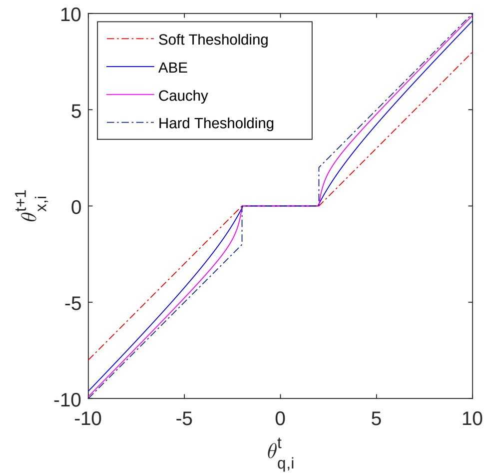

Fig. 3. The comparison of behavior among four different denoisers.

III. Cauchy-AMP for Compressed QAM Imaging

This section describes the key features of wavelet-based Cauchy-AMP together with the practical sensing patterns as a novel approach for QAM CS reconstruction.

A. *Wavelet based Cauchy-AMP*

Wavelet coefficients provide a sparse representation for natural images. In addition, they can be accurately modelled using heavy tailed distributions such as the $\alpha-$stable distribution [22], [23]. The Cauchy distribution is a special case of the $\alpha-$stable family which not only has a heavy tailed form but has a compact analytical probability density function given by [11]:

$$P(w) = \frac{\gamma}{w^2 + \gamma^2}, \tag{9}$$

where w and γ are the wavelet coefficient value and the dispersion parameter (controlling the spread of the distribution) respectively. Given (9), a maximum *a posteriori* (MAP) estimator method (10) can lead to the derivation of explicit formulae (14) estimating a clean wavelet coefficient w from an observed coefficient observation v contaminated with additive Gaussian noise (*i.e.* $n = v - w$ with noise variance σ^2) [12].

$$\hat{w} = arg \max_{w} P_{w|v}(w|v). \tag{10}$$

The posterior probability $P_{w|v}(w|v)$ can be expressed as (11) by Bayes' theorem

$$P_{w|v}(w|v) = \frac{P_{v|w}(v|w)P_w(w)}{P_v(v)}. \tag{11}$$

Assuming $P_{v|w}(v|w) \sim N(0, \sigma^2)$, the logarithmic form of (10) is given in (12) which is mathematically more intuitive. The evidence $P_v(v)$ is constant for all inputs and therefore can be ignored.

$$\hat{w}(v) = arg \max_{w} \left[-\frac{(v-w)^2}{2\sigma^2} + log\left(\frac{\gamma}{w^2+\gamma^2}\right)\right]. \tag{12}$$

To find the solution to (12), take the first derivative of the terms in the bracket relative to w and set to zero:

$$\hat{w}^3 - v\hat{w}^2 + (\gamma^2 + 2\sigma^2)\hat{w} - \gamma^2 v = 0. \tag{13}$$

Using Cardano's method, the estimate of w can be found in (14) of which first derivative is (15).

$$\hat{w} = \eta(v) = \frac{v}{3} + s + t, \tag{14}$$

$$\hat{w}' = \eta'(v) = 1/3 + s' + t', \tag{15}$$

where s and t are values determined by v and σ^2 iteratively updated at each iteration together with a constant value γ; σ^2

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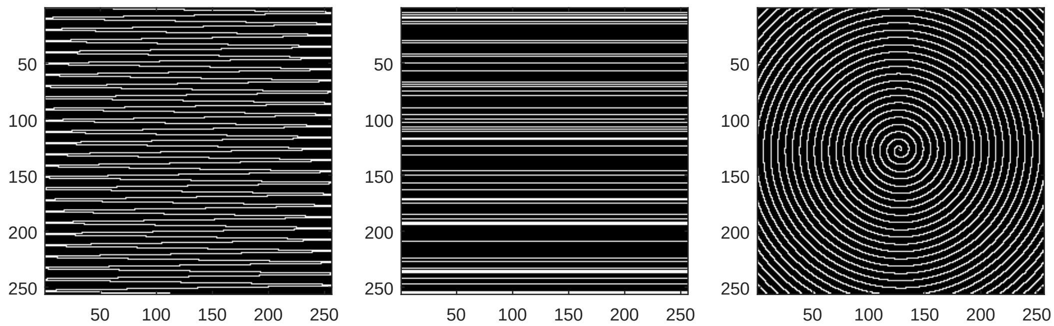

(a) (b) (c)

Fig. 4. The proposed three different types of sampling masks, (a) Diagonal, (b) Row random and (c) Spiral.

is estimated as the variance of the $\mathbf{z}$ vector defined in (6). s and t are defined as:

$$\begin{aligned} s &= \sqrt[3]{\tfrac{q}{2}+dd}, \quad t = \sqrt[3]{\tfrac{q}{2}-dd}, \\ dd &= \sqrt{p^3/27+q^2/4}, \\ p &= \gamma^2+2\sigma^2-v^2/3, \\ q &= v\gamma^2+2v^3/27-(\gamma^2+2\sigma^2)v/3. \end{aligned} \tag{16}$$

s' and t' are found as follows:

$$\begin{aligned} s' &= \frac{q'/2+dd'}{3(q/2+dd)^{(2/3)}}, \quad t' = \frac{q'/2-dd'}{3(q/2-dd)^{(2/3)}}, \\ dd' &= \frac{p'p^2/9+q'q/2}{2dd}, \\ p' &= -2v/3, \\ q' &= -2\sigma^2/3+2\gamma^2/3+2v^2/9. \end{aligned} \tag{17}$$

TABLE I
NUMERICAL RESULTS OF RECOVERY QUALITY (GAUSSIAN RANDOM SENSING)

Method	SSIM		PSNR (dB)	
	Lymph Node	USAF	Lymph Node	USAF
Cauchy	0.841	0.429	39.08	37.54
ABE	0.811	0.418	39.01	37.45
ST	0.724	0.380	38.41	35.95
IRLS	0.698	0.333	34.97	32.85
L1LS	0.457	0.290	32.14	31.30

TABLE II
THE COMPARISON OF EXECUTION TIME: THE AVERAGED VALUES OVER 30 TRIALS

Method	Runtime (secs)	
	Lymph Node	USAF
Cauchy	3.32	3.47
ABE	2.86	3.00
ST	2.82	2.93
IRLS	62.88	333.61
L1LS	4.10	6.88

B. Practical sensing patterns for QAM

Theoretically, optimal sensing matrices based on randomness are impractical for QAM data acquisition because RF data are typically acquired continuously as the motor stages are moved. Therefore, this paper investigates three practical sensing schemes, which can be easily implemented using servo motors. The diagonal sensing schemes raster scans oblique lines using a constant predefined angle which is used to vary the measurement rate, *i.e.*, a smaller angle leads to denser sampling. The row random sensing pattern is a naive but practical attempt to preserve randomness. Data are also collected using a practical raster scanning approach, but only on randomly selected rows using the random number generator (rng) of Matlab. An input value for rng is used to dictate the measurement rate. Finally, the spiral sensing scheme is also a practical sensing scheme which originates in the center of area to be sampled and spreads out following a spiral pattern. The pace of the spreading is parametrized and used to prescribe the measurement rate. For comparison purposes, the spiral pattern was truncated to cover the same square area as the other two patterns. In actual experiments, the scanned area by the spiral pattern would consist approximately of a circle passing through the four corners of the square.

Fig. 4 illustrates all sensing schemes used to sample data from a target composed of 256 $\times$ 256 pixel. A measurement rate of 20% is shown for all three schemes and the white pixels corresponds to the area to be spatially sampled.

IV. SIMULATION RESULTS

Two different sets of experiments have been conducted and results are reported in Sections IV-A and IV-B. The objective of the first set of experiments was to evaluate the performance of the proposed Cauchy-AMP algorithm. The second set of experiments shows the interest of the proposed sampling schemes in QAM and the ability of Cauchy-AMP algorithm to recover high quality images from the resulting under-sampled data. In addition to visual inspection, the peak signal to noise ratio (PSNR) and the structural similarity (SSIM) index [32] were used to assess the quality of the reconstructed images by comparing them to the corresponding fully-sampled quantitative maps.

A. Simulation A: reconstruction results with random sensing schemes

The objective of this subsection is to validate the efficiency of the proposed Cauchy-AMP algorithm in comparison to al-

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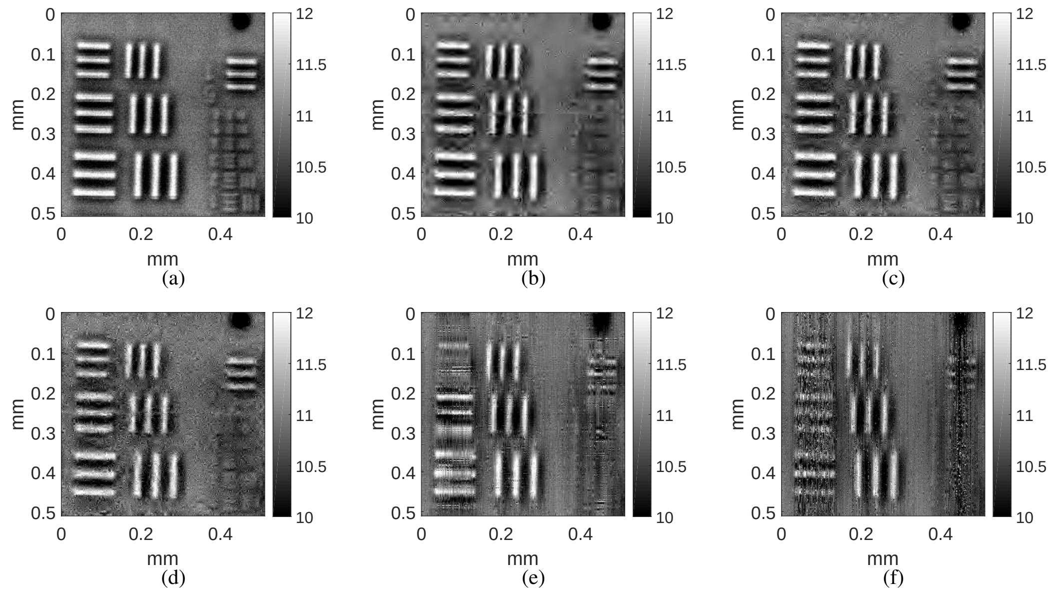

Fig. 5. (a) Fully-sampled impedance (*MRayl*) map estimated from RF data acquired on the USAF 1951 resolution test chart, reconstruction results from Gaussian random measurements for a measurement ratio of 0.25 with (b) proposed Cauchy-AMP, (c) ABE-AMP, (d) ST-AMP, (e) IRLS and (f) L1LS algorithms.

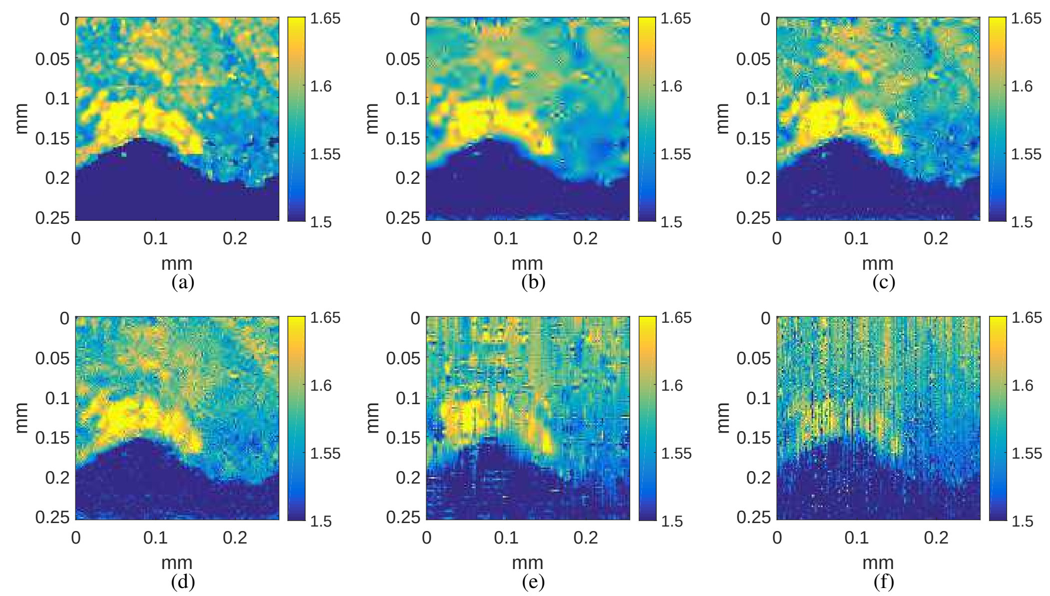

Fig. 6. (a) Human lymph node's fully-sampled impedance (*MRayl*) map representing a reconstruction results from Gaussian random measurements for a measurement ratio of 0.25 with (b) proposed Cauchy-AMP, (c) ABE-AMP, (d) ST-AMP, (e) IRLS and (f) L1LS algorithms.

ternative methods, previously proposed for CS reconstruction. Two of these were described in Section II-C and, while also AMP-based, they use ST and ABE as shrinkage functions in eq. (7) and (8). In addition, we also compare to conventional CS reconstruction algorithms, including the L1LS method and the IRLS algorithm for l_1-norm and ℓ_p minimisation, respectively. These are succinctly outlined in the following:
L1LS (l_1-regularized Least Squares):
This l_1 based algorithm solves an optimization problem of the form

$$\min \|\Phi x - y\|^2 + \lambda \sum_{i=1} |x_i|, \tag{18}$$

where λ, a positive number, is a regularisation parameter; in this work we adopted, by cross validation, 0.01 as the value of λ.

IRLS (iteratively reweighed least squares):

$$\hat{x} = \min_x \|x\|_p \quad \text{subject to} \quad y = \Phi x. \tag{19}$$

When it comes to estimating a sparse vector characterised by an α-stable distribution, (19) leads to solving an l_p minimisation problem. Thus, in order to choose the optimum value of p, we employed the approach described in [30]. This approach was found to be superior to existing l_p solvers when applied to CS reconstruction of conventional B-mode images.
The incoherence between the sensing matrix and the sparsifying transform is important in CS applications. Hence, in order to fairly evaluate the performance of the reconstruction algorithms, the results in this section are obtained with two random sensing matrices widely used in the CS literature:

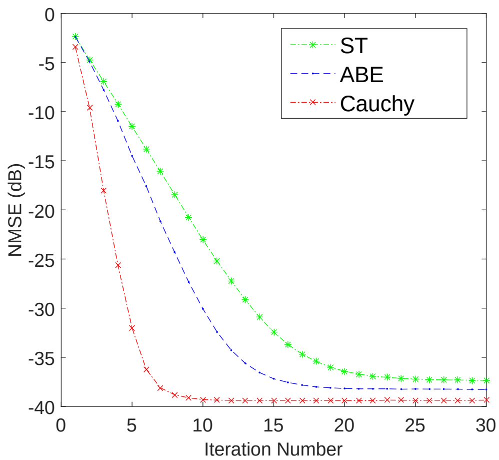

Fig. 7. The comparison of NMSE according to iteration number for three AMP recovery methods: NMSE valuse are averaged over 30 simulated QAM images.

image projections on random Gaussian vectors and point-wise multiplication with Bernoulli vectors formed by uniformly random distributed zeros and ones.

Two experimental data volumes were used, from which impedance maps were estimated point-wise using the method in [14]. The first was acquired from a spatial-resolution target consisting of small bars of known width and spacing. Because the chrome used to form those bars is deposited using photolithography, the metal thickness (*i.e.*, ~ 0.12 μm) is much smaller than the wavelength at 250 MHz (*i.e.*, ~ 6 μm) and therefore only an effective acoustic impedance (z_{eff}) can be estimated. The amplitudes of the reflected signal (A) and the reference signal (B) were used to calculate z_{eff} using the following equation from the pressure reflection law [15]:

$$z_{eff} = z_w \frac{(1 + R_{ref}\frac{A}{B})}{(1 - R_{Ref}\frac{A}{B})}, \tag{20}$$

where z_w is the known acoustic impedance of water and R_{ref} is the pressure reflection coefficient between water and glass slide:

$$R_{ref} = \frac{z_g - z_w}{z_g + z_w}, \tag{21}$$

where z_g is the known acoustic impedance of the glass slide. The second data volume was acquired from a 12-μm thick section obtained from a lymph node excised from a colorectal cancer patient using the 250-MHz QAM system. For both Gaussian and Bernoulli measurement matrices, the reconstruction results correspond to a measurement rate of 25%, *i.e.*, the ratio between the number of CS measurements and the number of pixels in the fully sampled QAM image.

1) Gaussian random measurements: Figs. 5 and 6 illustrate the impedance images obtained with the five reconstruction algorithms from Gaussian random measurements. It highlights that IRLS and L1LS methods severely distorted the fully-sampled image compared to the AMP-based algorithms. By closely comparing the AMP-based methods, one may remark

TABLE III
NUMERICAL RESULTS OF RECOVERY QUALITY (BERNOULLI RANDOM SENSING)

Method	SSIM		PSNR (dB)	
	Lymph Node	USAF	Lymph Node	USAF
Cauchy	0.851	0.424	38.72	34.56
ABE	0.837	0.417	38.56	34.33
ST	0.815	0.415	37.88	34.09

that Cauchy-AMP shows a tendency of noise removal with a slightly excessive smoothing effect, whereas ST-AMP and ABE-AMP suffer from several reconstruction artefacts. Table I regroups the PSNR and SSIM values corresponding to the results in Figs. 5 and 6. Additionally, Table II provides the runtime of the five methods, averaged over 30 trials. All the algorithms were implemented in Matlab R2014a environment and executed on a desktop computer equipped with a 2.6GHz Intel(R) CoreTM $i7-6500C$ processor with 8GB RAM.

AMP algorithms outperform the two conventional recovery approaches IRLS and L1LS. Particularly, Cauchy-AMP yields the most accurate results compared to its AMP counterparts, at the cost of an execution time marginally higher than ABE- and ST-AMP. The execution time increase per iteration is explained by the number of parameters to be estimated during the denoising process. Indeed, Cauchy-AMP requires the estimation of an extra parameter compared to ST- and ABE-AMP, *i.e.* the dispersion parameter that determines the spread of the Cauchy distribution. However, the extra computational cost per iteration is significantly mitigated by the faster convergence of Cauchy-AMP as revealed in Fig. 7.

2) Bernoulli random measurements: The above overall evaluation confirms that AMP-based algorithms are the most promising QAM recovery methods from under-sampled data. Nevertheless, measurements obtained by linear projections on Gaussian vectors are not of practical use in QAM. As explained previously, QAM data is acquired point-wise by raster scanning the sample. Thus, Bernoulli random measurements corresponding to random spatial positions are further adapted to QAM acquisition system. Therefore, the three AMP-based methods are tested in this section on the same image used previously but on Bernoulli randomly sampled data. Similar to the previous results, the proposed Cauchy-AMP outperforms ABE- and ST-AMP algorithms. The three reconstructed images are shown in Figs. 8 and 9. The corresponding quantitative results are regrouped in Table III.

B. Simulation B: reconstruction results with sensing schemes dedicated to QAM

The results shown in the previous section proved the superiority in reconstructing QAM images of the proposed Cauchy-AMP algorithm against four well-established methods. However, Gaussian random measurements are impractical for QAM data acquisition. Similarly and although technically possible, it would be inefficient to move the transducer to transmit and receive ultrasound signals at spatial locations following a Bernoulli random measurements. Therefore, in this second set of simulations, the three AMP-based algorithms

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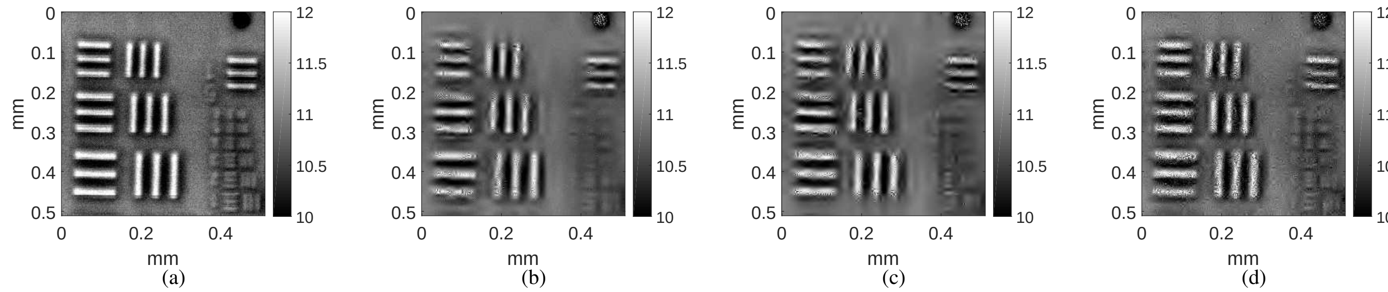

Fig. 8. (a) Fully-sampled impedance (*MRayl*) map estimated from RF data acquired on the USAF 1951 resolution test chart, reconstruction results from Bernoulli random measurements for a measurement ratio of 0.25 with (b) proposed Cauchy-AMP, (c) ABE-AMP, (d) ST-AMP algorithms.

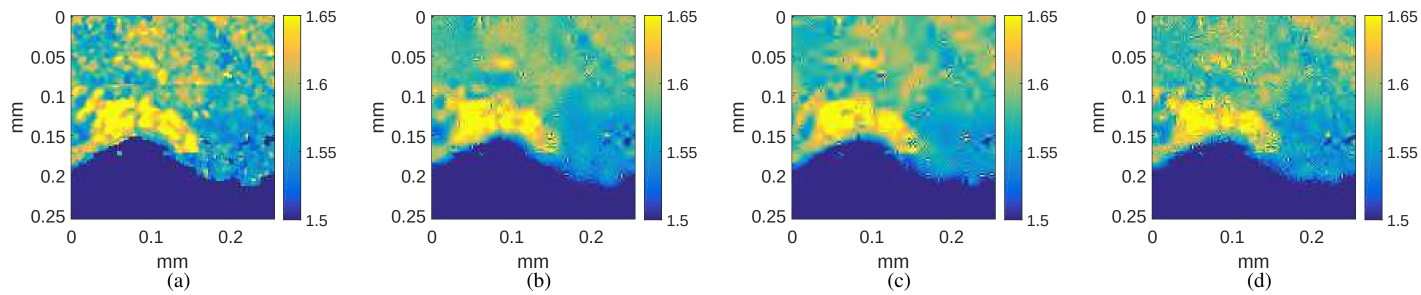

Fig. 9. (a) Fully-sampled impedance (*MRayl*) map representing a reconstruction results from Bernoulli random measurements for a measurement ratio of 0.25 with (b) proposed Cauchy-AMP, (c) ABE-AMP, (d) ST-AMP algorithms.

are employed to assess the relevance of the practical sensing patterns proposed in this study (see Section III-B) for QAM imaging.

The simulations used experimental results obtained from three real QAM maps. The first map corresponds to the speed of sound (SoS) map obtained from a human cornea sample using the 500-MHz QAM system. The two other maps are SoS and impedance maps obtained using the 250-MHz QAM system on a human lymph node thin section obtained from a colorectal cancer patient. The fully sampled images correspond to standard raster scanning at conventional spatial scanning frequencies, resulting into a pixel size of 1 μm per 1 μm and respectively of 2 μm per 2 μm for the 500 MHz and 250 MHz data.

All the AMP-algorithm investigations were performed using measurement ratios ranging from 20% to 60% of the data obtained using the conventional raster scanning approach. Fig. 10 displays the resulting PSNR values and permits comparing the QAM image reconstruction quality between the three proposed sensing patterns and the three AMP-based reconstruction algorithms. Blue regions in these images were not included in quantitative analyses because they were devoid of tissues. Independent of the image or algorithm under consideration, results indicate that the spiral pattern always provided the highest PSNR, followed by the diagonal pattern. Figs. 11, 12 and 13 show the fully-sampled images and the ones recovered by the three algorithms from data generated with the three considered patterns for a measurement rate of 40%. Also for the sake of the quantitative evaluation corresponding to the figures, the numerical results are in the Table IV offered. Overall, visual inspections of these images are consistent with the results shown in Fig. 10, the spiral pattern provide the best result and the quality of the reconstructions improves with measurement ratio. The images obtained with a measurement ratio of 40%, *i.e.* Figs. (11, 12, 13) illustrate nicely the relative performance of each tested sensing pattern. Fig. 10 reveals that Cauchy denoising provides better PSNR values. The corresponding 2D maps are shown in (b)-(d) of Figs. (11, 12, 13). The row random pattern results shows many artifacts appearing as "transverse" lines. In contrast, the spiral and diagonal sensing patterns do not contain any visually-apparent artifacts. In order to determine which of these two sensing patterns performs better for QAM, one can arguably see in Figs. 11-13 that the dense yellow area are better reconstructed using the spiral than the diagonal sensing pattern. This visual assessment is consistent with the quantitative results shown in Fig. 10 and Table IV. Another potential benefit of spiral pattern resides in significantly reduced scanning time. QAM estimation time is typically less important than QAM data acquisition time because tissue properties may change during scanning. Nevertheless, while the proposed AMP approach significantly decreases scanning time, it turns out that it also significantly decreases image formation time, because QAM parameter estimation is done independently on each RF line and is much more time consuming than AMP (cf. Table II). For example, in the case of the 40% spiral, scanning time is reduced by more than 80% because in conventional raster scanning most of the time is spent accelerating and decelerating in each scan line, whereas the spiral is a smooth continuous curve which can be scanned at almost constant speed with servo motors. In addition, initial parameter estimation time is also reduced by 60% prior to the application of the AMP algorithm. The raster scanning and parameter estimation times for the lymph node example (Fig. 12 and Fig. 13) were approximately 20 and 15 minutes. The 40% spiral AMP approach would reduce these times to approximately 4 and 8 minutes. In conclusion, these sets of simulations reveal that combining a spiral sensing pattern with a measurement ratio of 40%, and a Cauchy-AMP

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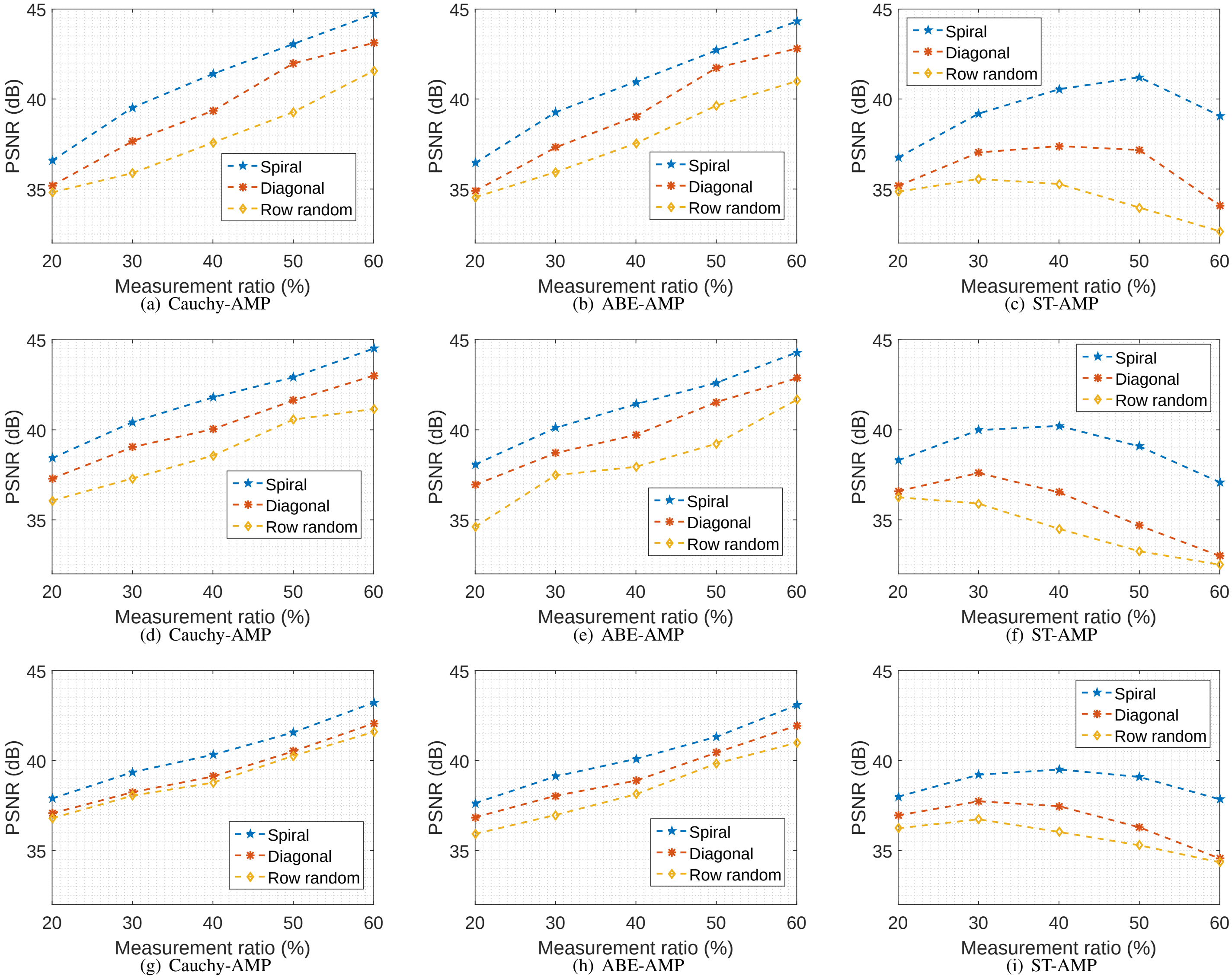

Fig. 10. PSNR results as a function of the measurement rate, the sensing pattern (diagonal, random rows or spiral) and recovery algorithm (proposed Cauchy-AMP, ABE-AMP and ST-AMP):(a) Cauchy, (b) ABE and (c) ST of Human cornea at 500 MHz of SOS mode. (d) Cauchy, (e) ABE and (f) ST of Human lymph node at 250 MHz of SOS mode. (g) Cauchy, (h) ABE and (i) ST of Human lymph node at 250 MHz of impedance mode.

recovery is the best compromise between a practical spatial sampling patten easily implementable with servo motors and image reconstruction quality for QAM imaging.

However in three graphs (right column) corresponding to ST-AMP of Fig. 10, intractable problems are found. To date researches associated with CS recovery normally have been reporting that the relationship between recovery quality and measurement ratio is a monotonically increase or decrease within usually simulated range. By contrast, ST-AMP shows unfamiliar results. Indeed CS has been constructed on the premise of sensing matrices satisfying mathematical completeness such as RIP and incoherence to ensure perfect recovery of sparse signals. Nevertheless, since this work prioritized the aspect of practical implementation of sensing strategy, the proposed sensing patterns unavoidably followed deterministic sensing trajectories rather than randomness dominating CS sensing arena owing to meeting essential conditions stated above [34]. From this perspective, further study will focus on the development of practical sensing schemes retaining the pertinent properties of random matrices [35].

V. CONCLUSIONS

In this paper, we introduced a new framework for compressive sampling reconstruction of QAM images together with associated sampling patterns. We proposed and tested three compressive sampling measurement matrices, with a view of reducing both acquisition time and the amount of samples required, while taking into account the constraints imposed by the design of current experimental QAM systems. Specifically, we assessed the relative merits of diagonal sampling, row random sampling and spiral scanning as underlying patterns in designing a CS measurement matrix. We adopted an approximate message passing strategy for the image reconstruction component of our framework, owing to its similarity to l_p minimisation. In particular, in the multiscale wavelet domain, we employed a Cauchy-based MAP estimation algorithm

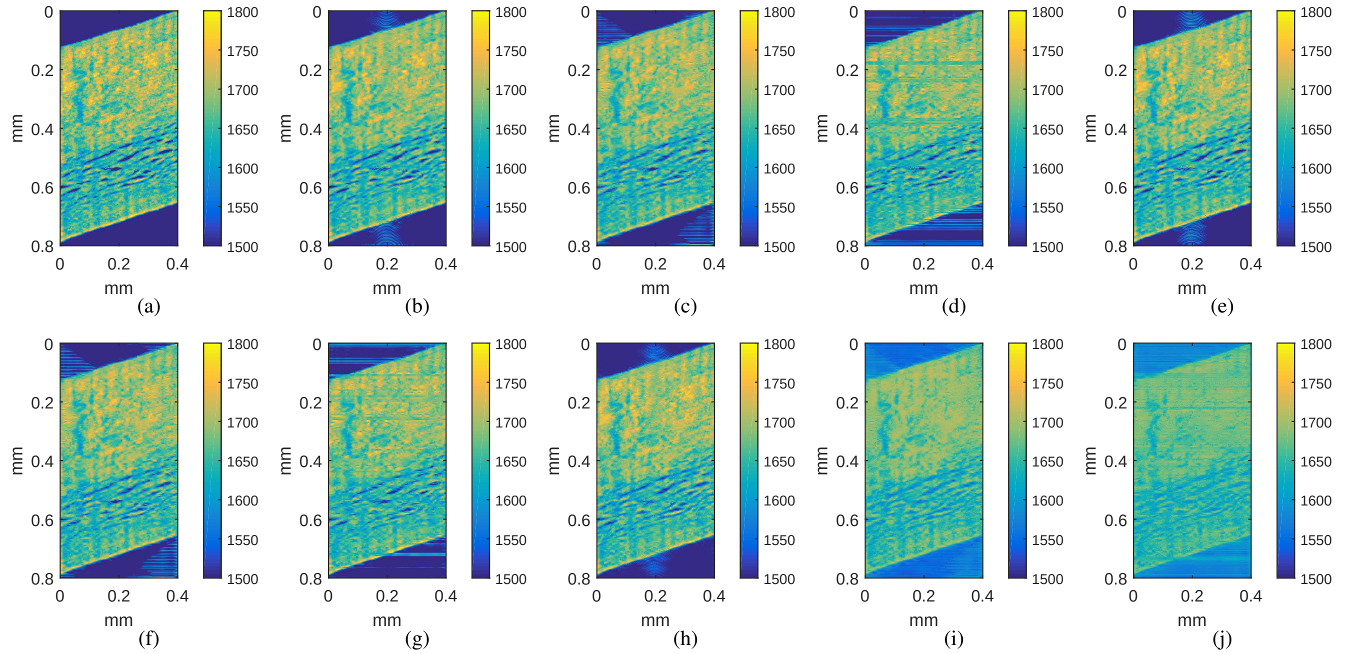

Fig. 11. Reconstruction results of SoS (m/s) map estimated from human cornea data acquired at 500 MHz: (a) original fully sample data at pixel resolution of 1 μm per 1 μm, (b-d) reconstructed images with the proposed Cauchy-AMP algorithm for spiral, diagonal and row random sampling patterns, (e-g) reconstructed images with ABE-AMP algorithm for spiral, diagonal and row random sampling patterns, (h-j) reconstructed images with ST-AMP algorithm for spiral, diagonal and row random sampling patterns. All the results correspond to a measurement ratio of 40%.

TABLE IV
NUMERICAL RESULTS OF RECOVERY QUALITY FOR THE RECONSTRUCTED IMAGES SHOWN IN FIGS. 11, 12 AND 13

Image	Method	SSIM			PSNR		
		SPIRAL	DIAGONAL	Y RANDOM	SPIRAL	DIAGONAL	Y RANDOM
Conear 500MHz (SoS)	Cauchy	0.530	0.458	0.415	41.40	39.35	37.58
	ABE	0.509	0.435	0.393	40.97	39.03	37.54
	ST	0.502	0.373	0.306	40.54	37.39	35.28
Lymph Node 250MHz (SoS)	Cauchy	0.445	0.388	0.342	41.80	40.04	38.57
	ABE	0.438	0.374	0.323	41.42	39.72	37.95
	ST	0.418	0.351	0.301	40.22	34.50	36.53
Lymph Node 250MHz (Impedance)	Cauchy	0.911	0.884	0.868	40.32	39.12	38.27
	ABE	0.907	0.878	0.864	40.09	38.89	38.13
	ST	0.896	0.868	0.859	39.51	37.47	36.04

to perform the image denoising step required by an AMP algorithm.

We tested our methods in comparison with various compressive image reconstruction algorithms, when applied to QAM data. Our results showed improved performance both with respect to alternative AMP techniques that use different denoising strategies as well as to other, more standard, approaches to CS reconstruction, which employ l_1-norm, or l_p minimisation.

The results of this study could prove invaluable in QAM imaging. CS has the potential to yield significantly improved scan times, smaller datasets, faster image formation without degrading image quality. Moreover, CS approaches would reduce experimental challenges currently encountered in QAM imaging. For example, the spiral sampling approach could be implemented on cheap, potentially less precise, servo motors. In addition, reducing scan time would reduce changes that the tissue properties may suffer during scan and would limit temperature variations, particularly in the coupling medium, which can greatly effect speed of sound estimates. Therefore, CS approaches could potentially bring about a new generation of QAM systems which would be lower costs and simpler to use. Finally, the study of dominant factors having an effect on the convergence rate of the proposed method is definitely an interesting study that will be part of our future work.

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REFERENCES

[1] M. F. Marmor, H. K. Wickramasinghe, and R. A.Lemons, "Acoustic microscopy of the human retina and pigment epithelium," Invest. Ophthalmol. Vis. Sci., vol. 16, no. 7, pp. 660-666, Jul. 1977.

[2] D. Rohrbach, H. Lloyd, R. Silverman, and J. Mamou, "Fine-resolution maps of acoustic properties at 250-MHz of unstained fixed murine retinal layers," The Journal of the Acoustical Society of America, 137(5), pp.EL381-EL387, May. 2015.

[3] S. Irie, K. Inoue, K.Yoshida, J. Mamou, K. Kobayashi, H. Maruyama, and T. Yamaguchi, "Speed of sound in diseased liver observed by scanning acoustic microscopy with 80-MHz and 250-MHz," The Journal of the Acoustical Society of America, 139(1), pp.512-519. Jan. 2016.

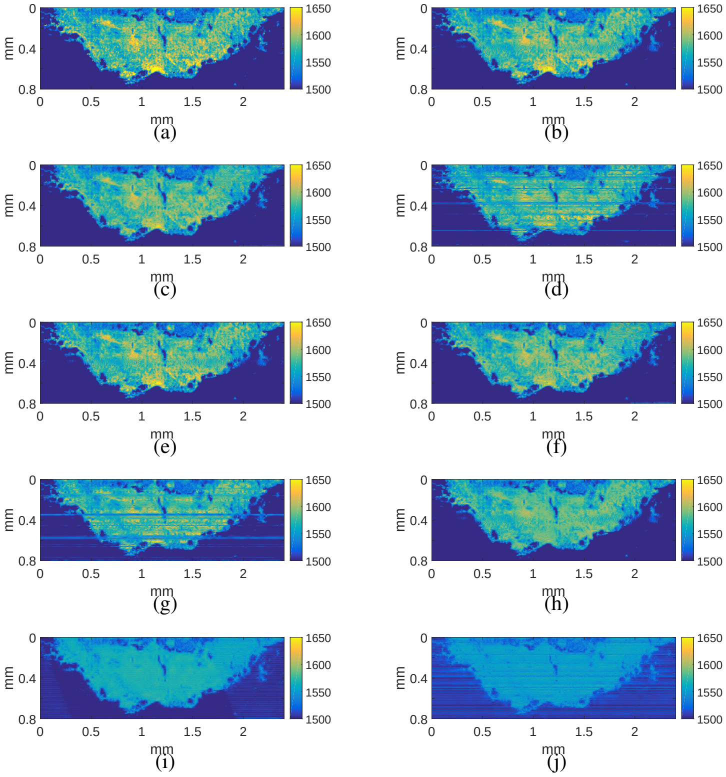

Fig. 12. Reconstruction results of SoS (m/s) map estimated from human lymph node data acquired at 250 MHz: (a) original fully sample data at pixel resolution of 2 μm per 2 μm, (b-d) reconstructed images with the proposed Cauchy-AMP algorithm for spiral, diagonal and row random sampling patterns, (e-g) reconstructed images with ABE-AMP algorithm for spiral, diagonal and row random sampling patterns, (h-j) reconstructed images with ST-AMP algorithm for spiral, diagonal and row random sampling patterns. All the results correspond to a measurement ratio of 40%.

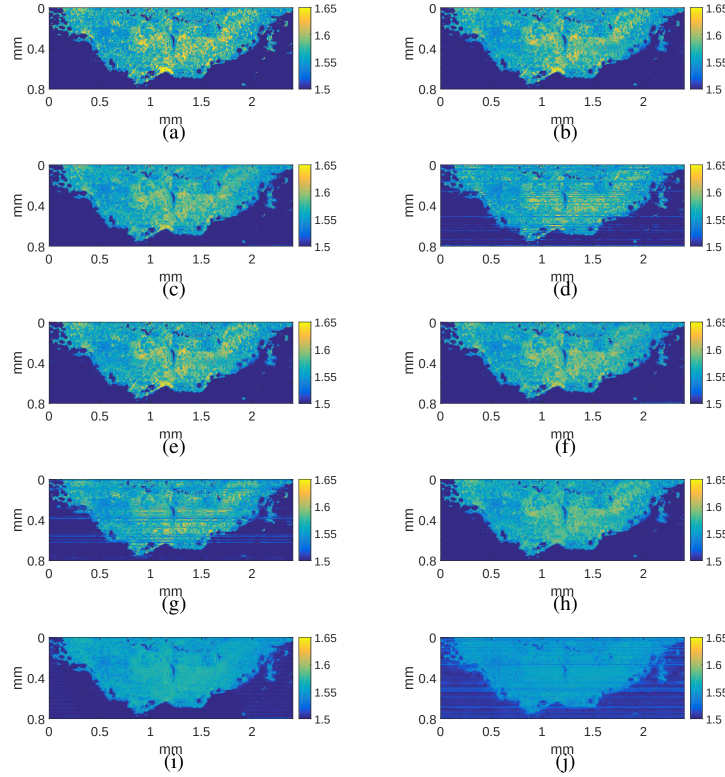

Fig. 13. Reconstruction results of impedance ($MRayl$) map estimated from human lymph node data acquired at 250 MHz: (a) original fully sample data at pixel resolution of 2 μm per 2 μm, (b-d) reconstructed images with the proposed Cauchy-AMP algorithm for spiral, diagonal and row random sampling patterns, (e-g) reconstructed images with ABE-AMP algorithm for spiral, diagonal and row random sampling patterns, (h-j) reconstructed images with ST-AMP algorithm for spiral, diagonal and row random sampling patterns. All the results correspond to a measurement ratio of 40%.

[4] J. A. Hildebrand, D. Rugar, R. N. Johnston and C. F. Quate, "Acoustic microscopy of living cells," Proc. Nat. Academy. Sci., USA Vol. 78, no. 3, pp.1656-1660, Mar. 1981.

[5] J. Mamou, D. Rohrbach, E. Saegusa-Beecroft, E. Yanagihara, J. Machi and E. J. Feleppa, "Ultrasound-scattering models based on quantitative acoustic microscopy of fresh samples and unstained fixed sections from cancerous human lymph nodes," 2015 IEEE International Ultrasonics Symposium (IUS), Taipei, pp. 1-4, Oct. 2015.

[6] K. Dabov, A. Foi, V. Katkovnik and K. Egiazarian, "Image denoising by sparse 3-d transform-domain collaborative filtering," IEEE Transactions on Image Processing, vol. 16, no. 8, pp. 2080-2095, Aug. 2007.

[7] M. Unser, P. Tafti, and Q. Sun, "A Unified Formulation of Gaussian Versus Sparse Stochastic Processes-Part I: Continuous-Domain Theory," IEEE Trans. Inf. Theory vol 60, no. 3,pp. 1945-1962. Mar. 2014.

[8] E. Candès, J. Romberg, and T. Tao, "Robust uncertainty principles: exact signal reconstruction from highly incomplete frequency information," Information Theory, IEEE Transactions on, vol. 52, pp. 489-509, Feb. 2006.

[9] D. L. Donoho, A. Maleki, and A. Montanari, "Message passing algorithms for compressed sensing," Proc. Nat. Academy Sci., vol. 106, no. 45, pp. 18914-18919, Nov. 2009.

[10] J. Tan, Y. Ma and D. Baron, "Compressive Imaging via Approximate Message Passing With Image Denoising," IEEE Transactions on Signal Processing, 63(6), pp. 2085-2092, Feb. 2015.

[11] P. R. Hill, J. H. Kim, A. Basarab, D. Kouame, D. R. Bull and A. Achim, "Compressive imaging using approximate message passing and a Cauchy prior in the wavelet domain," 2016 IEEE International Conference on Image Processing (ICIP), Phoenix, AZ, USA, 2016, pp. 2514-2518.

[12] J. Ilow and D. Hatzinakos, "Analytic alpha-stable noise modelling in a Poisson field of interferers or scatterers," IEEE Transactions on Signal Processing, vol. 46, pp. 1601-1611, Jun. 1998.

[13] T. Chernyakova, and Y.C. Eldar, "Fourier-Domain Beamforming: The Path to Compressed Ultrasound Imaging," IEEE Trans. Ultrason. Ferroelectr. Freq. Control , vol. 61, no.8, pp.1252-1267, Aug. 2014.

[14] D. Rohrbach, A. Jakob, H. Lloyd, S. Tretbar, R. Silverman, and J. Mamou, "A Novel Quantitative 500-MHz Acoustic-microscopy System for Ophthalmologic Tissues," IEEE Transactions on Biomedical Engineering, pp.715 - 724, May. 2016.

[15] L. E. Kinsler, A. R. Frey, A. B. Coppens, and J. V. Sanders, "Fundamentals of acoustics," 4th ed. New York, NY: Wiley, 2000.

[16] D. Donoho, "Compressed sensing," Information Theory, IEEE Transactions on, vol. 52, pp. 1289-1306, Apr. 2006.

[17] R. Chartrand and W. Yin, "Iteratively reweighted algorithms for compressive sensing," in Proc. IEEE Int. Conf. Acoust. Speech Signal Process. (ICASSP-08), Apr. 2008, pp. 3869-3872, Apr. 2008.

[18] J. Tropp, A. Gilbert, "Signal Recovery from Random Measurements via Orthogonal Matching Pursuit," IEEE Trans. Inf. Theory, vol. 53, no. 12, pp. 4655-4666, Dec. 2007.

[19] T. Blumensath and M. Davies, "Iterative hard thresholding for compressed sensing," Applied and Computational Harmonic Analysis, vol. 27, no. 3, pp. 265-274, 2009.

[20] D. Donoho, "De-noising by soft-thresholding," Information Theory, IEEE Transactions on, vol. 41, no. 3, pp. 613-627, 2002.

[21] C.A. Metzler, A. Maleki and R.G. Baraniuk, "From denoising to compressed sensing," arXiv preprint arXiv:1406.4175, 2014.

[22] A. Achim, A. Bezerianos, and P. Tsakalides, "Novel Bayesian multiscale method for speckle removal in medical ultrasound images," IEEE Transactions on Medical Imaging, 20(8), pp. 772-783, 2001.

[23] A. Achim and E. E. Kuruoglu, "Image denoising using bivariate α-stable distributions in the complex wavelet domain," in IEEE Signal Processing Letters, vol. 12, no. 1, pp. 17-20, Jan. 2005.

[24] M. A. Figueiredo and R. D. Nowak, "Wavelet-based image estimation: an empirical Bayes approach using Jeffreys' noninformative prior," Image Processing, IEEE Transactions on, vol. 10, no. 9, pp. 1322-1331, 2001.

[25] M. A. Kutay, A. P. Petropulu, and C. W. Piccoli, "On modelling biomedical ultrasound RF echoes using a power-law shot noise model,"

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IEEE Trans. on Ultrasonics, Ferroelectrics, and Frequency Control, vol. 48, pp. 953-968, Jul. 2001.

[26] A. Petropulu, J.-C. Pesquet, and X. Yang, "Power-law shot noise and its relationship to long-memory alpha;-stable processes," Signal Processing, IEEE Transactions on, vol. 48, pp. 1883-1892, Jul. 2000.

[27] D. L. Donoho and I. M. Johnstone, "Ideal spatial adaptation by wavelet shrinkage," Biometrika, vol. 81, pp. 425-455, Aug. 1994.

[28] D. L. Donoho, A. Maleki, and A. Montanari, "How to Design Message Passing Algorithms for Compressed Sensing," preprint, Feb. 2011.

[29] J. H. Kim, A. Basarab, P. R. Hill, D. R. Bull D. Kouame and A. Achim, "Ultrasound image reconstruction from compressed measurements using approximate message passing," European Signal Processing Conference (EUSIPCO), pp. 557-561. Aug. 2016.

[30] A. Achim, B. Buxton, G. Tzagkarakis, and P. Tsakalides, "Compressive Sensing for Ultrasound RF Echoes Using α-Stable Distribution," in 32nd Annual International Conference of the IEEE EMBS (EMBC-2010), Buenos Aires, Argentina, pp. 4304-4307, 2010.

[31] S. S. Chen, D. L. Donoho, and M. A. Saunders. "Atomic decomposition by basis pursuit," SIAM J. Sci. Comput., Vol. 20, pp. 33-61, 1999.

[32] Z. Wang, A. C. Bovik, H. R. Sheikh and E. P. Simoncelli, "Image quality assessment: from error visibility to structural similarity," IEEE Transaction on Image Processing, vol. 13, no. 4, pp. 600-612, Apr. 2004.

[33] E. Candès and J. Romberg, "Sparsity and incoherence in compressive sampling," Inverse Problems, vol. 23, p. 969, 2007.

[34] J. C.Emmanuel and W.B. Michael, "An introduction to compressive sampling," IEEE signal processing magazine, 2008.

[35] G. Kutyniok, "Theory and applications of compressed sensing," GAMM-Mitteilungen, 36(1), pp.79-101. Jul. 2013.

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